

A Statistical Approach to Estimating Water Quality Parameter: A Case Study on Turkey's Rivers

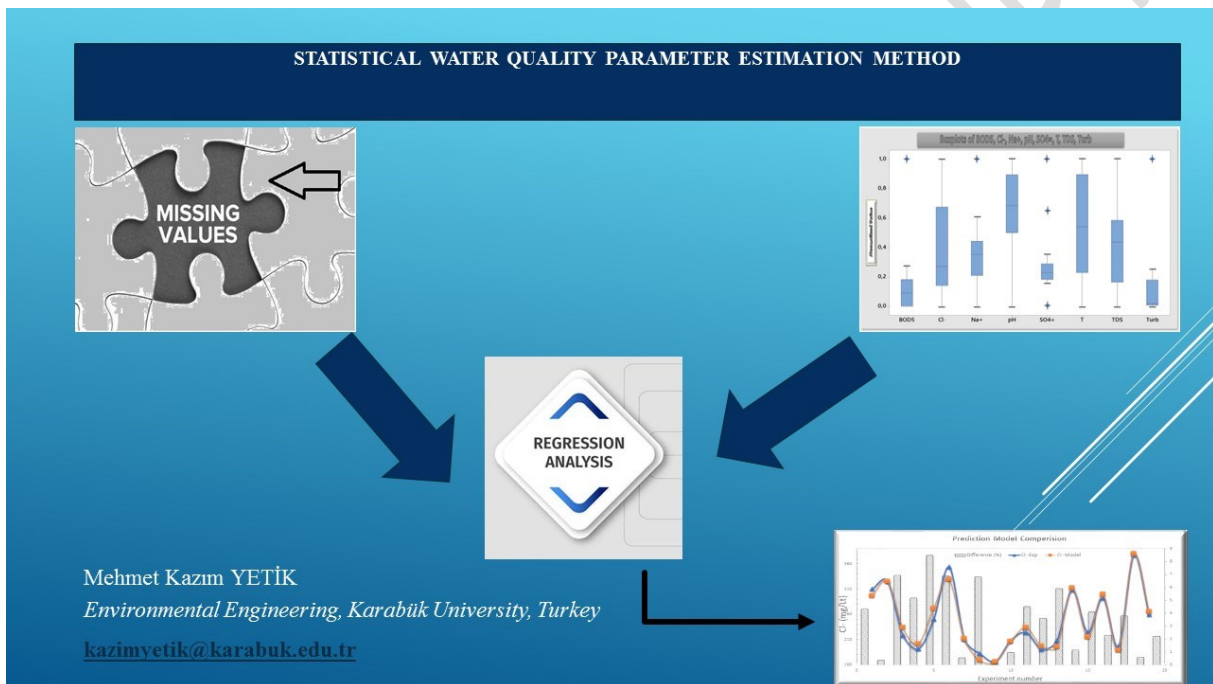
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Graphical Abstract



Abstract

Monitoring water quality parameters in rivers is of critical importance for decision makers and researchers. However, difficulties such as missing data, test values exceeding certain limits and parameters that are not measured but need to be monitored are among the main problems in monitoring water quality. In this study, these three main problems in water quality monitoring processes were addressed and solution-oriented approaches were developed. Solutions were applied for missing and dirty data problems, and multivariate regression and prediction models were proposed for unmeasured parameters. A prediction model was developed using parameters such as BOD₅, Cl⁻, Na⁺, pH, SO₄, temperature, TDS and turbidity, and the performance of the model was analyzed in detail for SO₄, Cl⁻, Na⁺ and BOD₅ parameters. The accuracy of the model was evaluated with statistical indicators such as MSE, MAPE and correlation coefficient (r). The model showed high accuracy with MAPE values below 10% for most parameters. For example, for the Cl⁻ parameter, MSE was calculated as 118, MAPE as 3.6 and r value as 0.984. In addition, a user-friendly graphical user interface (GUI) has been developed and used to create an automatic regression model for the Cl⁻ parameter. This system, integrated with VBScripts, has been tested on the Kızılırmak River to prove its applicability within a single program framework for all rivers. The results obtained show the effectiveness and wide-ranging applicability of the proposed method.

Key Words: Water Quality Parameters, Missing data, Boxplot, Multivariate Analysis, user friendly GUI, Outlier Detection.

28 1.Introduction

29 Water is one of the most significant elements on our planet. No living species on earth can survive without it. It is
30 a substance that is used by all living organisms. Industrialization and urbanization are rapidly developing near
31 water resources, causing numerous contaminants from industry to impact water resources. These waste products
32 from industrialization and urbanization change the natural concentration and characteristics of the water,
33 increasing the level of water pollution in the region. Furthermore, river water affects every point of its route (Isaac
34 & Siddiqui, 2022). Managing water resources is critical to basin management. In recent years, there has been an
35 increasing interest in monitoring water quality indicators. In certain nations, collecting water samples manually
36 and then analyzing them in a laboratory is mandatory (Islam Khan et al., 2022). The water quality index (WOI) is
37 widely used by policymakers, decision-makers, and other stakeholders to obtain a clear and comprehensive picture
38 of a water body's pollution status. It is one of the most commonly used concepts to express water quality in this
39 area (Tripathi & Singal, 2019; Sadiq et al., 2022).

40 Monitoring water quality parameters in streams is very important to have information about the river, researchers
41 and decision makers organize measures in the riverbed according to these parameters on the river. The most
42 important problem that researchers and decision makers encounter at this stage is that incorrect data from analyses
43 or online sensors cannot be determined immediately, or some information is missing due to sensor and analysis
44 deficiencies, or a parameter that will be needed is not available in the system. In this study, solutions were applied
45 based on a data set with these two problems and presented to researchers. In the third problem, a multiple regression
46 model was created for some parameters selected from the data set to show that an existing parameter can be
47 estimated correctly. In this stage, an interface was created with (Visual Basic Script) VBScript to make the
48 processes fast and error-free, allowing researchers and decision makers to perform easy operations.

49

50 This article explores how dirty data can be removed from the dataset and how missing data can be retroactively
51 added, as well as how a complete dataset can be created without outliers by applying relevant operations.
52 Additionally, the effects of water quality parameters on each other were analyzed, and a model for estimating
53 water quality parameters was presented. For this purpose, the water quality parameters of the data set of the
54 Kızılırmak River for 5 years were used.

55

56 The literature review revealed that data sets were used in all analyses. However, measurement errors and data
57 deficiencies are common in water quality test data due to seasonal and regional conditions. These shortcomings
58 can directly influence the research results. In this study, methods to address these shortcomings were discussed
59 and the proposed approach was applied to a data set. In addition, the process of estimating some parameters that
60 are difficult to determine using the modelling method was explained in detail. The developed model was supported
61 by statistical analyses and its accuracy and effectiveness were demonstrated. It is assessed that the methods
62 presented in the study can provide important guide in the field of river research. In addition to proving the accuracy
63 of the hypothesis supported by statistical analyses, the methods used contribute to the evaluation of the data
64 obtained and to the planning of research processes to be carried out in different rivers. In this respect, the study
65 has a quality that can serve as a guide for scientists and practitioners in the field of river research. The Kızılırmak
66 river, which is particularly significant for Turkey and the countries bordering the Black Sea, has always been a
67 focus of researchers, and scores of studies on its water have been undertaken. Because estimating or directly
68 monitoring the water characteristics of the Kızılırmak river is of critical importance for the region. In this study, 8
69 different water quality parameters taken from the station on the Kızılırmak River were used, and the created
70 prediction model allows the researcher to estimate a selected parameter. The model, which allows parameter
71 change, was tested one by one with statistical methods for four different parameters, and the results were
72 interpreted and made available to researchers. A modeling study was also carried out with normalized data, in
73 order to compare the factor values of the parameters with each other (Lumb et al., 2011; Zhou et al., 2021). These
74 effects of the parameters on each other will be especially useful for researchers doing Artificial Neural network
75 (ANN) and artificial intelligence (AI) studies (Wenyan et al., 2023). For this purpose a user-friendly Graphical
76 User Interface (GUI) was created by software coding in VBScripts, and this interface was used to create a model
77 for a parameter chlorine ion (Cl).

78 1.1 Literature

79 Water plays a significant role in our lives. Water quality change or degradation endangers the aquatic environment,
80 affects human health, and has an impact on the region's social and economic growth. It is necessary to gather data
81 on water quality in order to avoid water contamination, especially in developing nations (Sun et al., 2019). Aquatic
82 organisms, waterside soil erosion and seawater entering parameters are all monitored for water quality (Setshedi
83 et al., 2021; Ma et al., 2020).

84 Human activities (agriculture, industry, and urbanization) and natural elements (soil, geology, and precipitation)
85 in the basin have an impact on the quality of surface water in this region (Sundaray et al., 2006; Noori et al., 2009).
86 Precipitation, hydrological conditions, and seasonal fluctuations on the streamline all contribute significantly to
87 pollution (Z. M. Zhang et al., 2022). Assessing the quality of its water is therefore critical because it directly
88 impacts public health (via drinking water) and aquatic life (via raw water) (Pande G. et al., 2015) .

89 Monitoring is seen that water quality is decreasing in modern societies due to increasing water scarcity. It is not
90 enough for communities to access and receive the required amount of water. In addition, the quality of the water
91 reached must be appropriate (Horvat et al., 2021).

92 As a result of cultures' excessive usage of water, the problem of water body reduction and pollution has occurred.
93 For this reason, due to environmental factors, completing this follow-up is a very costly and time-consuming
94 operation in some circumstances, and it requires a large and expert team, and it is critical to have hardware that
95 can provide full and accurate data. As a result, it is critical for researchers to evaluate water quality parameters or
96 to improve the effectiveness of the current evaluation procedure. In order to develop a better management plan
97 (Abyaneh, 2014), researchers are continuing their research.

