

Study on the Selection of Recycling Channels for Authorized Remanufacturing

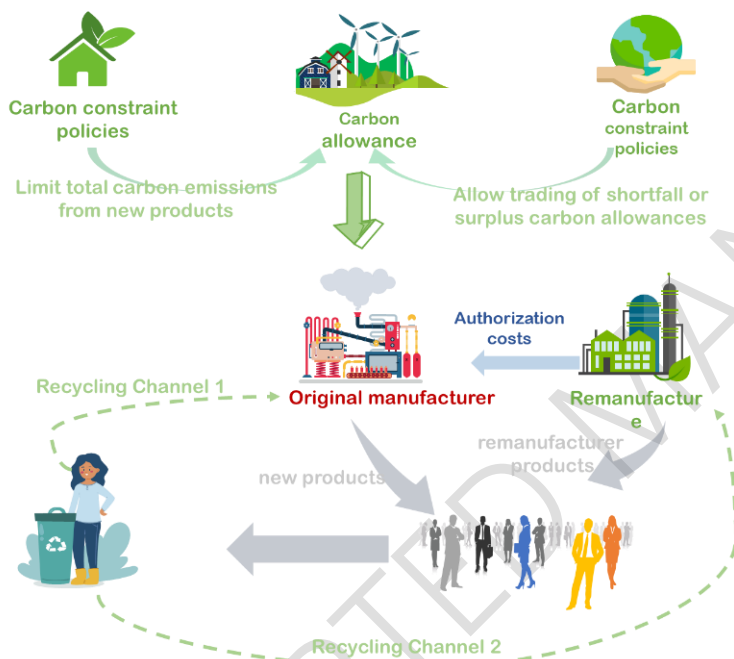
Models under Carbon Allowance

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Graphical Abstract



Abstract

To analyze the impact of allocation methods of carbon allowances on the choice of recycling channels for original manufacturers under the authorized remanufacturing model. A Stackelberg game model of original manufacturer recycling and remanufacturer recycling under the grandfathering rule and benchmarking rule is established, which assumes that both decision-making parties are completely rational, and the impacts of different allocation methods of carbon allowances on new and remanufactured products under different recycling channels are investigated. Further, this paper analyzes the impact of consumer green preference and recycling scale on remanufactured products

18 by using numerical simulation with reference to the parameter settings of related literature. The study
19 found that: (1) grandfathering rule are ineffective in promoting original equipment manufacturers'
20 investment in carbon-reducing technologies. Original equipment manufacturers (OEMs) were more
21 likely to respond to government-set grandfathering rule with strategies to increase product pricing or
22 reduce production; (2) Different carbon allowance allocation methods formulated by the government
23 will not directly affect the original manufacturers' licensing fee decisions, but they will affect the
24 original manufacturers' licensing fee decisions by indirectly acting on consumers' green consumption
25 preferences. (3) When the government formulates the grandfathering rule, the original manufacturer
26 will often choose the remanufacturer recycling channel, thus achieving a win-win situation for the
27 interests of both parties.

28 **Keywords:** Carbon allowance, Authorized remanufacturing, recycling channels, Stackelberg game.

29 **1. Introduction**

30 With the aggravation of climate change, the call for reducing carbon emissions and combating climate
31 change has been increasing (Zhou & Shan, 2023). Many countries are actively implementing carbon
32 emission reduction programs, carbon emission taxes, carbon trading, and quota systems to achieve
33 this common goal(Li et al., 2023). Led by the goal of ‘double carbon’ , China actively promotes
34 the carbon quota policy, carbon quota system becomes an important market-based instrument for
35 manufacturing enterprises to promote green transformation. As a market-based carbon emission
36 reduction policy tool (Liu et al., 2024), the carbon quota system incentivizes enterprises to optimize
37 resource allocation and reduce carbon emissions during production and operation by limiting the total
38 amount of carbon emissions and allowing trading of quotas(Xia et al., 2024). Currently, two free
39 allocation methods are mainly used: the grandfathering rule and the benchmarking rule for the
40 industry (Ji et al., 2017). The grandfathering rule is based on the past years' emission data, and the

41 industry benchmarking rule accounts for the overall emission level of the industry.

42 Under the influence of carbon quota system, manufacturing enterprises not only need to carry out
43 low-carbon technological innovation on the production side, but also pay more and more attention to
44 the green management of the whole life cycle of products (Selvanarayanan et al., 2024). As an
45 important support for the green transformation of enterprises, the recycling channel is not only the
46 main way to obtain waste resources(Hong et al., 2024), but also an important means of eliminating
47 the shortage of resources in the solid waste segment and promoting the development of a circular
48 economy(Wu et al., 2025).Remanufacturing is gradually becoming an important pathway due to its
49 significant resource-saving and carbon emission benefits(Yu, 2024) . The original manufacturer often
50 licenses the right to produce and sell the remanufactured product to the remanufacturer by charging
51 a patent license fee to a third-party independent remanufacturer, which is known as the licensed
52 remanufacturing model. This model has been successfully applied in several cases in the industry
53 (Zhou et al., 2020), such as the Volkswagen Group commissioning Volkswagen FAW Engine (Dalian)
54 Co., Ltd (VWED) to produce remanufactured engines by charging a certain amount of patent
55 licensing fees, while the sales are handled by the remanufacturer (VWED). However, the recycling
56 efficiency and quality of used products directly determine the cost and carbon emission benefits of
57 remanufactured products, and the choice of recycling channels is the key to the operational
58 effectiveness of the authorized remanufacturing model.

59 Specifically, introducing carbon quotas has significantly affected firms' choice of recycling channels.

60 On the one hand, the formulation of different carbon allowance allocation mechanisms is directly
61 related to the carbon cost burden of enterprises(Wang et al., 2019); on the other hand, the interest
62 game between the original manufacturer and the remanufacturer in the construction of recycling

63 channels also affects the implementation effect of the low-carbon strategy of enterprises(Kadeer et
64 al., 2024). Therefore, firms face multiple trade-offs between recycling scale, quality control, and
65 carbon responsibility. In addition, in high-carbon emitting industries, carbon emission constraints
66 further exacerbate this trade-off, making the rational choice of recycling channels a central challenge
67 in optimizing resource allocation and achieving carbon emission targets.

68 In summary, the carbon quota allocation method puts forward higher requirements for the selection
69 of recycling channels under the authorized remanufacturing mode. Considering the characteristics of
70 the authorized remanufacturing mode, and in order to promote the rapid development of the
71 remanufacturing industry, this paper considers three key questions: (1) How can manufacturers
72 optimize the authorization fee and the pricing of new products in order to balance the market
73 competition and profit maximization under the constraints of carbon quota? (2) How do different
74 carbon quota allocation methods affect the choice of recycling channels and competition in the
75 manufacturing/remanufacturing market? (3) How can the government and enterprises develop the
76 most effective decision-making model that balances economic and environmental benefits to achieve
77 mutual benefits?

78 **2. Literature review**

79 At present, domestic and foreign remanufacturing research focuses on different aspects. After sorting
80 out the literature, the current research hotspots focus on two aspects: firstly, the choice of
81 remanufacturing recycling channels, and secondly, the impact of carbon quota allocation methods on
82 remanufacturing.

83 In the context of the study on the selection of recycling channels, focusing on recycling channel
84 selection, Savaskan et al. (2004) investigated a closed-loop supply chain structure, including

85 manufacturers and retailers, using a game theoretic approach. Analyses show that the cost of recycling
86 in the retailer recycling channel is lower than in the manufacturer or third-party recycler recycling
87 channel. Based on this, Savaskan and Van Wassenhove (2006) studied the selection of recycling
88 channels in the presence of one manufacturer and two retailers. And then, with the emergence of the
89 carbon emission problem, more and more scholars have researched the choice of recycling channels
90 in different contexts. For example, Huang et al. (2017) conducted a study on the existence of dual
91 recycling channels in a closed-loop supply chain and found that the intensity of competition in the
92 recycling channel directly affects recycling costs, both from the perspective of the manufacturer and
93 the consumer. Lu and Li (2016) developed a recycling model in a retailer's competitive environment
94 considering electronic products' life cycle and demand pricing characteristics. Studies have shown
95 that manufacturers choose retailers to recycle when the government determines the recycling rate and
96 recycle better when recyclers determine the recycling rate. Kushwaha et al. (2022) studied the channel
97 mix of recycling channels chosen by manufacturers to maximize profits over a limited planning
98 horizon. In addition, Yang et al. (2023) have suggested that manufacturers can outsource recycling
99 activities to retailers to form a more effective price incentive mechanism. On the other hand, research
100 on the selection of recycling channels for used power batteries has also attracted extensive attention
101 in recent years. Relevant studies mainly focus on the technological innovation path for high-value
102 recycling of battery materials (Gu et al., 2024; Quan et al., 2024), as well as the operational efficiency
103 and environmental performance under different recycling modes in the closed-loop supply chain (Jiao
104 et al., 2023). Most of the above studies on recycling channel selection ignored the selection of
105 recycling channels under carbon tax policy implementation.