98 According to Saikat Islam Khan and colleagues (2022), assessing water quality is one of the biggest challenges
99 the world has faced in recent years, and their study aims to examine the research methods that researchers have
100 used in the last few years for water quality management systems. Multiple linear regression, least squares method,
101 decision tree, random forest method, wavelet neural network approach, and recursive wavelet network have been
102 examined. The climate has been significantly impacted by these recently developed methods for monitoring water.
103 Nevertheless, these models necessitate a considerable number of input parameters (Islam Khan et al., 2022;
104 Uncumusaoğlu A. A., 2018).

105 Monitoring of water quality is essential for anticipating future hazards to the aquatic environment and for managing
106 water resources. In the long-term research of accurate monitoring and evaluation of water quality, there are many
107 obstacles. To reduce these challenges, several researchers used Multivariate Statistical Techniques (MST) and the
108 Water Quality Identification Index (WQII) in their studies to examine the change in water quality in a river and
109 identify key sources of pollution (Ma et al., 2020; Li et al., 2018).

110 Researchers have developed prediction models by using different numbers of parameters and incorporating
111 different parameters into the model (Agegnehu et al., 2024; Li et al., 2018; Islam Khan et al., 2022; Ma et al., 2020).
112 Some scientists, on the other hand, investigated strategies for developing a multivariate statistical model prediction
113 model with fewer parameters for river estimate (Isaac & Siddiqui, 2022). In the index selection procedure, some
114 scholars investigated the scientific basis of the multivariate statistical analysis approach (Liu et al., 2021; Gurjar
115 & Tare, 2019; Anifowose & Odubela, 2018). Multivariate statistical methods have been used by many researchers
116 to monitor and predict water quality pollution in their research. (Z. M. Zhang et al., 2022; Yidana & Yidana, 2010;
117 Abyaneh, 2014; Noori et al., 2010; Kazi et al., 2009; Azhar et al., 2015; Fathi, Zamani-Ahmadm Mahmoodi, and
118 Zare-Bidaki 2018; Sakizadeh, 2016).

119 On-site study of water quality parameters can be challenging due to geographical restrictions; also, inaccuracies
120 in data may arise during on-site measurement due to meteorological factors such as air temperature, rain, etc.
121 Because various factors might influence measurement values, different approaches are employed to discover and
122 delete incorrect data from the data set. In outlier investigations, Tukey's (1977) boxplot method, which is described
123 in detail in the book, is employed. The boxplot also produces excellent results in data extraction studies in many
124 different fields. For example, the boxplot analysis method was used to evaluate data from surface water samples
125 and discover outliers in water quality investigations (Ahmad et al., 2001).

126 Missing data causes issues in the statistical analysis of water quality data obtained through machine learning. Some
127 have investigated the success of various methods for dealing with defects in databases (Betrie et al., 2016; .Y.
128 Zhang & Thorburn, 2022). It is commonly used for the elimination of missing data in the creation of data sets,

129 particularly in machine learning studies(Yang, 2022). Using an existing data set, researchers created estimation
 130 models using multivariate statistical approaches (Wang et al., 2012).

131 2. Material and procedure

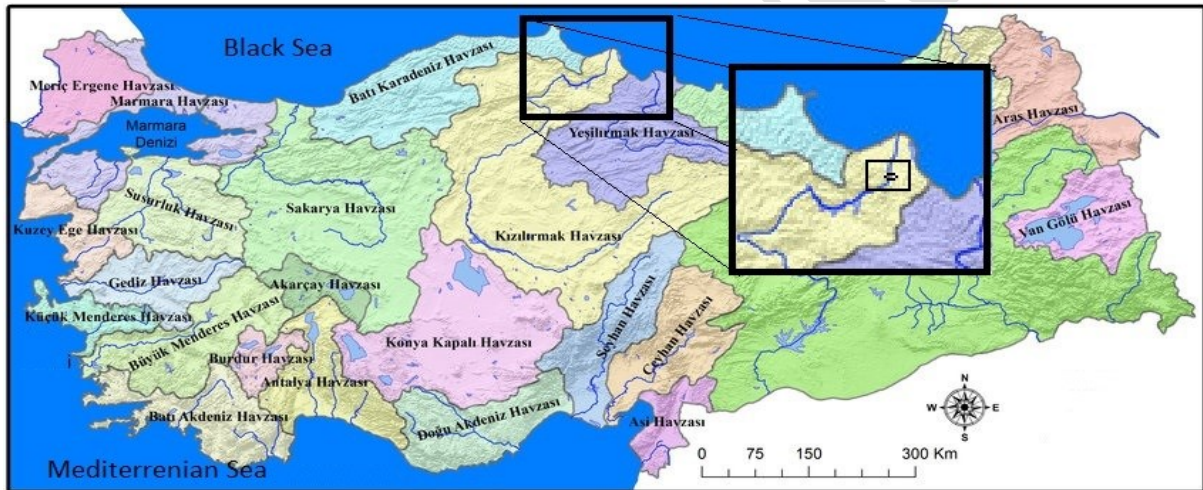
132 2.1 Study area (case study)

133 This research was carried out with the data set of water quality parameters obtained from samples taken from the
 134 observation station on the Kızılırmak River.

135 The coordinates of the Station point, which is located on the (nearest point of the) coast in the Black Sea region
 136 and on the Kızılırmak, are 41°35'02.84'' North 35°53'30.16'' East, as seen in Figure 1. This station is one of the
 137 last stations on Kızılırmak due to its location. The location of the river and the station is important in revealing the
 138 parameters of pollutants discharged into the sea.

139 The longest river that starts in Turkey and discharges into the sea in Turkey is the Kızılırmak, which is 1151
 140 kilometers long. Its basin, including its tributaries, covers an area of approximately 82 thousand square kilometers.
 141 The river runs through 45 different districts in 11 different provinces, with a total population of more than 11
 142 million people living in the provinces it flows through. In addition to being a significant river for Turkey, it is also
 143 an important river for countries along the Black Sea coast due to its flow.

144



145
 146 **Fig. 1.** The station point's location (position within the basin) where the samples were taken to compile the data
 147 on the map of Turkey.

148 2.2 Data collection

149 Some water quality-determining parameters are analyzed on-site by experts from the General Directorate of State
 150 Hydraulic Works (is called as DSI in Turkey) using river samples, while others are measured in authorized
 151 laboratories. Analyzes of more than 50 parameters are conducted four times a year. This study was carried out
 152 using the findings of an analysis of data collected for 5 years. Biological oxygen demand (BOD5), chlorine ion
 153 (Cl), sodium ion (Na), pH, sulfate ion (SO4), Temperature (T), Total Dissolved Solids (TDS), and Turbidity (Turb)
 154 are the parameters employed in this research. The parameters, unit, Mean, Max, Min, Variance, and Coefficient of
 155 Variance (CV) are displayed in Table 1. The value of turbidity has the largest variance and CV in this table. The
 156 value variance and CV of pH are the lowest.

157 **Table 1** Table showing the statistical analysis values for the raw data set on which the study will be conducted.
 158

Parameter	Unit	Mean	Max	Min	Variance	CV
BOD5	mg/L	2.928571	12	1	7.066327	90.76973
Cl	mg/L	247.5316	377.52	166.76	3711.257	24.61104
Na	mg/L	185.0211	307.64	117.82	1697.83	22.27029

pH	-	7.841176	8.5	6.6	0.298893	6.972306
SO4	mg/L	360.8211	1239	16.2	63964.29	70.09337
T	°C	15.625	21	9	16.73438	26.18091
TDS	mg/L	1141.533	1524	875	26937.58	14.37774
Turb	NTU	50.60667	418	0.4	10695.18	204.3555

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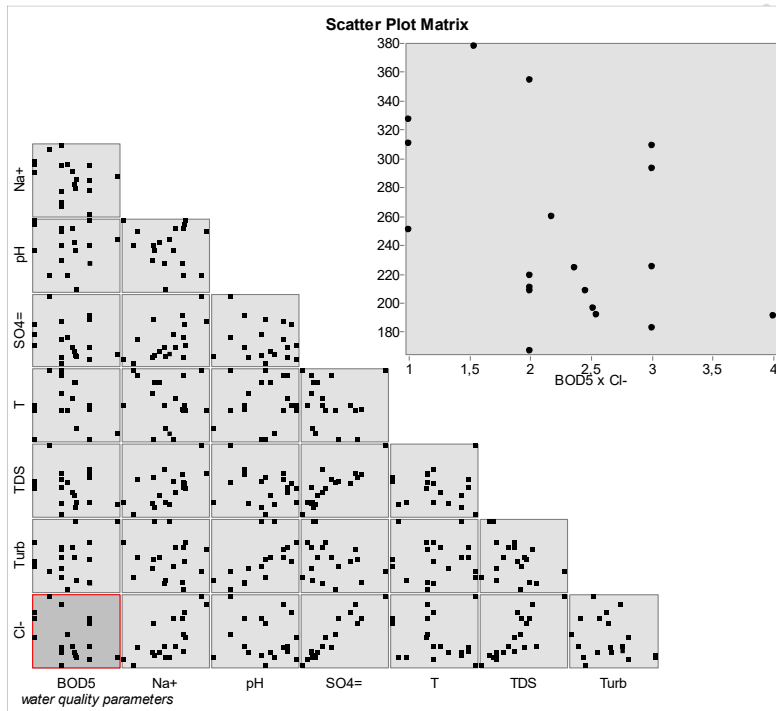
160 2.3 Method methodology

161 To develop a multivariate regression model based on the selected water quality parameters, the interactions and
 162 mutual influences among these parameters were analyzed. This preliminary analysis is critical for understanding
 163 the relationships between variables and identifying significant predictors. The observed effects of these
 164 interactions are presented in Figure AAB, which provides a detailed visual representation of the correlations and
 165 dependencies within the dataset.

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170 Fig. 2: Scatter plot Matrix of selected water quality parameters

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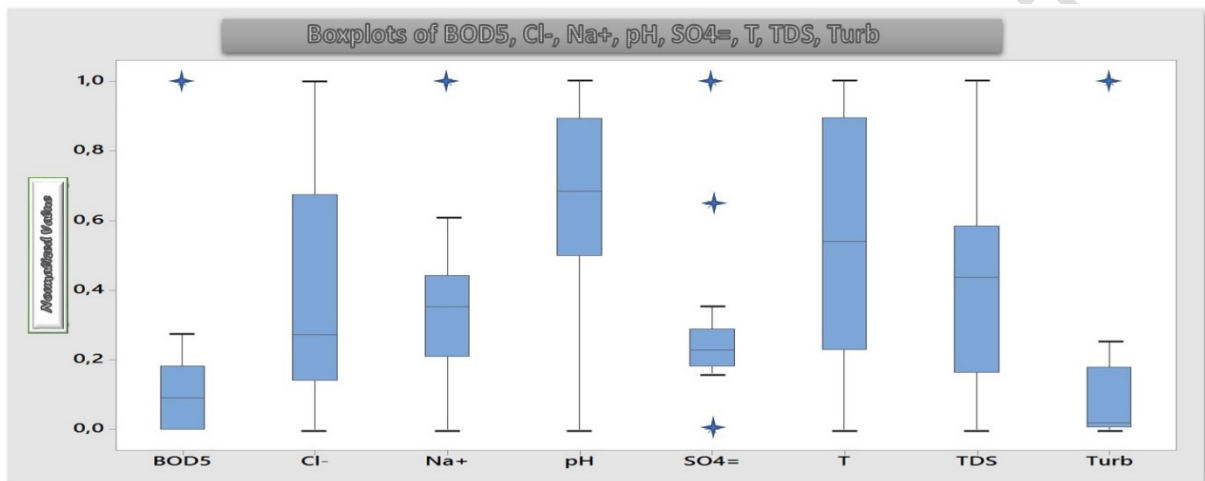
172 Some Researchers used variance and CV values while examining water quality parameters in their studies (Azhar
 173 et al., 2015; Abyaneh, 2014). As shown in Table 1, several maximum and minimum values are quite far from the
 174 mean (i.e. BOD5 and Turb values), and the variance value for this parameter is also very high. In such cases,
 175 Tukey (1977) introduced outlier detection methods with boxplot graphics in his study. Similarly, other researchers
 176 employed boxplot visuals to eliminate data noise (Islam Khan et al., 2022; Dawson, 2011). The boxplot approach
 177 was employed in several of these investigations to determine the extreme values of water quality parameters. The
 178 correction was accomplished by determining the extreme values (Tripathi & Singal, 2019; Horvat et al., 2021).
 179 The methodologies used are examined one by one below.

180

181 **2.3.1 Boxplots**

182 In the boxplot, a box shape is formed by drawing lines from the first quartile (Q1) to the third quartile (Q3); in this
 183 box shape, where the median of the data set is also marked, whiskers extending from the first quarter to the
 184 minimum and from the third quarter to the maximum are drawn, and a boxplot is formed. Outlier detection analysis
 185 was done on the data set in this study, and boxplots were utilized to extract data noise. Fig. 2. shows the creation
 186 of boxplots and the determination of outliers. Whiskers are typically much longer than the box; small whiskers
 187 may have a uniform distribution with sharp cuts (Dawson, 2011). Outliers are described as being far from whiskers.

188 Outlier detection analysis were done on the data set in this study, and boxplots were utilized to extract data noise.
 189 Figure 2 shows the creation of boxplots and identification of outliers (with normalized values). This figure has
 190 been normalized so that the data can be aggregated.



191
 192 **Fig. 2.** For outlier detection , BOD5, Cl⁻, Na⁺, pH, Turb, SO₄, T, TDS, Turb parameters' boxplots graphics (with
 193 normalized value).

194 As seen in boxplot graphs, some graphs are also seen with '*' except for whiskers extending from the outside of
 195 the box to the minimum the first quarter (Q1) and from the third quarter (Q3)to the maximum (whiskers). As
 196 shown in the figure, the '*' value is far from the data values where the box is produced. BOD5, Na, SO₄, and Turb
 197 values, in particular, appear to have contradictory values when compared to the data set structure. Table 2 shows
 198 the boxplot values for these (selected) parameters.

199 **Table 2** Outlier values and boxplot analysis values obtained as a result of Boxplot analysis for outlier value
 200 detection.

Parameter	Q1	Q3	Median	Bottom	Up
BOD5	1.75	3	2	1	4
Na	157.8	201.8	184.6	117.8	233.5
SO ₄	239.4	368.5	295.7	215.7	446.1
Turb	3.2	75.5	8.4	0.4	106

201

202 **2.3.2 Missing Value**

203 After outliers are detected by boxplot analysis, these parameters were examined by comparing them with other
 204 station data on the same river. It was observed that these extreme values were incompatible even with the seasonal
 205 changes of the river, and therefore these extreme values were removed from the data set. Missing value studies
 206 were carried out to replace the deleted values in the data set. However, since all data for a particular month was

207 missing in the data set, no work was done to find a value to replace the data for that month, and the data for that
 208 month was completely removed from the analysis."

209 The data set was checked for missing values after it had been cleansed of extreme values by using outlier detection.
 210 The measurements were conducted with samples obtained from the same point of the river. The missing value is
 211 obtained sometimes owing to meteorological causes and sometimes from the sample (storage, transportation, etc.).
 212 Due to the issues that have arisen, it is not possible to examine and assemble data. However, the data in the data
 213 set must be complete in order to analyze and construct a new model. Researchers have developed new ways to
 214 achieve this goal by examining different methodologies for various data sets and methods for eradicating missing
 215 data in data sets (Betrie et al., 2016; Y. Zhang & Thorburn, 2022).

216 As a method of replacing missing data in the data set, several studies calculate the median or mean values of the
 217 relevant data set. In reality, some researchers claim that it is acceptable to use arbitrary values in some data sets
 218 (Yang, 2022). Among these studies, the linear regression method, which is developed by the least squares method,
 219 produces very effective results for missing data elimination (Wang et al., 2012). The correlation between
 220 parameters is examined by this method, and a linear estimating model is formed by choosing the parameter with
 221 the highest correlation for missing data. Table 3 displays the correlation values of the parameters in the data set.
 222 The estimated value is calculated using the values in the same order as the missing data.

223 **Table 3** Correlation values between parameters in the raw data set.
 224

<i>Parameters</i>	BOD5	Cl	Na	pH	SO4	T	TDS	Turb
BOD5	1	-0.359	-0.286	-0.109	-0.118	-0.265	0.021	0.333
Cl	-0.359	1	0.669	-0.070	0.943	-0.173	0.813	-0.288
Na	-0.286	0.669	1	0.031	0.529	-0.274	0.450	-0.084
pH	-0.109	-0.070	0.031	1	-0.153	0.119	-0.026	0.509
SO4	-0.118	0.943	0.529	-0.153	1	-0.048	0.842	-0.141
T	-0.265	-0.173	-0.274	0.119	-0.048	1	0.107	-0.049
TDS	0.021	0.813	0.450	-0.026	0.842	0.107	1	-0.409
Turb	0.333	-0.288	-0.084	0.509	-0.141	-0.049	-0.409	1

225
 226 For the purpose of imputation, the missing parameter estimation was performed using linear regression between
 227 the two parameters with the highest correlations in this table (Chen et al., 2022). The data set deficiencies were
 228 removed by using this method. (Burchard-Levine et al., 2014). For example, for SO4 imputation, the Cl data with
 229 the highest correlation is chosen. The table shows that the correlation between SO4 and Cl is 0.94307. Similarly,
 230 for lack of TSD values, the SO4 data with the highest correlation was chosen (0.842242). The estimation model is
 231 built using the linear regression equations listed below (1-3) (Ortas et al., 2019). Fig. 3. displays the residual graph
 232 and linear regression graph for SO4 vs. Cl. Also, correlation is very high between these parameters.