106 In terms of research on the impact of carbon quota allocation methods on remanufacturing, numerous

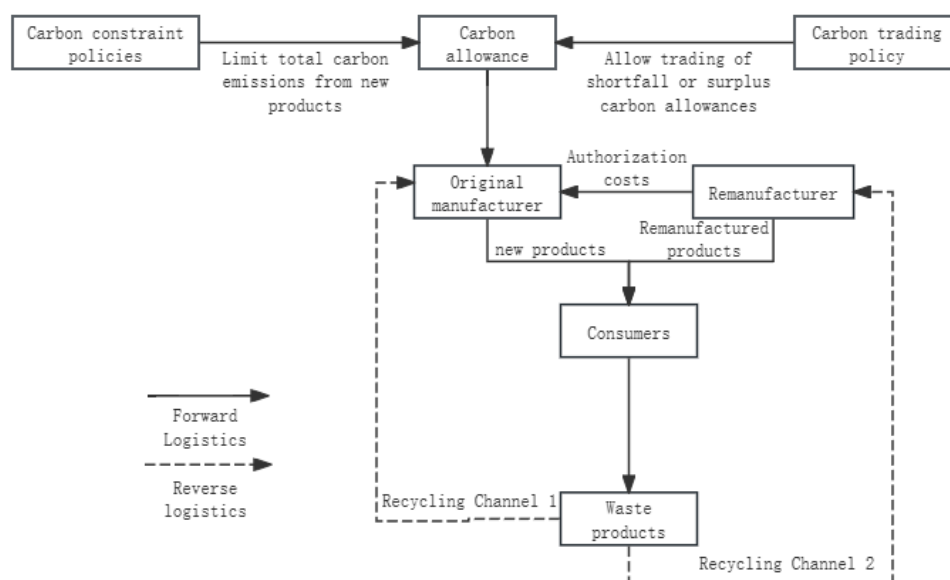
107 studies have shown that carbon allowances significantly influence key decisions on remanufacturing
108 activities by constraining and incentivizing firms' carbon emissions (Xia et al., 2023). On the one
109 hand, carbon allowances are beneficial for remanufacturing in both ordinary and green markets. They
110 can mitigate the negative impacts of total carbon emission control and carbon trading mechanisms
111 (Chai et al., 2018). On the other hand, the constraint of carbon allowances can achieve more favorable
112 production and management strategies (Shu et al., 2017). Then, with the establishment and
113 development of the carbon trading market, scholars exam attention to the enterprise production
114 pricing strategy and carbon emission reduction behavior under the carbon trading mechanism, and
115 the research began to explore the impact of carbon trading price fluctuations on the cost-benefit and
116 emission reduction incentives of the enterprise, as well as the reasonable formulation of the
117 government's carbon price (Zhu et al., 2024). In recent years, with the promotion of the
118 remanufacturing model, studies have begun to incorporate the relevant contexts. Xia et al. (2024)
119 explored the issue of the government's carbon quota allocation method and the choice of
120 remanufacturing model for original remanufacturers in the context of intellectual property protection.
121 They found that original manufacturers would choose different remanufacturing models under
122 different carbon quota allocation methods.

123 In addition, most of the previous studies adopt the traditional Gono game(Hu et al.) or complete
124 information game(Ghosh et al., 2020; Huang et al., 2021) to analyze, however, these research methods
125 fail to adequately portray the display characteristics of the power difference and decision-making
126 sequence between manufacturers and remanufacturers(Xia et al., 2023). In particular, under the
127 constraints of carbon quota policy, manufacturers, as authorized parties, usually have stronger
128 dominant power and pricing first-mover advantage, a feature that has not yet been effectively

129 reflected in traditional approaches. In contrast, the Stackelberg game, as a typical leader-follower
130 game framework(Li et al., 2024), can better portray the master-slave relationship between
131 manufacturers and remanufacturers in the context of authorized remanufacturing, and reasonably
132 reflect the decision-making sequence of different subjects and the characteristics of the interest
133 game(Xia et al., 2025). Therefore, this paper constructs a decision-making model of recycling channel
134 selection based on the Stackelberg game, which not only makes up for the shortcomings of the
135 existing research in the application of the method, but also fits the actual operation of the authorized
136 remanufacturing situation better, and has stronger theoretical value and practical guiding significance.
137 Summarizing the above literature, it is found that the literature on recycling channel selection
138 considers the impact of different recycling channels and competitive intensity on recycling costs and
139 recycling channel selection. A study on the impact of carbon quota allocation methods on
140 remanufacturing only considered the impact of carbon quota policy on the operational decision-
141 making of remanufacturing in their studies while ignoring the recycling channel selection, which is a
142 key aspect of remanufacturing. In summary, this paper concludes that the problems and shortcomings
143 of the above research content: (1) the existing research ignores the integrated impact of carbon quota
144 and different recycling channels on the recycling cost and the decision-making process of channel
145 selection; (2) there are fewer studies on what kind of systematic stability strategy combinations of the
146 carbon quota trading mechanism and recycling channels have, in particular, the existing literature
147 seldom takes into account the win-win situation of economic and environmental benefits; (3) fewer
148 literature integrates the context of intellectual property protection, especially in the process of
149 recycling waste products.

3. Model description and analysis

3.1. Description of the model



152

153 **Figure 1.** Original Manufacturer Recovery Channel Manufacturing/Remanufacturing Game Models

154

155 In this paper, we construct a remanufacturing game model consisting of an original manufacturer and
 156 a remanufacturer, and Xia et al. (2023) regards the original manufacturer as the dominant player in
 157 the game and the remanufacturer as the follower. Original manufacturers, which are responsible for
 158 the production and sale of new products protected by patents and the setting up of recycling channels
 159 for used products, are high-carbon-emitting enterprises regulated by the government's carbon tax
 160 policy. Under the carbon trading policy, the government sets the carbon trading price and determines
 161 the initial carbon emission quotas based on the grandfathering rule and the benchmarking rule,
 162 respectively. Owing to technological and financial constraints on remanufacturing, OEMs choose
 163 recycling channels to collect used products and license remanufacturing production and sales

operations to remanufacturers. Considering the protection of intellectual property rights, the OEMs charge a licensing fee so that the remanufactured products compete with new products in the market. Taking the Volkswagen Group as an example, the Volkswagen Group authorized the remanufacturing right of the engine EA888 by charging a licensing fee to Volkswagen FAW (Dalian) Co. In this paper, the manufacturing/remanufacturing game models under two recycling channels are constructed based on the different allocation methods of carbon quotas set by the government, respectively, as shown in Fig. 1.

3.2. Description of symbols

The symbols and descriptions used in this paper are specified in Table 1.

Table 1. Description of symbols

notation	description
decision	
variables	
p_{in}^j, p_{ir}^j	Denote the unit pricing of new and remanufactured products in the two recycling channels under mode j , respectively, where $j \in \{L, H\}, i \in \{OR, RR\}$
τ_i^j	denotes the recovery rate of used products from the two recycling channels under model j
z_i^j	Indicates the cost per unit of remanufacturing authorization for both recycling channels under model j
parameters	
OR, RR	Indicates original manufacturer recycling channel and remanufacturer recycling channel, respectively
L, H	Indicates historical emission method and sectoral baseline method, respectively
n, r	Indicates original manufacturer and remanufacturer, respectively

k	Indicates the scale factor for recycling used products, the larger the value, the greater the recycling cost for recycling the same amount of used products
E, α	Indicates the total amount of carbon allowances determined by the Government on the basis of the historical emissions method and the baseline carbon allowances determined on the basis of the baseline method, respectively.
q_{in}^j, q_{ir}^j	Denote the sales of new and remanufactured products from the two recycling channels under mode j, respectively
e_n, p_e	Indicates the carbon emissions per unit and the carbon trading price per unit of the new product, respectively
c_n, c_r	Representation of production uplift costs for new and remanufactured products, respectively; $c_n > c_r$
δ	Indicates the green preference coefficient of consumers, i.e., the coefficient of consumers' preference for remanufactured products, with higher values indicating that consumers are more willing to purchase remanufactured products
π_{in}^j, π_{ir}^j	Denote the profits of the original manufacturer and the remanufacturer in the two recycling channels under model j, respectively

175

176 3.3. Model functions

177 (1) Demand function

178 Referring to the research results of Chai et al. (2018) and Zhu et al. (2024), the market demand
 179 function for new and remanufactured products can be obtained as: $q_{in}^j = \frac{1-\delta-p_{in}^j+p_{ir}^j}{1-\delta}$, $q_{ir}^j = \frac{\delta p_{in}^j - p_{ir}^j}{\delta(1-\delta)}$,
 180 this leads to the derivation of the classical inverse consumer demand function for the two products
 181 as: $p_{in}^j = 1 - q_{in}^j - \delta q_{ir}^j$, $p_{ir}^j = \delta(1 - q_{in}^j - q_{ir}^j)$, where $i \in \{OR, RR, SR\}$, $j \in \{L, H\}$.