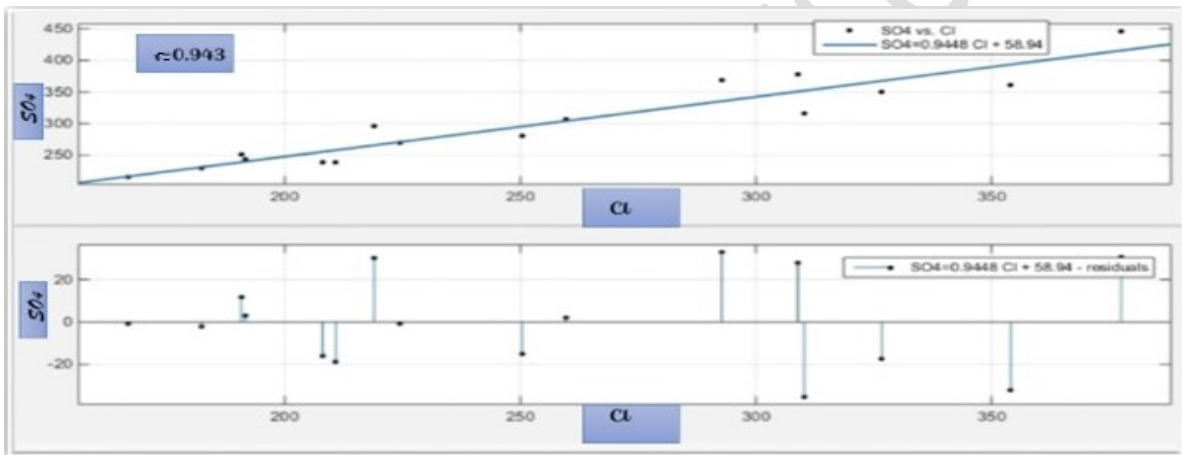
233
$$\alpha = \frac{\sum((x_i - \bar{x})(y_i - \bar{y}))}{\sum(x_i - \bar{x})^2} \quad (1)$$

234
$$\beta = \bar{y} - \alpha \bar{x} \quad (2)$$

235
 236
$$\hat{y}_i = \alpha x_i + \beta \quad (3)$$

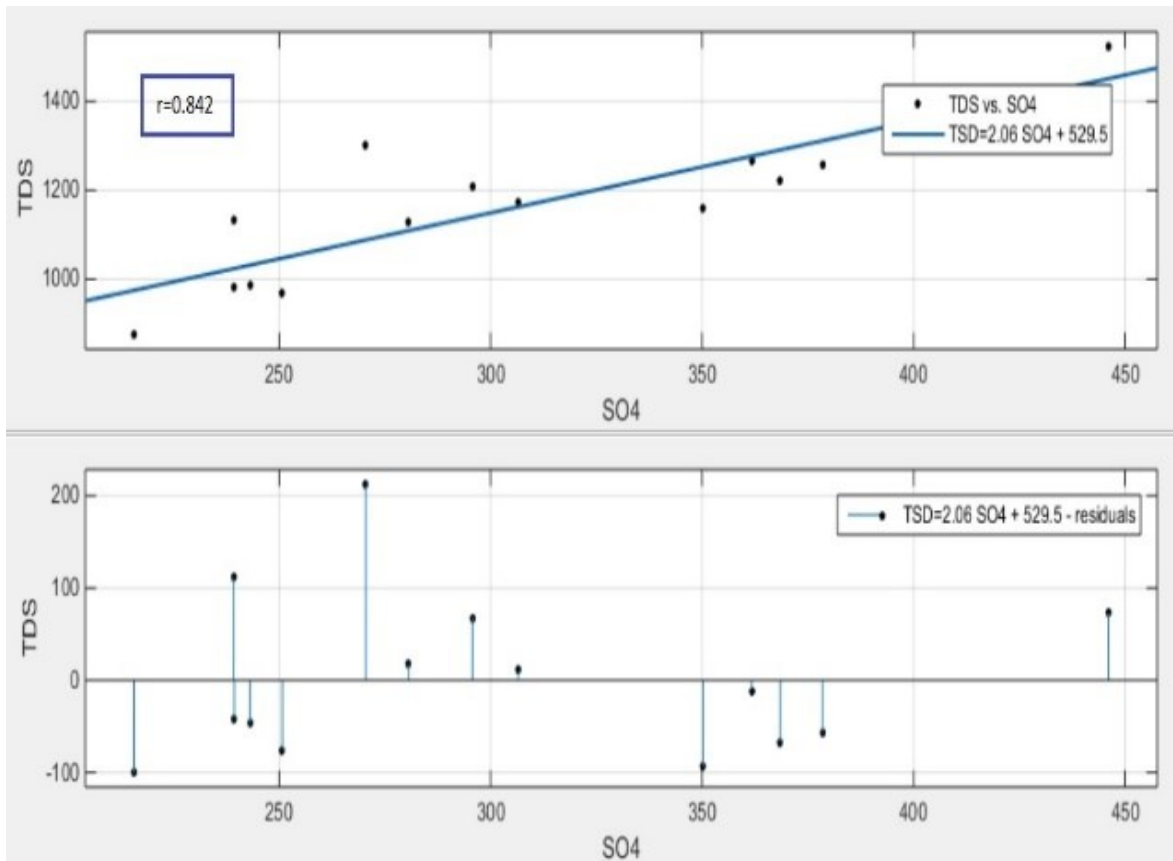
237
 238
$$\alpha = \text{slope}$$

239 $\beta = \text{intercept}$
 240 $x_i = \text{value of parameter}$
 241 $\bar{x} = \text{mean of parameter}$
 242 $y_i = \text{value of parameter}$
 243 $\bar{y} = \text{mean of parameter}$
 244 $\hat{y}_i = \text{predicted value of parameter}$
 245
 246
 247
 248
 249



250
 251
 252 **Fig. 3.** Linear regression and residual value plot between SO4 and Cl parameters.

253 Likewise, a prediction model was developed with SO4 data within the TDS value. The graph prepared for the
 254 developed model is given below. Fig. 4 shows the residual plot and linear regression plot for TDS and SO4. In
 255 residual graph, only one value appears to be too far out.



256

257 **Fig. 4.** Linear regression and residual value plot between TDS and SO4 parameters.

258

259 Outliers and missing values are therefore deleted and rearranged in the data set. External values and defects in the
 260 entire data set are removed using this procedure. Table 4 shows the statistical distribution of the arranged data set.

261

262 **Table 4** The statistical table of the final version of the data set, purified from outliers and imputed values for
 263 missing parameters.

264

Parameters	Unit	Mean	Max	Min	Variance	CV
BOD5	mg/L	2.242	4	1	0.581	33.988
Cl	mg/L	247.2532	377.52	166.76	3711.26	24.611
Na	mg/L	179.478	233.54	117.82	905.716	16.768
pH	-	7.786	8.5	6.6	0.293	6.952
SO4	mg/L	292.819	446.1	215.7	3693.55	20.755
T	°C	15.42	21	9	14.352	24.568
TDS	mg/L	1127.36	1524	875	23007.6	13.455
Turb	NTU	8.906	19.6	0.4	28.427	59.868

265

266 The variance of the TDS value is 23007.6, as shown in the table, whereas the CV value is estimated as 13.455,
 267 which is rather high. This value shows that the TDS data is distributed around the mean. Likewise, the variance of

268 SO4 value is 3693.55, while the CV value is 20.755, indicating that the available data are distributed around the
 269 mean. Despite the fact that the variance of the turbidity value was not very high, the CV value was determined as
 270 the highest (59.868). Since a portion of the river basin where the study was done is in the Black Sea region, as is
 271 the station, the data is considered valid. There is abundant rainfall and dense forest cover in the Black Sea region.
 272 For this reason, many floods mix with the river along with rainfall. As a consequence, substantial CV in Turbidity
 273 values is expected. Furthermore, for compatibility, these data were compared to data from other stations on the
 274 river, and it was verified that the parameters were compatible with the data from other stations.

275 Many methods have been developed by researchers for water quality monitoring. Some of them are modeling
 276 systems, while others are various systems ranging from Artificial Neural Network (ANN) to Genetic Algorithm
 277 (GA). In others, methodologies are used to investigate the correlations between water quality measures. In other
 278 methods, relationships between parameters of water quality are examined. Prediction models have been developed
 279 that allow water quality monitoring of one or more parameters (Burchard-Levine et al., 2014; Mishra, S. et al.,
 280 2016..Sakizadeh, 2016; Barcellos & Souza, 2022, Yeon L. S. et al, 2008).

281 3. Results

282 3.1 Multivariate Statistics Results

283 The correlation values of these parameters selected for multivariate statistical analysis after outlier analysis and
 284 missing value adjustment are given in Table 5.

285 Fig. 5. (a) and (b) show the highly connected (Na and Cl) and (pH and Turb) plots. Despite the impressive
 286 correlation of this data, linear regression does not provide adequate efficiency in parameter estimation. Because
 287 the correlation coefficients for the Cl parameter are 0.947 for SO4 and 0.820 for TSD when checked in the
 288 correlation table. This demonstrates that the representation of some parameters with many parameters is high. Fig.
 289 5. (c) depicts this situation with a graph of Cl - SO4 - TDS.

290

291

292 **Table 5** Adjusted experimental data set correlation table.

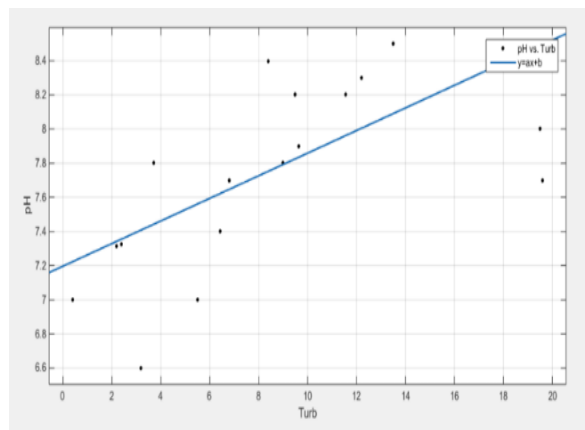
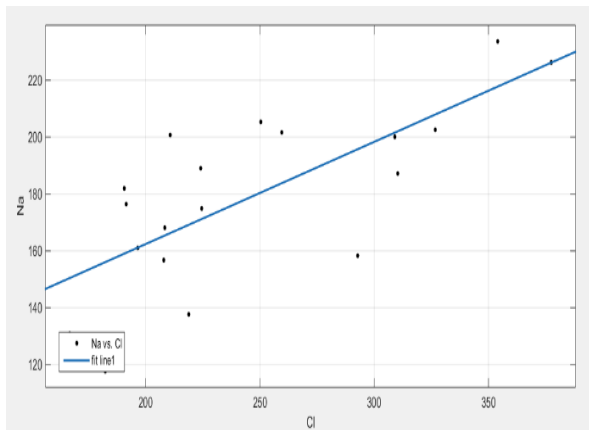
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<i>Parameters</i>	BOD5	Cl-	Na+	pH	SO4=	T	TDS	Turb
BOD5	1,0000	-0,4317	-0,3416	-0,1591	-0,2534	-0,2301	-0,2454	0,1840
Cl-	-0,4317	1,0000	0,7277	-0,0959	0,9471	-0,1852	0,8199	-0,2669
Na+	-0,3416	0,7277	1,0000	-0,1299	0,6166	-0,1432	0,6079	-0,1118
pH	-0,1591	-0,0959	-0,1299	1,0000	-0,1920	0,1022	-0,1965	0,6467
SO4=	-0,2534	0,9471	0,6166	-0,1920	1,0000	-0,1377	0,8613	-0,3077
T	-0,2301	-0,1852	-0,1432	0,1022	-0,1377	1,0000	0,0053	0,0126
TDS	-0,2454	0,8199	0,6079	-0,1965	0,8613	0,0053	1,0000	-0,3931
Turb	0,1840	-0,2669	-0,1118	0,6467	-0,3077	0,0126	-0,3931	1,0000

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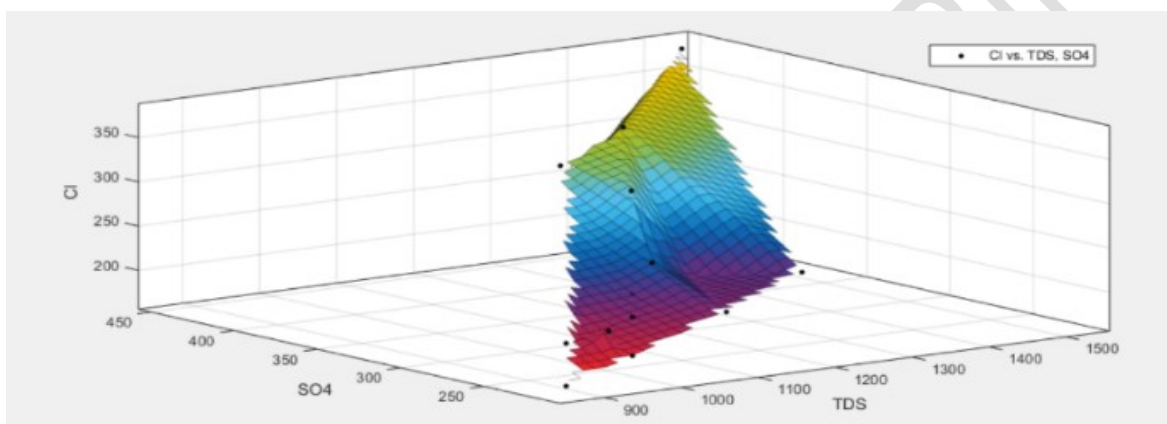


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298

a)

b)



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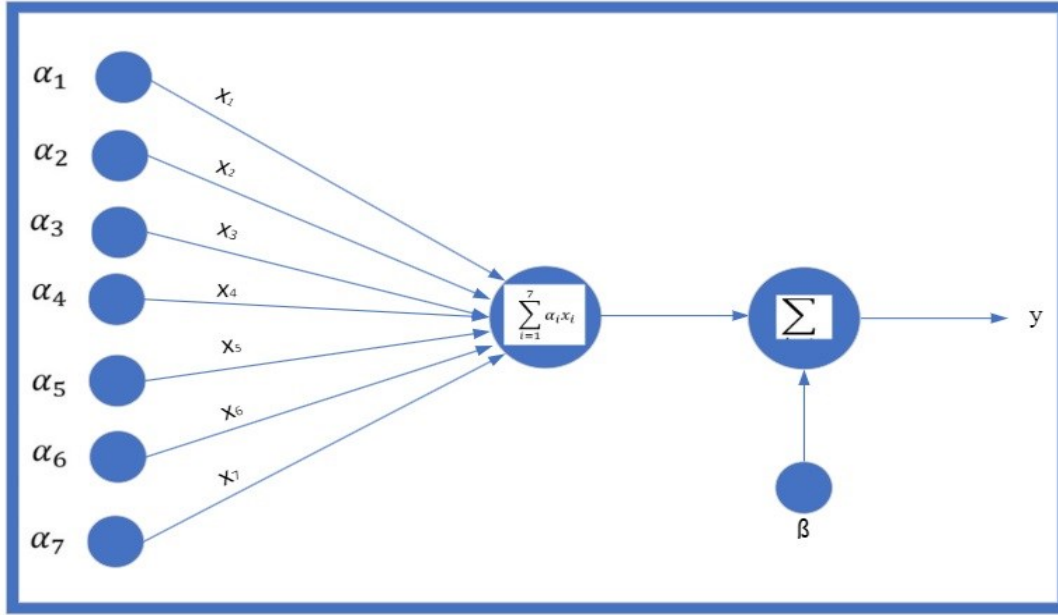
c)

301 **Fig. 5.** a) Na vs Cl linear regression graph b) pH vs Turb linear regression graph c) Cl vs SO₄, TDS linear
 302 regression graph.

303 As shown in the graphs and the correlation table, several parameters have more than one effective parameter. The
 304 correlation chart in Table 5 shows that the effect of T parameter (on other parameters) is not particularly strong.
 305 This parameter's maximum absolute correlation's value is about 0.23 (Table 4). Although the correlation value
 306 had a minor effect on the parameters, it was included in the model. The rationale for this is that it is the most easily
 307 ascertained parameter physically, and it has been chosen and included in the evaluation to help to the model's
 308 progress, albeit in a minor way.

309 Moreover, the coefficient ratios of all factors have different effects on the prediction models. A linear prediction
 310 model was created by analyzing the effect of other parameters on one parameter using multivariate statistical
 311 approaches (Liu et al., 2021; Maiolo & Pantusa, 2021; Betrie et al., 2016). In general, the linear model is given in
 312 Fig 6 and in equation 4.

313



314
315 Fig. 6. Linear prediction model general representation.

316 $\hat{y} = \alpha_1 x_1 + \alpha_2 x_2 + \alpha_3 x_3 + \alpha_4 x_4 + \alpha_5 x_5 + \alpha_6 x_6 + \alpha_7 x_7 + \beta$ (4)

317
318 $\alpha_i =$ each parameters coefficients

319 $x_i =$ each parameter

320 $\beta =$ intercepts of errors.

321
322 **3.2 Statistical Tests Results**

323 According to the selected parameter, the coefficient in front of the parameters was determined one by one
324 according to the least squares method. These are $\alpha_1 \dots \alpha_7$ coefficients and β value, and a prediction model has been
325 developed for 4 different parameters to examine the established modeling system. With the multi-statistical model
326 created (for the selected parameter), \hat{y} (estimate) values were derived, and correlation coefficient (r) with equation
327 5, Mean Squared Error (MSE) with Equation 6, and Mean Absolute Percentage Error (MAPE) with equation 7 on
328 the obtained values and existing (edited experimental) values were examined (Wang et al., 2012; Salman et al.,
329 2017; Nicolson & Paliwal, 2019; Bagla et al., 2021; Jiang et al., 2021; Longqin & Shuangyin Liu, 2013)

330
$$r = \frac{\sum x_i y_i - \frac{\sum x_i \sum y_i}{n}}{\sqrt{(\sum x_i^2 - \frac{(\sum x_i)^2}{n})(\sum y_i^2 - \frac{(\sum y_i)^2}{n})}}$$
 (5)

331
332
$$MSE = \frac{\sum (y_i - \hat{y}_i)^2}{n}$$
 (6)

333
334
$$MAPE = \frac{\sum (\frac{Abs(residual)}{real})}{n} * 100$$
 (7)

335 $residual = y_i - \hat{y}_i$

336 The statistical table for the r, MSE, and MAPE values derived for the SO4, Cl, Na, and BOD5 models is provided
 337 below.

338 **Table 6** Estimation model results for four selected parameters, as well as comparison statistics obtained from the
 339 data set.

Parameters	MSE	MAPE	r
SO4	151.061	3.731	0.979
Cl	118.716	3.627	0.984
Na	292.661	8.695	0.822
BOD5	0.224	20.737	0.784

341 As seen in Table 6, the MAPE values of the models were SO4, Cl, and for Na with MAPE <10% it produces value
 342 for the parameter predicted with very high accuracy (MAPE < 10% in scientific studies for model studies: It gives
 343 excellent prediction performance). The MAPE value for BOD5 is roughly 20%, which is within safe ranges.
 344 Correlation values in these parameters between the experimental data and the prediction model demonstrated that
 345 the models were compatible for SO4, Cl, and Na. Experimental data and prediction model' results are also within
 346 acceptable limits for BOD5. In addition, the fact that the MSE value for BOD5 is quite small shows that the
 347 experimental data and the prediction model produce results that are quite compatible.