182 (2) Recycling cost

183 There is no linear relationship between the cost of recycling and the amount of recycling, and the
 184 difficulty of recycling increases with the scale of recycling (Zhu et al., 2024). According to the

classical recycling function in the studies of Zheng et al. (2021) and Huang et al. (2017), assuming that both new and remanufactured products can be sold and there is no inventory effect, the recycling rate of old products is $\tau_i = \frac{q_{ir}^j}{q_{in}^j}$, the ratio of the number of old products recycled to the number of new products sold. Assuming that the recycling cost is a convex function of the recycling quantity, we can get the recycling cost of used products as $\frac{k}{2} q_{ir}^{j^2} = \frac{k}{2} \tau_i^{j^2} q_{in}^{j^2}$, where k is the recycling coefficient of used products.

3.4. Model hypotheses

(1) It is assumed that manufacturers' decisions are made in a single cycle, in which the remanufacturers can obtain used products to meet the market demand for remanufacturing production. In this paper, we study the stable market, and the single-cycle model can be regarded as an infinite-period model for the study. In addition, the single-cycle model allows us better to analyze the comparative study of the recycling channels, reducing the analysis's complexity.

(2) Drawing on Chai et al. (2018) and Savaskan and Van Wassenhove (2006), it is assumed that the original manufacturer has sufficient channel power and is the dominant player in the supply chain, and the remanufacturer is a follower in the supply chain.

(3) Referring to the studies of Huang et al. (2017), it is assumed that the used products recovered by original manufacturers, remanufacturers, and retailers undergo a rigorous testing process and can all be used for remanufacturing production, and that there is a substitutability (not a complete substitution) between the new and remanufactured products in order to create competition in the market.

(4) This paper assumes a fully regulated carbon trading market, where the carbon price, as a key variable in the government's regulation of the market and the game between buyers and sellers, is guided by the government to be formed.

4. Modelling and solving

4.1. Modelling

(1) OEM Recovery Model (OR Model)

OEMs control the aftermarket channels for their products so they can recycle and reuse used products to maximize the use of resources. At the same time, OEMs have a clearer understanding of the structure and function of the product and can guarantee that the used product can be used for remanufacturing. In this model, the original manufacturer grants the right to remanufacture and sell the used product to a third-party remanufacturer by recycling the waste from the consumer. Each party determines the wholesale price of new and remanufactured products which retailers sell. For example, Apple recycles consumers' e-waste through a trade-in program and delegates the remanufacturing rights to Foxconn. Thus, the profit function for the original manufacturer, the remanufacturer, and the retailer in this model is:

Grandfathering rule (Model L):

$$\pi_{ORn}^L = (p_{ORn}^L - c_n)q_{ORn}^L + z_{OR}^L \cdot q_{ORr}^L - kq_{ORr}^{L^2}/2 - (e_n q_{ORn}^L - E)p_e \quad (1)$$

$$\pi_{ORr}^L = (p_{ORr}^L - c_r)q_{ORr}^L - z_{OR}^L \cdot q_{ORr}^L \quad (2)$$

In equation (1) $(p_{ORn}^L - c_n)q_{ORn}^L$ represents the original manufacturer's revenue from the production and sale of new products, $z_{OR}^L \cdot q_{ORr}^L$ represents the licensing fee charged by the original manufacturer to the authorised remanufacturer under the protection of intellectual property rights, $\frac{k}{2}q_{ORr}^{L^2}$ represents the recycling cost that the manufacturer needs to invest in to recycle the used products, $(e_n q_{ORn}^L - E)p_e$ represents the carbon trading situation of the original manufacturer under the grandfathering rule, when $e_n q_{ORn}^L - E > 0$, it represents the need to purchase additional carbon credits from the carbon trading market in order to meet the production needs of the enterprise,

when $e_n q_{ORn}^L - E < 0$, it represents that the original manufacturer can sell the remaining carbon credits in the carbon trading market to benefit. In equation (2), $(p_{ORr}^L - c_r) q_{ORr}^L$ denotes the revenue of the remanufacturer from the production and sale of units of remanufactured products.

Benchmarking rule (Model H):

$$\pi_{ORn}^H = (p_{ORn}^H - c_n) q_{ORn}^H + z_{OR}^H \cdot q_{ORr}^H - k q_{RRr}^{H^2} / 2 - (e_n - \alpha) q_{ORn}^H p_e \quad (3)$$

$$\pi_{ORr}^H = (p_{ORr}^H - c_r) q_{ORr}^H - z_{OR}^H \cdot q_{ORr}^H \quad (4)$$

(2) Remanufacturer Recovery Model (RR Model)

The remanufacturer has more specialized scrap recycling channels and comprehensive product testing technology. Under this model, the original manufacturer is responsible for the manufacture and sale of new products, and after charging a certain licensing fee, it grants to the remanufacturer the right to recycle and remanufacture the used products and the production and sale of the remanufactured products. Take BMW as an example, it has entrusted the right to recycle and remanufacture gearboxes to ZF Sales and Service (China) Co. Thus under this model, the profit function for the original manufacturer, the remanufacturer and the retailer is:

Grandfathering rule (Model L):

$$\pi_{RRn}^L = (p_{RRn}^L - c_n) q_{RRn}^L + z_{RR}^L \cdot q_{RRr}^L - (e_n q_{RRn}^L - E) p_e \quad (5)$$

$$\pi_{RRr}^L = (p_{RRr}^L - c_r) q_{RRr}^L - z_{RR}^L \cdot q_{RRr}^L - k q_{RRr}^{L^2} / 2 \quad (6)$$

Benchmarking rule (Model H):

$$\pi_{RRn}^H = (p_{RRn}^H - c_n) q_{RRn}^H + z_{RR}^H \cdot q_{RRr}^H - (e_n - \alpha) q_{RRn}^H p_e \quad (7)$$

$$\pi_{RRr}^H = (p_{RRr}^H - c_r) q_{RRr}^H - z_{RR}^H \cdot q_{RRr}^H - k q_{RRr}^{H^2} / 2 \quad (8)$$

4.2. Model Analysis

In order to obtain the optimal solution for different recycling channels under the two carbon allowance

allocation methods, Lemma 1 is first given.

Lemma 1

(i) Eq. (2) is a concave function with respect to τ_{OR}^L , and the optimal solution obtained through Eq. (2) is substituted into Eq. (1), which is a concave function with respect to q_{ORn}^L and z_{OR}^L ; Eq. (4) is a concave function with respect to τ_{OR}^H , and the optimal solution obtained through Eq. (4) is substituted into Eq. (3), which is a concave function with respect to q_{ORn}^H and z_{OR}^H .

(ii) Eq. (6) is a concave function with respect to τ_{RR}^L , and the optimal solution obtained through Eq. (6) is substituted into Eq. (5), which is a concave function with respect to q_{RRn}^L and z_{RR}^L ; Eq. (8) is a concave function with respect to τ_{RR}^H , and the optimal solution obtained through Eq. (8) is substituted into Eq. (7), which is a concave function with respect to q_{RRn}^H and z_{RR}^H .

The relevant proof process will not be described in detail. From the above, it is possible to draw conclusions:

Conclusion 1

The optimal solutions under the OR model are detailed in **Table 2**. The optimal solutions under the RR model are detailed in **Table 3**. From **Conclusion 1**, **Conclusions 2 to 8** can be obtained.

Table 2. Optimal solutions under the OR model

	L	H
z_{OR}^{j*}	$\frac{-c_r(-2+k)}{-4+k} + \frac{(-2+k + \frac{1}{2}(-4+k)(1-c_n-e_n p_e)\delta)}{-4+k}$	$\frac{-c_r(-2+k)}{-4+k} + \frac{\left(-2+k + \frac{1}{2}(-4+k)(1-c_n-(e_n-\alpha)p_e)\right)\delta}{-4+k}$
q_{ORr}^{j*}	$\frac{2c_r}{2(-4+k)\delta} + \frac{(2+c_n(-4+k)-k+e_n(-4+k)p_e)}{2(-4+k)\delta}$	$\frac{2c_r}{2(-4+k)\delta} + \frac{(2+c_n(-4+k)-k+(e_n-\alpha)(-4+k)p_e)}{2(-4+k)\delta}$
q_{ORn}^{j*}	$\frac{1-c_n-e_n p_e}{2}$	$\frac{1-c_n-(e_n-\alpha)p_e}{2}$

p_{ORr}^{j*}	$\frac{-c_r + (-3 + k)\delta}{-4 + k}$	$\frac{-c_r + (-3 + k)\delta}{-4 + k}$
p_{ORn}^{j*}	$\frac{1 + c_n + e_n p_e - 2q_r \delta}{2}$	$\frac{1 + c_n + (e_n - \alpha)p_e - 2q_r \delta}{2}$
τ_{OR}^{j*}	$\frac{-2(c_r + z_{OR}^L) - (1 + c_n + e_n p_e)\delta}{2(-1 + c_n + e_n p_e)\delta}$	$\frac{-2(c_r + z_{OR}^H) - (1 + c_n + e_n p_e)\delta}{2(-1 + c_n + e_n p_e)\delta}$

267 The optimal solutions under the RR model are detailed in Table 3. From **Conclusion 1**, **Conclusions**
268 **2** to 8 can be obtained.

269

270 **Table 3.** Optimal solutions under the RR model

271

	L	H
z_{RR}^{j*}	$\frac{\delta - c_r}{2}$	$\frac{\delta - c_r}{2}$
q_{RRr}^{j*}	$\frac{\delta(c_n + e_n p_e) - c_r}{2(2\delta + k - \delta^2)}$	$\frac{\delta(c_n + e_n p_e - \alpha p_e) - c_r}{2(2\delta + k - \delta^2)}$
q_{RRn}^{j*}	$\frac{1}{2} + \frac{\delta c_r - (2\delta + k)(c_n + e_n p_e)}{2(2\delta + k - \delta^2)}$	$\frac{1}{2} + \frac{\delta c_r - (2\delta + k)(c_n + e_n p_e - \alpha p_e)}{2(2\delta - \delta^2 + k)}$
p_{RRr}^{j*}	$\frac{\delta}{2} + \frac{\delta(1 - \delta)c_r + \delta(\delta + k)(c_n + e_n p_e)}{2(2\delta + k - \delta^2)}$	$\frac{\delta}{2} + \frac{\delta(1 - \delta)c_r + \delta(\delta + k)(c_n + e_n p_e - \alpha p_e)}{2(2\delta + k - \delta^2)}$
p_{RRn}^{j*}	$\frac{1 + c_n + e_n p_e}{2}$	$\frac{1 + c_n + (e_n - \alpha)p_e}{2}$
τ_{RR}^{j*}	$\frac{\delta(c_n + e_n p_e) - c_r}{(2\delta + k)(c_n - e_n p_e) - \delta^2 - \delta c_r}$	$\frac{\delta(c_n + c_n p_e - e_n p_e) - c_r}{2(\delta - k - \alpha p_e) - c_r}$

272 **Conclusion 2** Comparative analysis of authorization fees for recycling channels under different
273 allocation methods of carbon allowances:

274 It is known that $z_{RRn}^{L*} = z_{RRr}^{H*}$, different allocation of carbon allowances under the remanufacturer
275 recycling channel does not affect the original manufacturer's remanufacturing authorization cost
276 decisions, i.e. different allocation of carbon allowances cannot change the authorization cost of the
277 original manufacturer, which is consistent with the conclusion of Xia et al. (2023). In conjunction
278 with the relevant findings, original manufacturers tend to shift the benefits of remanufacturers by
279 increasing the unit pricing of new products rather than adjusting the licensing fees. Selling more

280 remanufactured products increases the profit of the original manufacturer, and increasing the unit
281 licensing fee increases the cost of the remanufacturer, which reduces the incentive of the
282 remanufacturer to engage in remanufacturing and leads to a reduction in the benefits for both parties.
283 It is known that $z_{ORn}^{L*} > z_{ORr}^{H*}$, that is, when the original manufacturer is responsible for recycling, the
284 cost of authorization under the grandfathering rule is higher than that under the benchmarking rule.
285 This is because in the case where the original manufacturer is responsible for recycling, the
286 grandfathering rule will result in insufficient allowances due to its high emission level in the past,
287 which will in turn increase its authorization fee. In contrast, the benchmarking rule, which authorizes
288 allowances based on the average or advanced level of the whole industry, can better reflect the
289 effectiveness of manufacturers in reducing emissions after low-carbon transformation and alleviate
290 the pressure on their carbon costs. This contrasts with Zhu et al. (2024) that the cost of
291 remanufacturing authorizations is unaffected by government carbon trading policies, as the latter
292 treats the cost of authorizations as a relatively rigid decision that is unresponsive to changes in carbon
293 policy, focusing on emissions investments and production control. In contrast, we model the cost of
294 authorization as a strategic variable, and our findings highlight how carbon policy can reshape pricing
295 decisions across the supply chain beyond production-related costs.

296 Management insights: Different ways of allocating carbon allowances are not effective in changing
297 the licensing cost decisions of OEMs. However, it is found that an increase in the demand for
298 remanufactured products will have a positive impact on the economic performance of both original
299 manufacturers and remanufacturers, and will also help to promote socio-economic circularity. In view
300 of this, the Government should strengthen its support for the remanufacturing industry through
301 measures such as lowering the taxes associated with remanufactured products, providing subsidies

302 for purchases, and raising public awareness of the reuse of used and end-of-life products.

303 **Conclusion 3** Impact of the carbon quota allocation methodology on product prices in the two
304 recycling channels:

305 (i) $p_{ORn}^{L*} > p_{ORn}^{H*}$, $p_{ORr}^{L*} = p_{ORr}^{H*}$;

306 (ii) $p_{RRn}^{L*} > p_{RRn}^{H*}$, $p_{RRr}^{L*} > p_{RRr}^{H*}$;

307 **Conclusion 3** shows that in the OEMs recycling channel, pricing of new products under the
308 grandfathering rule is higher than under the benchmarking rule, while changes in the carbon
309 allowance allocation method do not affect the price of remanufactured products. This is mainly due
310 to additional carbon allowance purchase costs and technology adaptation costs associated with high
311 emissions. Prices of remanufactured products, on the other hand, are not affected by the way carbon
312 allowances are allocated. In the recycling channel of remanufacturers, prices of new and
313 remanufactured products are higher under the grandfathering rule than under the benchmarking rule.
314 The main reason for this is that while the Government's carbon tax policy has forced original
315 manufacturers to reduce carbon emissions, the grandfathering rule, which determines carbon
316 allowances based on historical data, provides a scope of protection and fails to effectively promote
317 emissions reductions, leading original manufacturers to increase product pricing and reduce
318 production to meet emissions reduction targets, while at the same time increasing the pricing of
319 remanufactured products in order to increase profits. The benchmarking rule, which determines
320 carbon allowances based on industry carbon emission data, puts pressure on high-emission
321 manufacturers, who tend to invest in emission reduction technologies rather than increase product
322 pricing to cope with high carbon emission costs. As a result, both products are priced higher under
323 the grandfathering rule.

324 Management insights: Under the grandfathering rule, OEMs with higher carbon emissions usually
325 compensate for the cost of carbon emissions by increasing the unit pricing of their products and
326 passing it on to consumers. In order to safeguard consumers' rights, the government should consider
327 adopting the benchmarking rule, a move that not only ensures consumers' interests, but also helps to
328 incentivize OEMs to invest in carbon-reducing technologies, thus achieving a win-win situation. In
329 the long run, companies should also incorporate carbon reduction into their sustainable development
330 strategies and integrate environmental protection concepts into their corporate cultures and business
331 models in order to adapt to increasingly stringent environmental regulations and consumer
332 preferences.