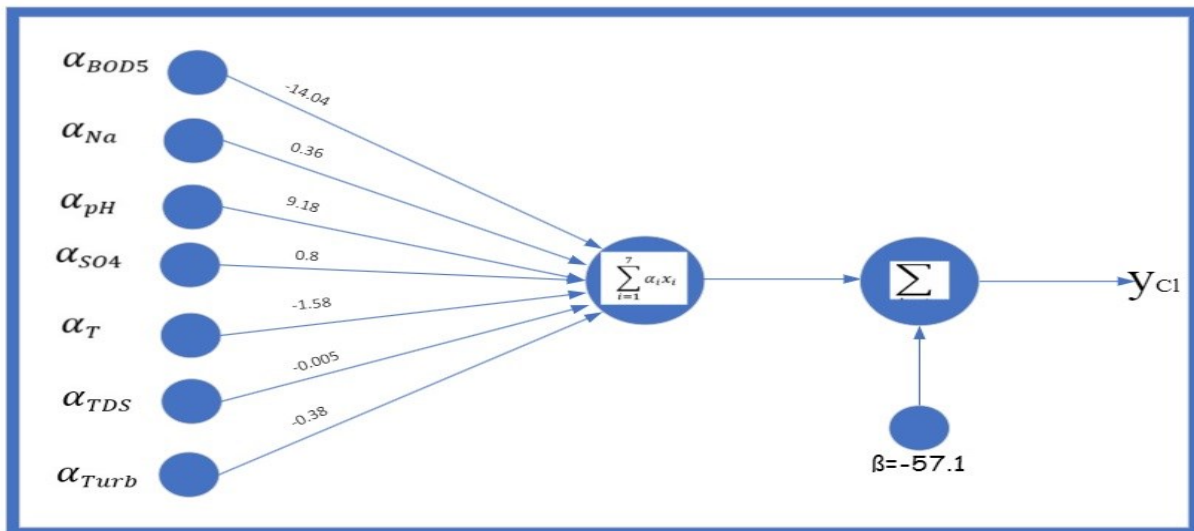
348 **4 Conclusion**

349 **4.1 Conclusion for prediction model**

350 Fig. 7 and equation 8 shows the generated Cl prediction model. The coefficients in the models built individually
 351 for the other parameters were derived separately based on the parameters.

352

353



354

355 **Fig. 7.** Cl prediction model with parameters and weight.

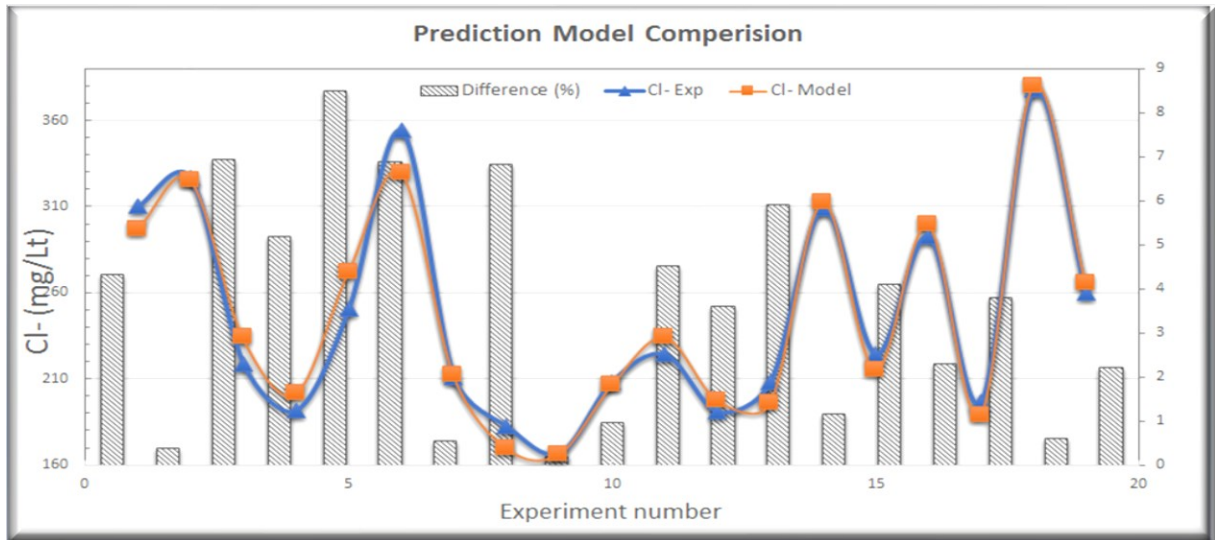
356

357 $\hat{y}_{Cl} = -14.04\alpha_{BOD5} + 0.36\alpha_{Na} + 9.18\alpha_{pH} + 0.8\alpha_{SO4} - 1.58\alpha_T - 0.005\alpha_{TDS} - 0.38\alpha_{Turb} - 57.1$ (8)

358

359 The agreement between the experimental data and the estimating moles created by the multivariate statistical
360 analysis approach and the data acquired was shown using comparison charts. The Cl comparison graph is shown
361 in Fig. 8. When the graph is examined, the data are found to be quite compatible. Additionally, the percentage
362 difference between the values can be seen in the graph.

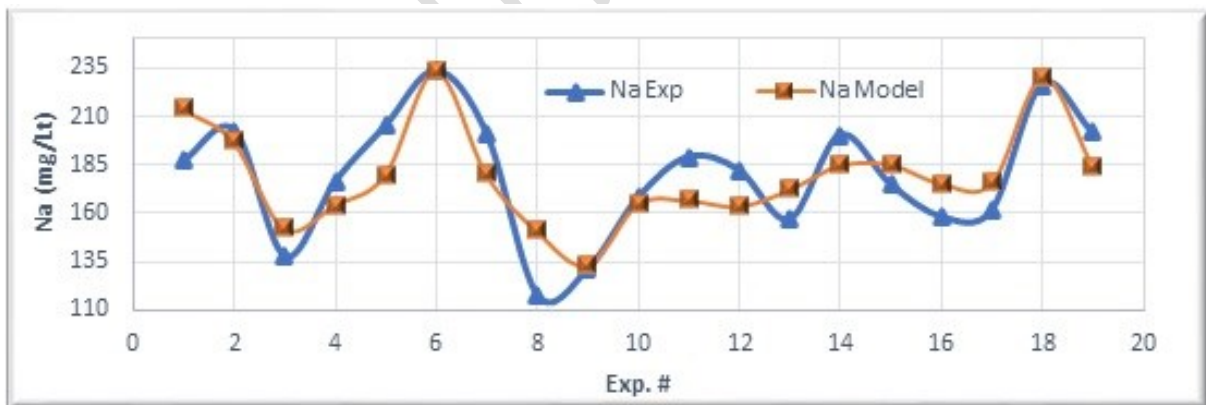
363



364

365 **Fig. 8.** Experimental (Cl-Exp) and prediction model (Cl-Model) comparison plot for Cl with difference percentage.

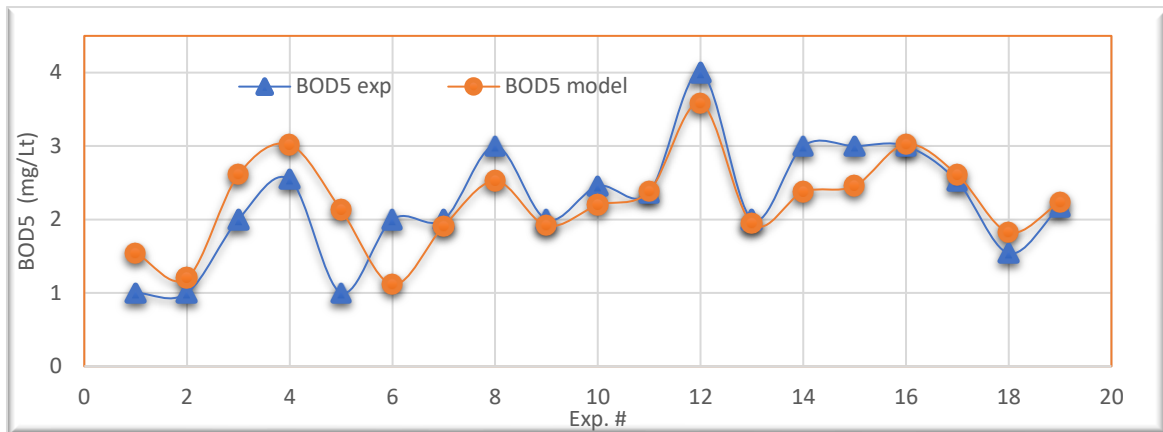
366 Fig. 9. shows the graph generated using the simulation model for Na in multivariate statistical modeling done using
367 the least squares method. Although the MSE value on the tested data has the greatest value, the MAPE and r values
368 demonstrate that the prediction model yields findings that are consistent.



369

370 **Fig. 9.** Experimental (Na Exp) and model (Na model) comparison plot for Na.

371 Fig. 10. shows the graph obtained using the BOD5 model defined for multivariate statistical modeling using the
372 least squares method. It is the prediction model with the smallest MSE value and generates an increase and decrease
373 trend prediction value that is generally accurate.

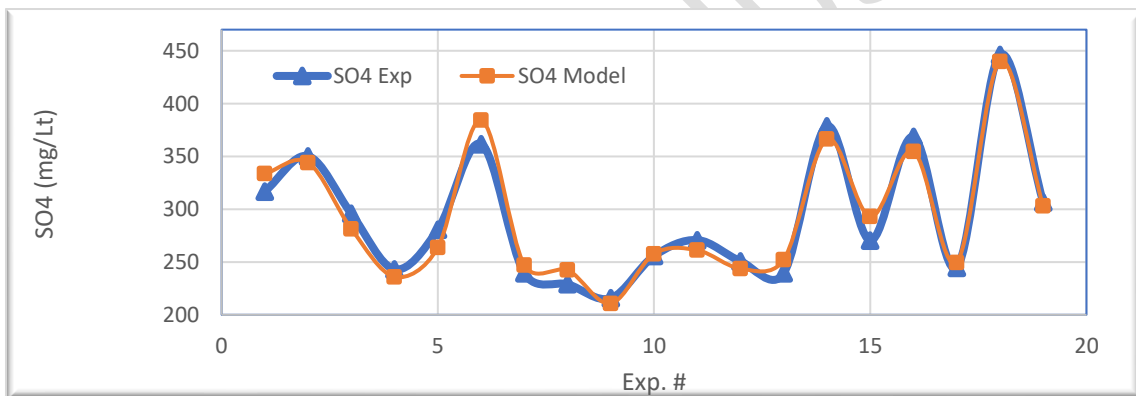


374

375 **Fig. 10.** Experimental (BOD5 exp) and model (BOD5 model) comparison plot for BOD5.