333 **Conclusion 4** Impact of Carbon Allowance Allocation Methods on Product Sales in Two Recycling
334 Channels:

335 (i) $q_{ORn}^L < q_{ORn}^H$, $q_{ORr}^L < q_{ORr}^H$;

336 (ii) $q_{RRn}^L < q_{RRn}^H$, $q_{RRr}^L > q_{RRr}^H$;

337 **Conclusion 4** shows that sales of new and remanufactured products under the grandfathering rule are
338 always higher than the industry benchmarking rule when the original manufacturer is responsible for
339 recycling. Combined with **Conclusion 2**, under the grandfathering rule, OEMs and remanufacturers
340 will choose to raise the unit pricing of their products, while OEMs will choose to reduce the
341 production of new products in order to reduce carbon emissions, thus weakening the purchasing
342 behavior of consumers. When the remanufacturer is responsible for recycling, under the
343 grandfathering rule, the original manufacturer raises the unit pricing of the new product, which leads
344 to an increase in sales of the remanufactured product under market competition.

345 Management Insight: If the government adopts the grandfathering rule, it will encourage the sales of

346 remanufactured products using the recycling channel of remanufacturers and increase the motivation
347 of consumers to buy remanufactured products, while for remanufactured products using the recycling
348 of the original manufacturer, the sales of remanufactured products will be reduced due to the increase
349 in the pricing of remanufactured products per unit in the competitive market game, so the government
350 should understand the actual situation of the enterprises and combine it with the trading mechanism
351 of the carbon market to formulate a more targeted carbon allowance allocation method to enhance
352 environmental benefits. Therefore, the government should understand the actual situation of the
353 enterprises and combine the carbon market trading mechanism with the carbon market trading
354 mechanism to formulate a more targeted carbon quota allocation method to enhance the
355 environmental benefits.

356 **Conclusion 5** Impact of the carbon quota allocation method on the recycling rate of used products
357 from two recycling channels:

358 (i) $\tau_{OR}^{L*} > \tau_{OR}^{H*}$

359 (ii) $\tau_{RR}^{L*} > \tau_{RR}^{H*}$

360 **Conclusion 5** shows that the recycling rate of used products when the Government allocates carbon
361 allowances based on the grandfathering rule is always higher than that of the benchmarking rule. The
362 combination of **Conclusion 3** and **Conclusion 4** shows that under the grandfathering rule, the sales
363 volume of remanufactured products can be improved, and the incentive to recycle used products may
364 be strengthened, thus increasing the recycling rate. In addition, under the benchmarking rule, the price
365 of new products is lower, and thus the sales volume of new products can be improved, and under the
366 influence of market competition, the consumer's demand for remanufactured products is reduced, so
367 that the incentive of enterprises to recycle used products may be relatively low which leads to a

368 decrease in the recycling rate of used and end-of-life products. However, observation of **Conclusion**
369 **4** reveals that when the manufacturer is responsible for recycling used products, the sales of
370 remanufactured products are lower under the grandfathering rule than the benchmarking rule, but the
371 recycling rate of used products is higher, which is because the original manufacturer under the
372 grandfathering rule may participate in the recycling of used products more actively in order to obtain
373 more carbon allowances, as this can assist in proving that it is taking measures to reduce carbon
374 emissions. Therefore, although sales of remanufactured products are lower, the recycling rate of used
375 products may be higher due to the increased incentive to recycle used products.

376 Management insights: When the original manufacturer is responsible for recycling used products, in
377 order to avoid a situation where the original manufacturer passively recycles more used products in
378 order to obtain more carbon quotas and a backlog of remanufactured products occurs, the Government
379 should take into account the enterprises' responses when setting carbon quotas and adopt a more
380 appropriate carbon quota allocation method. When remanufacturers are responsible for recycling used
381 products, in order to encourage the development of the remanufacturing industry, the Government
382 should set a lower carbon quota to limit the production activities of the original manufacturers so as
383 to promote the sale of remanufactured products.

384 Governments should adopt carbon tax policies to limit the negative environmental impacts of
385 manufacturing processes. Therefore, in order to analyze the environmental impacts of the different
386 allocation of carbon allowances in the two recycling channels, the environmental impacts of new and
387 remanufactured products are considered to be: $e_i^j = e_n q_{in}^j + e_r q_{ir}^j$.

388 **Conclusion 6** Environmental impacts of two recycling channels under different allocation of carbon
389 allowances:

390 (i) $e_{OR}^L < e_{OR}^H$;

391 (ii) $e_{RR}^L < e_{RR}^H$;

392 Comparison with Savaskan and Van Wassenhove (2006)'s research, this paper further talks about the
393 environmental impacts of different ways of carbon quota allocation under different recycling channels,
394 taking corporate responsibility and government benefits into view. **Conclusion 6** shows that the
395 environmental impacts of both recycling channels under the grandfathering rule are always weaker
396 than those of the benchmarking rule. This is because the volume of product sales is directly linked to
397 the environmental impacts, and **Conclusion 4** shows that the volume of product sales under the
398 grandfathering rule is always lower than that of the benchmarking rule. However, we find a situation
399 in (ii) of **Conclusion 4** and (ii) of **Conclusion 6**: i.e., in the recycling channel of remanufacturers, the
400 sales volume of remanufactured products under the grandfathering rule is lower than that of the
401 benchmarking rule, but the impact on the environment is lower, which is due to the fact that the
402 difference in the sales volume of new products under the different allocation methods is greater than
403 that of remanufactured products, which means that the impact on the environment caused by the new
404 products is greater than that caused by the remanufactured products. This is because the difference in
405 sales of new products is greater than the difference in sales of remanufactured products under the
406 different allocation methods. Combined with the sales volume, we can see that the environmental
407 impact of the grandfathering rule is lower than that of the benchmarking rule.

408 Management insights: Strict allocation of carbon allowances under a carbon trading policy can have
409 a significant impact on both the economic and environmental benefits of enterprises, which means
410 that the government should develop a mechanism for allocating carbon allowances that achieves a
411 "win-win" situation. The baseline law provides an incentive for companies to take more proactive

environmental measures to reduce their carbon emissions in order to comply with the baseline requirements and obtain additional carbon allowances. This competitive mechanism helps to promote environmental innovation and technological advancement, improve resource utilization efficiency and reduce negative impacts on the environment. It can also increase the sales volume of recycled products and consumer demand for recycled products, thereby promoting the development of the recycling industry.

Conclusion 7 Impact of Carbon Allowance Allocation Methods on Manufacturers' and Remanufacturers' Profits:

$$(i) \frac{\partial \pi_{ORn}^L}{\partial E} > 0, \frac{\partial \pi_{ORr}^L}{\partial E} = 0, \frac{\partial \pi_{ORn}^H}{\partial \alpha} > 0, \frac{\partial \pi_{ORr}^H}{\partial \alpha} < 0;$$

$$(ii) \frac{\partial \pi_{RRn}^L}{\partial E} > 0, \frac{\partial \pi_{RRr}^L}{\partial E} = 0, \frac{\partial \pi_{RRn}^H}{\partial \alpha} > 0, \frac{\partial \pi_{RRr}^H}{\partial \alpha} < 0;$$

$$(iii) \pi_{ORn}^L > \pi_{ORn}^H, \text{ when}$$

$$e_n > \frac{4c_r + (4 + 2c_n(-4 + k) + 4p_e\alpha - k(2 + p_e\alpha))\delta}{2(-4 + k)p_e\delta}$$

$$(iv) \pi_{ORr}^L > \pi_{ORr}^H, \text{ when}$$

$$e_n > \frac{4c_r k(-1 + \delta) + \delta(k^2(2 + p_e\alpha) - 2c_n(-4 + k)(-2 + k - 4\delta))}{2(-4 + k)p_e(-2 + k - 4\delta)\delta} + \frac{8(2 + p_e\alpha)(1 + 2\delta) - 2k(4 + 6\delta + p_e\alpha(3 + 2\delta))}{2(-4 + k)p_e(-2 + k - 4\delta)\delta}$$

$$(v) \pi_{RRn}^L > \pi_{RRn}^H, \text{ when}$$

$$\frac{E}{\alpha} > \frac{1}{4} \left(2 + \frac{2c_r\delta - 2(c_n + e_np_e)(k + 2\delta) + p_e\alpha(k + 2\delta)}{k - (-2 + \delta)\delta} \right)$$

$$(vi) \pi_{RRr}^L > \pi_{RRr}^H$$

Conclusion 7 shows that: in the original manufacturer recycling channel, the profit of the original manufacturer increases with the total amount of carbon allowances, while the profit of the remanufacturer is not related to the total amount of carbon allowances under the grandfathering rule and decreases with the increase of carbon allowances under the benchmarking rule; in the recycling

434 channel of the remanufacturer, the profit of the remanufacturer is not directly related to the total
435 amount of carbon allowances under the grandfathering rule and is a decreasing function of total
436 amount of carbon allowances under the benchmarking rule, while the profit of the original
437 manufacturer always has an increasing function. In the remanufacturer recycling channel, the profit
438 of the remanufacturer is not directly related to the total amount of carbon allowances under the
439 grandfathering rule and is a decreasing function of the total amount of carbon allowances under the
440 benchmarking rule, while the profit of the original manufacturer is always an increasing function. It
441 is worth noting that the profit of remanufacturers under the grandfathering rule is higher than that of
442 the benchmarking rule. We find that the profit of the original manufacturer always increases with the
443 increase of the total amount of carbon allowances, and the combination of **Conclusion 3** and
444 **Conclusion 4** shows that the larger the total amount of carbon allowances, the slightly lower the
445 government's carbon emission requirement for the enterprise, and the more new products the
446 enterprise produces and sells. In addition, we find that for the comparison of profits under the two
447 methods, there is a relationship with the unit carbon emissions of new products.

448 Management Insight: With the increasing environmental pollution problem, the government has
449 become increasingly strict in regulating carbon emissions of enterprises. This means that companies
450 will face a gradually decreasing total initial carbon allowance allocation, which will directly affect
451 their profitability. To cope with this challenge, companies need to increase their investment in carbon
452 reduction areas to lower the carbon emissions of their products and maintain a competitive edge in
453 the carbon emissions market. For manufacturers, it's time to take action to reduce carbon emissions.
454 At the same time, co-operating with fellow companies and investing in carbon reduction projects will
455 help to reduce costs, improve efficiency and move the industry towards more sustainable development.

Such co-operation will not only help to meet the government's stringent requirements on carbon emissions, but will also bring long-term economic and environmental benefits to businesses.

5. Numerical analysis

5.1. Parameter settings and data sources

In order to further validate the conclusions of this study, and to deeply analyze the green consumption preference of consumers who are affected by the government's promotion of green consumption concepts, combined with the changes in the scale of recycling by enterprises due to the change in consumers' concepts, we study the changes in the decision-making behaviors of each supply chain participant in terms of the pricing sales of the remanufactured products, as well as the changes in the licensing decision-making costs of the original manufacturer.

This paper takes Volkswagen FAW (Dalian) as the empirical object, considering the investment problem of remanufacturing technology, and authorizes the recycling and remanufacturing production of EA888 engine to Volkswagen FAW (Dalian) Co. Ltd, which means that the remanufacturer is in charge of recycling the used engine and producing and selling it. In this paper, MATLAB is used for numerical simulation and analysis. According to the data released by China Association of Automobile Manufacturers (CAAM) on remanufacturing of cycling parts, remanufactured engines can save 50% of the production cost compared with the new engines, so we assume that $c_n = 0.2$, $c_r = 0.1$.

Other model parameters are set with reference of Xia et al. (2023) and Zhu et al. (2024). and typical values from domestic carbon tax policies. Specifically, we set the carbon price $p_e = 0.3$ the baseline carbon allowances $\alpha = 0.4$, the unit carbon emission of new products $e_n = 1$, recovery scale factor $k \in (0,1]$, consumer green preference factor $\delta \in (0,1]$. While no raw firm-level data is

used, the parameter settings follow standard theoretical modeling practices to ensure comparability and consistency with existing studies.

5.2. Impact of δ and k on unit mandate costs

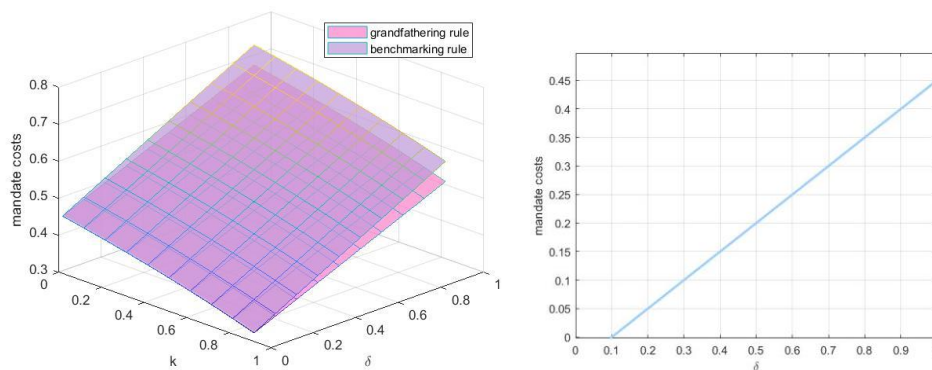


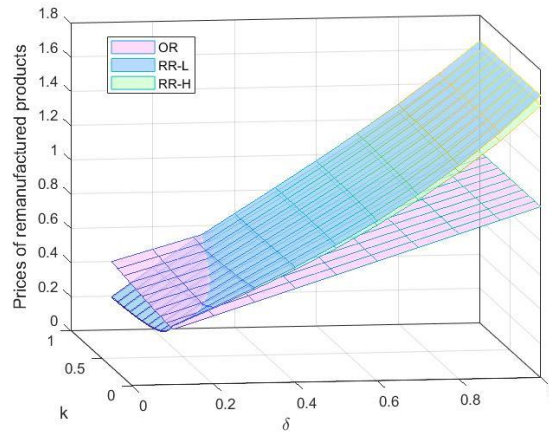
Figure 2. Impact of δ and k on the cost of unit authority under the historical and baseline approaches

As can be seen from the left panel of Fig.2, in the OEM recycling channel, the grandfathering rule mitigates to a certain extent the cost fluctuations due to the expansion of recycling scale and the enhancement of consumers' green preference. This is because the grandfathering rule allows firms to enjoy a more generous allocation of allowances at the initial stage, but the further expansion of the recycling scale with increasing green preference leads to complex non-linear changes in the authorization costs.

As can be seen from the right panel of Fig.2, in the remanufacturer recycling channel, the unit authorization cost is the same under both carbon allowance allocation methods. However, the unit authorization cost is positively correlated with consumers' green consumption preference, which is because the increase in demand for remanufactured products will cause a certain impact on the original manufacturer, and the profit of the original manufacturer will be reduced by it, and in order to increase the profit of the enterprise, the original manufacturer tends to increase the production cost of the remanufacturer through the increase of the unit authorization cost, which makes the remanufacturer increase the unit retail price of the product in order to reduce its Growing market

497 demand

498 *5.3. Impact of δ and k on unit retail prices of remanufactured products*



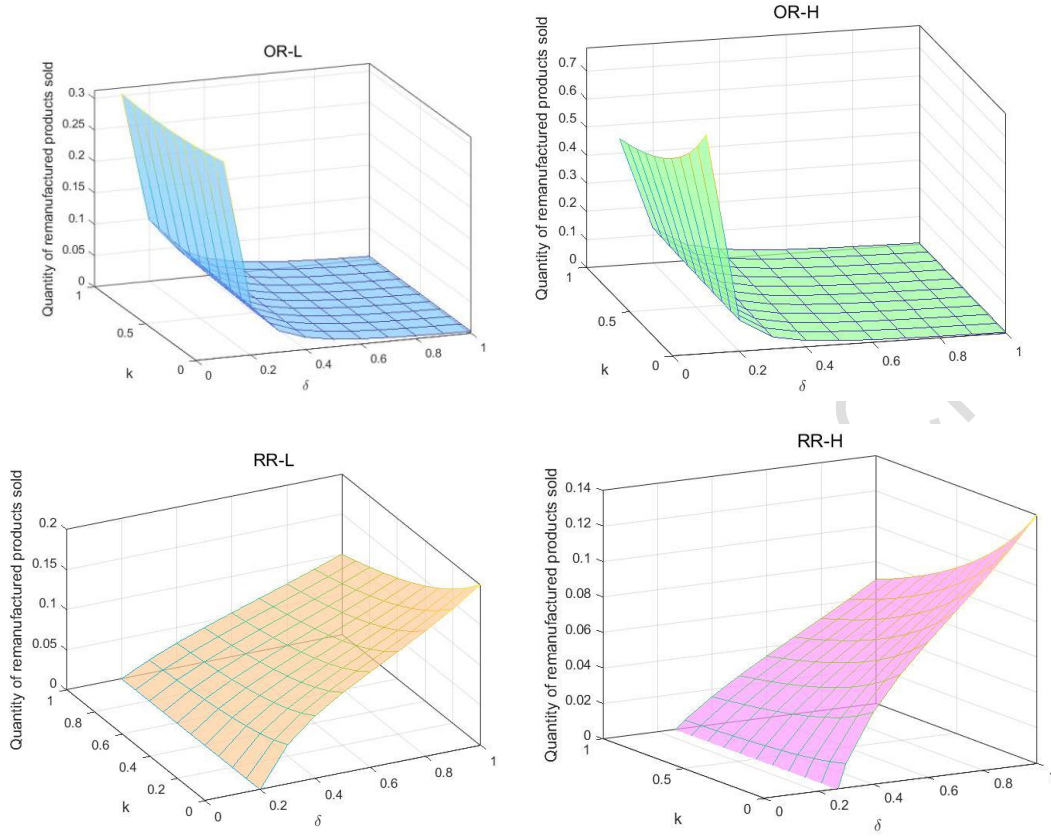
499

500 **Figure 3.** Impact of δ and k on unit retail prices of remanufactured products under the historical and baseline
501 approaches