376 The graphic generated by using model developed for SO4 is shown in Fig. 11. in the multivariate statistical
 377 modeling carried out using the least squares method. The graph shows that there is a clear agreement between the
 378 forecast model findings and the actual data. Additionally, Table 6's correlation value for the data sets is very near
 379 to 1.

380



381

382 **Fig. 11.** Experimental (SO4 Exp) and model (SO4 Model) comparison plot for SO4.

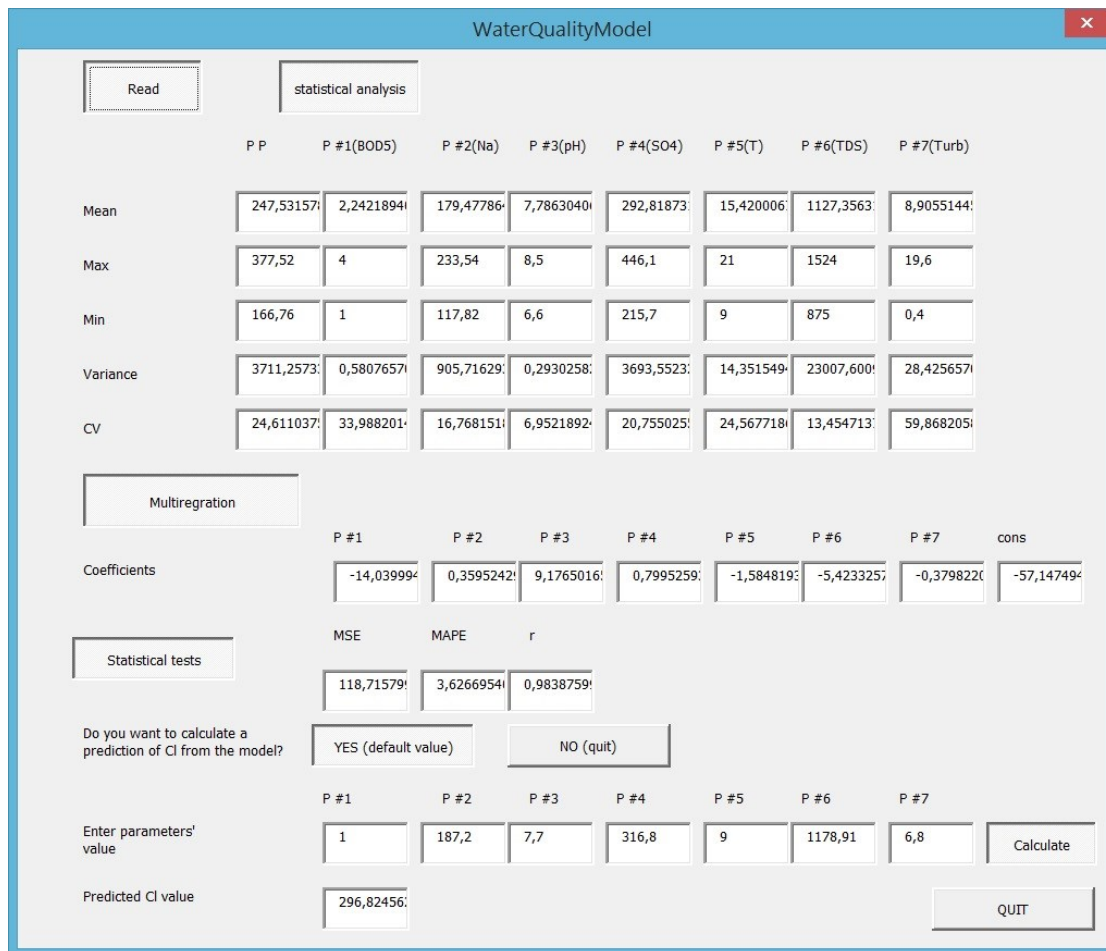
383

384 **4.2 Graphical User Interface for prediction model**

385 As stated above, the data set was edited and finalized after missing data and outlier analysis. After data editing
 386 studies, a water quality parameter estimation model was developed. The data obtained was tested statistically
 387 with real river data and the model studies carried out for four different parameters were found to be successful.
 388 However, the fact that the study has more than one phase makes it difficult for researchers to follow the process
 389 steps. For this reason, the process steps detailed above were combined in a single program and a user-friendly
 390 GUI was created using VBScripts to allow researchers to use the model in different data sets. Additionally, in
 391 order to simplify the GUI for researchers to understand more easily, a program that includes the working steps
 392 for only one water quality parameter (CI) has been created in this article. The created model interface is seen in
 393 Figure 12. The process steps for the interface are as follows:

- 394 1. Reading the edited data set
- 395 2. Statistical analysis
 - 396 a. Average
 - 397 b. Maximum
 - 398 c. Minimum
 - 399 d. Variance

- 400 e.CV (Coefficient of Variation)
- 401 3. Multiple regression (coefficients)
- 402 4. Statistical tests (with actual values)
- 403 5. Water quality parameter estimation (CI) with the model
- 404 (default value) enter any value
- 405 6. Predicted CI value
- 406



407
408
409 **Fig. 12.** Graphical User Interface for water quality parameter prediction model (for CI).

410
411 **4.3 Conclusion for normalized prediction model**

412 The estimates for SO4, Cl, Na, and BOD5 that were generated using the multi-statistical model are thought to be
 413 quite compatible with the actual MSE, and MAPE, and correlation values. However, it is difficult for researchers
 414 to determine which parameter has the most impact on the chosen parameter because of the variations in the units
 415 and data ranges of the parameters. Additionally, the agreement appears to be low in the charts for the parameters
 416 with high agreement in the charts discussed earlier. This is because the ranges in the relevant parameters are
 417 different, for example, the parameter range values used for BOD5 are between 0 and 4, while the parameter ranges
 418 used for SO4 are between 210 and 410. This makes it difficult to interpret graphs and statistical analyzes together.
 419 In order for the researchers to make this interpretation more easily and to understand the effects of the parameters
 420 on each other much more clearly, the existing data were normalized (equation 9) and all the parameters were taken
 421 to the range of 0-1 (Lumb et al., 2011; Simões et al., 2008; Ni & Chen, 2013; Y. Zhang et al., 2022). For this;

422

423
$$X_{Ni} = \frac{(x_i - x_{min})}{(x_{max} - x_{min})} \quad (9)$$

424

425 all experimental data were normalized using the above formula, and the previous procedures were carried out again
 426 for the four parameters that were chosen. The data set's parameters were first correlated. Table 7 lists the correlation
 427 coefficients for normalized data. The estimation model's equation 10, which is reorganized using normalized
 428 values, is provided. Equation 11 derived for the Cl parameter is provided as an example for the coefficient
 429 evaluation.

430

431 **Table 7** Correlations of parameters on normalized data.

432

Parameters	BOD5	Cl	Na	pH	SO4	T	TDS	Turb
BOD5	1	-0.432	-0.342	-0.159	-0.253	-0.230	-0.245	0.191
Cl	-0.432	1	0.728	-0.096	0.947	-0.185	0.820	-0.245
Na	-0.342	0.728	1	-0.130	0.617	-0.143	0.608	-0.090
pH	-0.159	-0.096	-0.130	1	-0.192	0.102	-0.197	0.652
SO4	-0.253	0.947	0.617	-0.192	1	-0.138	0.861	-0.277
T	-0.230	-0.185	-0.143	0.102	-0.138	1	0.005	0.002
TDS	-0.245	0.820	0.608	-0.197	0.861	0.005	1	-0.356
Turb	0.191	-0.245	-0.090	0.652	-0.277	0.002	-0.356	1

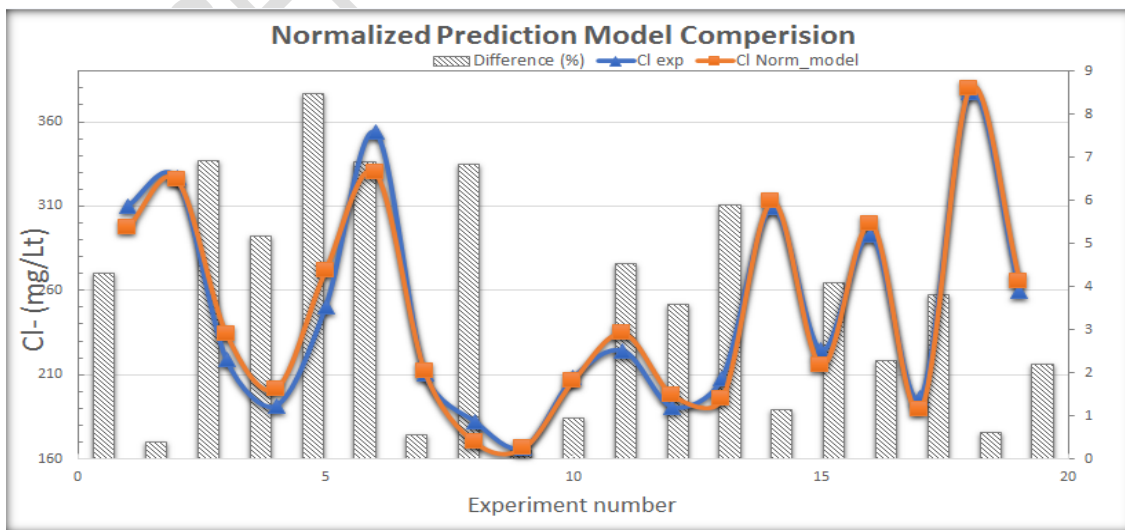
433

434
$$\hat{y} = ((\alpha_{n1}x_{n1} + \alpha_{n2}x_{n2} + \alpha_{n3}x_{n3} + \alpha_{n4}x_{n4} + \alpha_{n5}x_{n5} + \alpha_{n6}x_{n6} + \alpha_{n7}x_{n7} + \beta n) * (y_{max} - y_{min})) + y_{min}. \quad (10)$$