502 As can be seen from Figure 3, there is no significant difference between the two carbon quota
503 allocation methods in the recycling channel of original manufacturers, which suggests that when
504 original manufacturers have strong control and integration advantages in the recycling process, they
505 can smoothly meet the carbon quota requirements through internal synergy and overall control. The
506 retail price of remanufactured products is positively correlated with the recycling scale factor and
507 consumers' green consumption preference under the two allocation methods of carbon allowances,
508 because when the demand for remanufactured products increases, the remanufacturer needs more
509 resources and labor to recycle, upgrade and produce the remanufactured products, and these
510 additional costs lead to the rise in the cost of remanufactured products. In addition, as consumers'
511 green consumption preference increases, the licensing fee also increases gradually, so it can be seen
512 that the original manufacturer will control the unit licensing fee decision in order to put more cost
513 pressure on the remanufacturer, and in order to safeguard the profit, the remanufacturer will have to
514 respond to this by raising the unit retail price of the remanufactured product in order to safeguard the

515 profit in the face of the increasing cost pressure and competition in the marketplace.

516 *5.4. Impact of δ and k on the quantity of remanufactured products sold*



518
519 **Figure 4.** Impact of δ and k on the quantity of remanufactured products sold under the historical and baseline
520 methods

521 As can be seen in Figure 4, the sales volume of remanufactured products in the original manufacturer's
522 recycling channel, both in the grandfathering rule (OR-L) and the industry benchmarking rule (OR-
523 H), tends to decrease with the increase of the recycling scale factor k and the enhancement of the
524 consumer's green consumption preference δ , which suggests that, in the case of the original
525 manufacturer's control of the recycling channel, the larger scale of recycling and the higher green
526 preference may lead to the remanufactured products to be less competitive in the market. In addition,
527 the downward trend is more obvious in the historical emissions rule compared to the industry
528 benchmarking rule, which suggests that under the historical emissions rule, the original manufacturer

529 faces greater pressure on carbon costs under high recycling scale, and transfers production costs to
530 the remanufacturer through the licensing fee, which inhibits the sales of remanufactured products.

531 Sales of remanufactured products in the remanufacturer's recycling channel increase significantly
532 with an increase in the recycling scale factor k and an increase in consumers' green consumption
533 preference δ . However, the industry benchmarking rule shows a smaller increase in sales relative to
534 the historical grandfathering rule, which may be due to the fact that the historical grandfathering rule
535 provides more flexibility in the recycling channel when the remanufacturer controls the recycling
536 channel, allowing the remanufacturer to utilize the recycling resources more efficiently, which leads
537 to an increase in sales of remanufactured products.

538 The numerical analysis results show that regardless of the carbon quota allocation mode adopted by
539 the government, the increase of consumer green preference δ and recycling scale factor k will
540 have a significant positive effect on the price of remanufactured products; meanwhile, under the
541 environment of market competition game, original manufacturers will increase the licensing fee
542 accordingly in order to transfer the cost pressure brought by the carbon quota policy. This
543 phenomenon shows obvious differences under different recycling channel modes: when the original
544 manufacturer controls the recycling channel, the sales of remanufactured products, on the contrary,
545 show a decreasing trend with the increase of consumer green preference and recycling scale factor.

546 This implies that in the case of higher recycling cost or higher consumer green preference, the cost
547 pass-through effect triggered by the increase of licensing fee by the OEM will significantly inhibit
548 the competitiveness of the remanufacturer in the market. Therefore, under the market environment of
549 high cost and strong green preference, the OEM-led recycling channel selection needs to carefully
550 consider the strategic setting of licensing fees to avoid the sales decline of remanufactured products

551 being too obvious. And when the recycling channel is dominated by the remanufacturer, the sales
552 volume of remanufactured products increases with
553 δ and k increase significantly, suggesting that under this channel model, remanufacturers can more
554 effectively cope with high-cost or strong green preference environments and realize market share
555 expansion. In summary, the numerical simulations in this study highlight the significant effects of
556 changes in consumer preferences and recycling costs on the strategic choices of different recycling
557 channels, and the model conclusions are most robust in the context of moderate consumer preferences
558 and moderate recycling costs; under extreme parameter condition, firms need to be more cautious in
559 applying the strategic recommendations proposed in this paper.

560 **6. Conclusions, limitation and research prospects**

561 *6.1. Conclusions*

562 This paper constructs a closed-loop supply chain consisting of an original manufacturer and a
563 remanufacturer under an authorized remanufacturing model, based on the original manufacturer
564 recycling channel and the remanufacturer recycling channel respectively, and compares the impacts
565 of unit authorization cost, product price, sales volume, recycling rate of used products, the
566 environment and the profit of the enterprise according to the two ways of allocating the government's
567 carbon allowances: grandfathering rule and the benchmarking rule, so as to provide enterprises with
568 the optimal choice of recycling channels from the perspectives of both environmental and economic
569 benefits, to provide enterprises with the optimal choice of recycling channels. The main conclusions
570 of this paper are as follows:

571 (1) The grandfathering rule set by the Government is not effective in promoting original
572 manufacturers to invest in carbon-reducing technologies. Instead, OEMs tend to meet emission

573 reduction requirements by raising product prices or reducing production, rather than proactively
574 adopting cleaner technologies. Moreover, under competitive market pressure, they may also increase
575 the pricing of new products to enhance profitability. In contrast, the benchmarking method allocates
576 carbon allowances based on industry-wide emission standards, imposing greater pressure on high-
577 emission enterprises. Under the combined constraints of carbon trading and market competition, these
578 firms are more inclined to invest in low-carbon technologies rather than simply shifting carbon costs
579 through price increases.

580 (2) Whether or not the way carbon allowances are allocated affects the decision to authorize fees
581 depends on the dominant party in the recycling channel. When recycling is the responsibility of the
582 remanufacturer, the authorization fee set by the original manufacturer remains the same under
583 different carbon allowance policies, in which case the original manufacturer prefers to adjust the
584 pricing of the new product to make profit rather than playing the game by modifying the authorization
585 fee. However, when the original manufacturer assumes responsibility for recycling, the situation
586 changes significantly: the authorization fee under the grandfathering rule is higher than that under the
587 baseline rule. This is due to the fact that the grandfathering rule allocates allowances based on past
588 emission records, which results in higher carbon constraints on OEMs, which tend to increase the
589 authorization fee to pass on the cost, while the benchmarking rule allocates allowances based on a
590 uniform standard for the benchmarking rule, which is a better reflection of their emission reduction
591 effectiveness and eases the burden of carbon costs.

592 (3) The carbon allocation mechanism significantly affects the preference for recycling channels. This
593 preference is largely due to the OEMs' strategic responses under this allocation scheme, where they
594 are more likely to raise unit product prices and reduce output to meet carbon reduction targets. The

595 increase in new product prices enhances the market competitiveness of remanufactured products,
596 thereby boosting their sales and encouraging remanufacturers to intensify efforts in collecting end-
597 of-life products. Within this carbon quota framework, remanufacturer-led recycling not only supports
598 corporate carbon mitigation but also facilitates resource reuse and improves product circularity. As a
599 result, this approach yields both environmental and economic benefits. Therefore, the historical
600 emission method plays a positive role in guiding enterprises toward remanufacturer-based recycling
601 strategies and contributes meaningfully to the advancement of a circular economy.

602 (4) Numerical analysis shows that, regardless of the carbon allowance allocation method adopted by
603 the government, an increase in consumer green preference (δ) and recycling scale factor (k) positively
604 affects the price of remanufactured products and simultaneously drives OEMs to increase licensing
605 fees. In the remanufacturer-led recycling scenario, our results are consistent with Zhu et al. (2024),
606 who conclude that licensing fees remain unaffected by the carbon allocation mechanism. However,
607 when considering the OEM-led recycling scenario, our results diverge significantly from Zhu et al.'s
608 findings. We observe that the licensing fee varies considerably with the carbon allowance allocation
609 method, with higher fees under the benchmarking rule compared to the grandfathering rule. This is
610 due to the stronger carbon cost pressure imposed by benchmarking, prompting OEMs to transfer costs
611 via licensing fees. Furthermore, OEM-led recycling offers greater strategic flexibility under dual
612 pressures from carbon regulation and market competition, enabling OEMs to better manage
613 remanufacturing competition and optimize supply chain profits.

614 *6.2. Limitations and research prospects*

615 Although this study has made some progress based on existing research, there are still some
616 limitations. Although this paper has made initial progress in theoretical modeling and numerical

simulation, there are still some limitations. First, the modeling in this paper is based on a single-cycle static Stackelberg game model, which does not take into account the evolution of recycling behavior in a multi-cycle dynamic situation, and may underestimate the room for long-term strategy adjustment. Second, key parameters such as consumers' green preference and recycling scale are mainly set with reference to the existing literature. Although this is a common modeling approach in theoretical research, which ensures the consistency of the model in terms of resolvability and comparison with the literature, it also lacks the empirical calibration of actual enterprise data, and the extrapolation of conclusions still needs to be further strengthened. In addition, this paper assumes complete information symmetry and does not introduce game complexity factors such as information asymmetry and behavioral preferences, which are more common in reality.

Future research can be carried out in the following aspects: first, constructing a multi-cycle dynamic decision model to analyze the dynamic evolution of recycling channels and pricing strategies; second, introducing uncertainty factors, such as carbon price fluctuations, recycling cost perturbations, etc., to enhance the adaptability and robustness of the model; third, combining with the actual enterprise or industry data, empirically verifying the model to enhance the realistic feasibility and policy guidance value of the conclusions; Fourth, we will further explore the collaborative recycling strategy after the intervention of platform-type enterprises or third-party data platforms, so as to expand the research space of the closed-loop supply chain in the digital economy environment.

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Appendix

Proof of Lemma 1

Substituting $p_{ORn}^L = 1 - q_{ORn}^L - \delta q_{ORr}^L$, $p_{ORr}^L = \delta(1 - q_{ORn}^L - q_{ORr}^L)$, $q_{ORr}^L = \tau_{ORn}^L q_{ORn}^L$ into Eq. (2), one obtains:

$$\pi_{ORr}^L = [\delta(1 - q_{ORn}^L - q_{ORr}^L) - c_r] \tau_{ORn}^L q_{ORn}^L - z_{OR}^L \tau_{OR}^L q_{ORn}^L \quad (A.1)$$

Taking first-order and second-order partial derivatives of Eq. (A.1) with respect to τ_{OR}^L respectively, yields:

$$\frac{\partial \pi_{ORs}^L}{\partial \tau_{OR}^L} = -q_{ORn}^L (c_r + z_{OR}^L + \delta(-1 + q_{ORn}^L + 2\tau_{OR}^L q_{ORn}^L))$$

$$\frac{\partial^2 \pi_{ORs}^L}{\partial (\tau_{OR}^L)^2} = -2\delta q_{ORn}^L < 0$$

Since its second order derivative is 0, equation (2) is concave with respect to τ_{OR}^L .

Letting the first-order partial derivative be 0, we get $\tau_{OR}^L = \frac{c_r + z_{OR}^L + \delta(-1 + q_{ORn}^L)}{2q_{ORn}^L}$, and substituting this into Eq. (1), we get:

$$\begin{aligned} \pi_{ORn}^L = & \left(1 - q_{ORn}^L - \delta \frac{c_r + z_{OR}^L + \delta(-1 + q_{ORn}^L)}{2} - c_n \right) q_{ORn}^L \\ & + z_{OR}^L \frac{c_r + z_{OR}^L + \delta(-1 + q_{ORn}^L)}{2} \\ & - \frac{k}{2} \frac{(c_r + z_{OR}^L + \delta(-1 + q_{ORn}^L))^2}{4} - (e_n q_{ORn}^L - E) p_e \end{aligned} \quad (A.2)$$

The first and second order partial derivatives of Eq. (A.2) with respect to z_{OR}^L and q_{ORn}^L are obtained:

$$\begin{aligned} \frac{\partial \pi_{ORn}^L}{\partial z_{OR}^L} &= \frac{-c_r(-2+k) + (-2+k+(-4+k)-q_{ORn}^L)\delta}{-4+k}, \quad \frac{\partial \pi_{ORn}^L}{\partial q_{ORn}^L} = q_{ORn}^L - \frac{4(-1+c_n+e_n p_e+2)q_{ORn}^L}{8+(-4+k)\delta^2} \\ \frac{\partial^2 \pi_{ORn}^L}{\partial (q_{ORn}^L)^2} &= -2 - \frac{1}{4}(-4+k)\delta^2, \quad \frac{\partial \pi_{ORn}^L}{\partial z_{OR}^L \partial q_{ORn}^L} = \frac{1}{4}(-4+k)\delta \\ \frac{\partial \pi_{ORn}^L}{\partial q_{ORn}^L \partial z_{OR}^L} &= \frac{1}{4}(-4+k)\delta, \quad \frac{\partial^2 \pi_{ORn}^L}{\partial (z_{OR}^L)^2} = 1 - \frac{k}{4} \end{aligned}$$

The Hessian matrices of Eq. (A.2) with respect to z_{OR}^L and q_{ORn}^L are:

$$\begin{aligned} H &= \begin{pmatrix} -2 - \frac{1}{4}(-4+k)\delta^2 & \frac{1}{4}(-4+k)\delta \\ \frac{1}{4}(-4+k)\delta & 1 - \frac{k}{4} \end{pmatrix} \\ |H| &= \frac{1}{2}(-4+k) < 0 \end{aligned}$$

The main diagonal elements are all less than 0, so equation (1) is a concave function with respect to z_{OR}^L and q_{ORn}^L .

Similarly we can prove **Lemma (ii)** by reverse induction.

Proof of conclusion 1

Due to $\frac{\partial \pi_{ORn}^L}{\partial z_{OR}^L} = \frac{-c_r(-2+k) + (-2+k+(-4+k)-q_{ORn}^L)\delta}{-4+k}$
and $\frac{\partial \pi_{ORn}^L}{\partial q_{ORn}^L} = \frac{4-4c_n-4e_n p_e + \delta(c_r(-2+k) + (-4+k)z_{OR}^L - (-2+k)\delta)}{8+(-4+k)\delta^2}$
so, $z_{OR}^{L*} = \frac{-c_r(-2+k) + (-2+k + \frac{1}{2}(-4+k)(1-c_n-e_n p_e))\delta}{-4+k}$, $q_{ORn}^{L*} = \frac{1-c_n-e_n p_e}{2}$
Substituting this into the expression $\tau_{OR}^L = \frac{c_r + z_{OR}^L + \delta(-1 + q_{ORn}^L)}{2q_{ORn}^L}$ gives:

$$\tau_{OR}^{L*} = \frac{-2c_r + (-2 - c_n(-4 + k) + k - e_n(-4 + k)p_e)\delta}{(-4 + k)(-1 + c_n + e_np_e)\delta}$$

Solving in this loop we can get q_{ORn}^{L*} , q_{ORr}^{L*} , p_{ORn}^{L*} , p_{ORr}^{L*} , and substituting them into Eq. (1) and Eq. (2) we can get the optimal profit values of π_{ORn}^{L*} and π_{ORr}^{L*} for the original manufacturer and the remanufacturer. The above is the proof process of **Conclusion 1**. The rest of the model proof process is similar and will not be repeated.

Proof of Conclusion 2

$$(1) z_{OR}^{L*} = \frac{-c_r(-2+k) + (-2+k+\frac{1}{2}(-4+k)(1-c_n-e_np_e))\delta}{-4+k}$$

So, one gets: $z_{OR}^{L*} - z_{RR}^{L*} = 0$, $z_i^{H*} = z_i^{L*}$

The proof process for **Conclusions 3 to 8** is like that of **Conclusion 1** and will not be repeated in detail.