436

437
$$\hat{y}_{Cl} = ((-0.2x_{BOD5} + 0.197x_{Na} + 0.083x_{pH} + 0.874x_{SO4} - 0.09x_T - 0.0167x_{TDS} - 0.0346x_{Turb} + 0.0867) * (377.52 - 166.76)) + 166.76 \quad (11)$$

438 Each of the coefficients derived from the developed Cl prediction model reveals its effects on the model more
 439 clearly. The SO4 concentration, for instance, has a coefficient of 0.874 and is the most useful parameter in the Cl
 440 prediction model. Table 5's correlation data show that the correlation between Cl and SO4 is 0.9471. The table
 441 below contains a comparison of experimental Cl data and Cl values (Fig.12). The normalized model (Norm_model)
 442 performance is also fairly strong, as seen in the graph.



443

444 **Fig. 13.** Experimental and Normalized prediction model comparison plot for Cl with difference percentage.

445 The data are highly comparable when compared to the Normalized prediction model (Norm model) graphs and
 446 the Cl prediction model (model) graphs shown in Fig. 6. and 10 above. In addition, other parameters (Na, SO4,
 447 and BOD5) were studied and the compatibility of graphics and models was observed. In order to understand the
 448 comparison, the aggregated table (table 8) of the r, MSE and MAPE values of the models and normalized models
 449 is shown below. For researchers working on the topic, it will be simpler and clearer to evaluate the impact of each
 450 parameter on the parameter to be estimated in the estimation model created over normalized models.

451 **Table 8** Statistical table of prediction models (Model and normalized model (Norm model)).
 452

Parameters	MSE		MAPE		r	
	Model	Norm_model	Model	Norm_model	Model	Norm_model
SO4	151.061	151.4883	3.731	3.748	0.979	0.979
Cl	118.716	118.716	3.627	3.627	0.984	0.984
Na	292.661	292.661	8.695	8.695	0.823	0.823
BOD5	0.224	0.224	20.737	20.737	0.784	0.784

453

454 The Kızılırmak River, where the investigation was done, was given the created equations and estimating models.
 455 The parameter values of each river and their connections to the parameters make it impossible to consider this
 456 equation to be a general one. This study's objective is to show the modeling steps that can be used for each station
 457 with the modeling steps completed.

458 5. Discussion

459 Water quality parameters are of great importance in monitoring river pollution. It is necessary to analyze these
 460 parameters regularly, follow the changes and obtain information about the river. However, compiling this data is
 461 a difficult process and requires high costs. Along with the cost of analysis materials, expert personnel expenses
 462 are also quite high. Some problems encountered during the collection of this data are:

- 463 1. In on-site analyses, the values of some parameters are recorded incorrectly due to seasonal factors.
- 464 2. Due to the same seasonal reasons, the sample used in the measurement of some parameters cannot be stored
 465 properly, resulting in the experiments not being carried out, which leads to incomplete data.
- 466 3. Difficulties in tracking or estimating may arise if on-site measurements of certain parameters are disregarded or
 467 not gathered because of expense.

468 In this research, various solution methods for the three problems mentioned above were examined and the most
 469 suitable methods were tested with real data. To address analysis errors, the widely accepted boxplot method
 470 developed by Tukey, J. W. (1977) in the literature has been used to clean possible outliers in the data set.

471 There are many methods in the literature to correct missing data. Among these methods, linear regression was
 472 considered to be the most suitable for data with seasonal fluctuations. To complete the missing data, correlation
 473 analysis was performed to determine the relationship between the parameters, and an equation was created between
 474 the highly correlated parameters by determining the slope and intercept to create a linear regression equation with
 475 the existing data. Linear regression equation of more related parameter has been used as input for missing data.
 476 This method was repeated for each missing data and all deficiencies in the data set were completed.

477 At this stage, due to most of the data from February 2013 being missing, no imputation was done for this month,
 478 and all data for this month has been removed from the dataset The data set obtained after this stage was used for
 479 multivariate analyses.

480 Starting from the hypothesis of whether this parameter would be predictable if one of the parameters in the data
 481 set was missing, statistical analyzes were carried out again and parameters that could be estimated based on
 482 correlations were determined. At this stage, a multivariate regression model was created to determine the 8th
 483 parameter using 7 parameters. During the research, studies were conducted on the parameters SO4, Cl-, Na+, and
 484 BOD5. However, comparison tables are presented in the article only for Cl. In addition, the entire data set was
 485 normalized, the multivariate prediction model was run again, and comparison tables with real values were prepared
 486 so that the researchers could examine and interpret the parameters. It was examined whether the data obtained
 487 from the prediction model was within acceptable limits through statistical analysis.

488

489 The model obtained in this study was also examined with data obtained from different rivers, but the developed
490 prediction model did not produce very good results on different rivers. This is because rivers have different
491 characteristics from each other. However, each river can be modeled uniquely by performing prediction model
492 studies with a good data set. It is possible to perform predictive modeling studies on all rivers and get positive
493 results with new and comprehensive data sets, the process steps of which are presented in this study.

494 In this study, Minitab, Excel, and MATLAB program softwares were used for statistical analysis, calculations, and
495 graphics. VBscript was user for GUI

496

497 **6. Recommendation**

498 In many nations, there are legislative regulations governing the routine monitoring of water resources, and these
499 regulations are implemented by approved institutions and organizations. Experts have developed a variety of very
500 different techniques for monitoring water resources. Water quality monitoring can be achieved using various
501 models, from ANNs to genetic algorithms and artificial intelligence. In this study, data taken from one of the
502 stations of the Kızılırmak River was used, and the analyzes were carried out by the state institution responsible for
503 legal water monitoring. Because of data pollution, a problem that always exists with data sets, the series set was
504 first checked for outliers using the boxplot approach, and the data new set was then purified of them. Values
505 captured in the data set due to extreme values and seasonal factors were eliminated and imputation operations were
506 carried out for missing data and the data set was arranged. Thus, a new and reliable data set was created.

507 8 parameters from the edited data set (BOD5, Cl, Na, pH, SO4, T, TDS, Turb) were selected for the study. A
508 multivariate statistical model was developed using the least squares approach and a prediction model was created
509 for SO4, Cl, Na and BOD5. MSE, r, and MAPE values were used to study the accuracy of the model and compare
510 it with real values, and it was determined that the developed prediction model gave a usable prediction value. The
511 data set's parameter values were normalized to make it easier for researchers to see the effects of the parameters
512 and to interpret the graphs and statistical tables. All values were converted to the range of 0–1, and new models
513 were established for the chosen parameters, even though the estimation model produced accurate results. These
514 estimating models' output values passed the tests of statistical analysis (MSE, r, and MAPE) and were judged to
515 be accurate.

516 The following is an important point that researchers should focus on because, the relationships between the
517 parameters of each river vary and it is not possible to utilize the above - derived coefficients and provided models
518 directly. The variables identified by this study are related to one another. Examining the properties of many rivers
519 reveals that even the limit values and average values vary. In terms of techniques and coefficients, this paper offers
520 significant support to academics working on ANN modeling and machine learning algorithms. The output values
521 of these estimating models were found to be accurate and to have passed the statistical analysis tests (MSE, r, and
522 MAPE).

523 The following is a crucial topic that researchers should focus on because, the relationships between the parameters
524 of each river vary and it is not possible to utilize the above-derived coefficients and provided models directly. The
525 variables identified by this study are related to one another. Examining the properties of many rivers reveals that
526 even the limit values and average values vary. In terms of techniques and coefficients, this paper offers great
527 support to academics working on ANN modeling and machine learning algorithms.

528 A post-study recommendation to the researchers might be to develop a multivariate statistical estimating model
529 employing data from more stations along the same river, for this purpose, samples taken from more station
530 locations in shorter time intervals should be taken into account in the calculations. Additional parameters affected
531 by the values of the change rates of these parameters are expressed only in that river.

532 The computations for this should take samples from more station locations into account.

533 Additionally, by employing the above methods and adding more parameters to the models while using a larger
534 data set, more successful models can be attained in parameter estimations of the river of interest.

535

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675

676 **Statements & Declarations**

677 There isn't a conflict of interest or duty sharing because this study has just one author. There is no private
678 information in the article because the data used was tabulated.

679 Artificial intelligence was not used in this research.

680 **Ethical Approval**

681 This study is a research carried out for "Water Quality Parameter Estimation Method". The purpose of this study
682 is to show that a parameter that an unmeasured parameter can be estimated by a multivariate regression method
683 with eliminating missing data. Research data were taken from State Water Works. The statistical values of the data
684 were shared for study confidentiality reasons. There is no personal information in the study.

685 **Consent to Participate**

686 No personal data was used in the study.

687 **Consent to Publish**

688 "I have not submitted my manuscript to a preprint server before submitting it to Environmental Science and
689 Pollution Research"

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694 **Competing Interests**

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