

# Empirical correlation with dimensionless parameters for following the kinetic separation performance via reverse osmosis desalination process of groundwater

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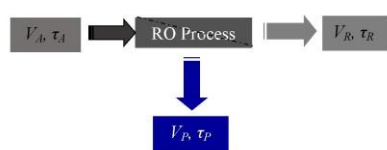
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## Graphical abstract

Summary of dimensionless parameters inputs for following the performance of GWRO process.



## Abstract

The present paper carries for novel modeling that are often used for evaluate the kinetic performance of groundwater reverse osmosis (GWRO) desalination system by empirical correlation with dimensionless parameters. About three hundred dimensionless empirical correlations have been proposed and validated for the calculation of three cumulative dimensionless volumes: alimentation, permeate and rejection as a function of the dimensionless filtration time and vice versa. This correlation has obtained by inspiration of the models already proposed in the literature from four unitary operation processes: filtration, adsorption, drying and extraction. The experimental data consists of 2561 points taken during the lifetime of 66 organics RO membranes. The interpreting of regression and residual results is validated by four statistical criteria: reduced chi-Sqr, residual sum of residual, r-square (COD) and adj. R-square ( $R^2$ ) and with two criteria in ANOVA analysis: sum of squares, mean square. Results show that 95 dimensionless empirical correlations (DEC) among 192 are highly capable to describe the separation kinetics on reverse osmosis desalination system curve with a least  $R^2$  was around 0.970 in comparison to the best correlation (DEC 1) with  $R^2$  of 0,998, 0,995 and 0,993 for alimentation, permeate and rejection, respectively, with negligible

errors and perfect alignment of correlation with RO kinetic separation according to statistical criteria.

**Keywords:** dimensionless empirical correlation, reverse osmosis process, kinetic separation, desalination.

## 1. Introduction

Reverse-osmosis (RO) process is one of the most popular technologies for purifying seawater (Elimelech *et al.*, 2011), groundwater and brackish water (Pearson *et al.*, 2021; Ling *et al.*, 2021; Al-Obaidia *et al.*, 2018; Dimitriou *et al.*, 2017; Reverberi *et al.*, 2011; Hoek *et al.*, 2008), because this process presents by: high efficiency, simple, eco-friendly and nature-friendly technology for a wide range of issues in various fields (Qasim *et al.*, 2019; Aladwani *et al.*, 2021; Zhang *et al.*, 2022). Few models have been developed and analyzed the kinetic separation of solvent and solute fluxes through RO membranes (Najid *et al.*, 2022; Haluch *et al.*, 2017; Ibrar *et al.*, 2020; Xu *et al.*, 2020; Niewersch *et al.*, 2020; Chong *et al.*, 2022). These studies were begun in the early 1950's with Samuel T. Yuster who imagined the concept of utilizing the Gibb's adsorption equation as a road map to discover methods for making fresh water from brackish water and seawater (Gu *et al.*, 2021; Ghernaout, 2017; Haluch *et al.*, 2017; Choi and Kim, 2015; Bartman, 2011; Mehdizadeh, 1990; Soltanieh, 1981). Other classical approaches have been studied, such as removal, fouling and biofouling resistance, osmotic pressure models which are complicated, not good predictive of kinetic separation or treated smallest experimental data. Furthermore, they don't take into account the subtle coupling between hydrodynamics, mass transfer in the bulk solution and membrane transport. Moreover, the evaluation of rejection rate is not provided by such models: theoretical, empirical and semi-empirical model. Therefore, process design still heavily relies on time-consuming pilot experiments. This disadvantage is even more serious when scarce or costly materials and hazardous substances are used or treated (Jogdand and Chaudhuri, 2015; Al-

Obaidiet *et al.*, 2018; Dimitriou *et al.*, 2017; Haluch *et al.*, 2017). For these purposes, dimensionless empirical correlations are very convenient as they combined rapidly, low cost and relatively easy implementation. The current work consists to developing a predictive dimensionless empirical correlation for applications ranging from reverse osmosis. The dimensionless empirical correlations do not use any experimental coefficients; it depends only on cumulative and maximum volume, instantly and maximum time of filtration. These inspired correlations have been obtained by analogy from the kinetic models of four unitary operations already proposed in the literature: filtration, adsorption, drying and extraction. The validation of tested correlations is made via statistical criteria and analysis of variance (ANOVA).

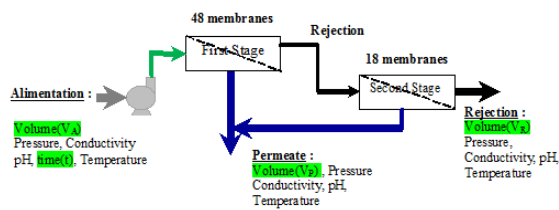


Figure 1. Simplified flowsheet of GWRO.

## 2. Materials and methods

### 2.1. Description of GWRO and plant data

The experiments were carried out at the Antibiotics Complex of Medea (Algeria). The groundwater (GWRO) was treated on three parts before using to an injectable ampule production. The practical operation of its desalination process effected during the life of the membrane (4 years). The water stream coming from the pre-treatment unit processed in a RO plant operating according to the scheme illustrated in Figure 1. Eleven modules constitute the RO plant depicted in Figure 1. They arranged in two stages in serial. The first and second stages contain six and five modules, respectively. Any module contains six membranes. Each of the pressure vessels of the RO plant containing a spiral wound polyamide membrane (ROGA® - HR 8.5") having a surface area of 38.6 m<sup>2</sup>. The data consists of 2561×3 matrix. It collected every 2 hours for five seasons.

Table 1. The dimension and dimensionless variables range.

| Ranges of variable | Dimension variable                                |   |   |                           | Dimensionless variable |                |                |   |
|--------------------|---|---|---|---------------------------|------------------------|----------------|----------------|---|
|                    | 10 <sup>-6</sup> v <sub>P</sub> (m <sup>3</sup> ) | 10 <sup>-6</sup> v <sub>R</sub> (m <sup>3</sup> ) | 10 <sup>-6</sup> v <sub>A</sub> (m <sup>3</sup> ) | 10 <sup>-3</sup> t(hours) | V <sub>P</sub>         | V <sub>R</sub> | V <sub>A</sub> | τ |
| min                | 0   | 0   | 0   | 0                         | 0                      | 0              | 0              | 0 |
| max                | 2144,07   | 1496,72   | 3603,78   | 36,37                     | 1                      | 1              | 1              | 1 |

### 2.2.2. Normalization of correlation constants

In order to limit the values of the correlation constants, normalization of this was done by the equation below:

$$a_n = 2 \times \frac{a_i - a_i(\min)}{a_i(\max) - a_i(\min)} - 1 \quad (4)$$

## 2.2. Modeling of separation on GWRO membrane

### 2.2.1. Empirical modeling

A dimensionless correlation was proposed for separation kinetic of GWRO desalination system filtration [ $v = F(\tau)$ ], which are recorded in Table 1. These correlations are obtained by inspiration from the four processes models already proposed in the literature: adsorption, drying, extraction and filtration. i.e., for separation on GWRO system, we keep the same empirical correlations of adsorption and extraction upstream and for drying and extraction downstream with:

$$V = \frac{v}{v_m} \quad (1)$$

and

$$\tau = \frac{t}{t_m} \quad (2)$$

V: cumulative dimensionless volume of the filtrate at time  $\tau$ . v: cumulative volume of the filtrate at time  $t$  (m<sup>3</sup>). v<sub>m</sub>: maximum cumulative volume of the filtrate at time  $t$  (m<sup>3</sup>). t: filtration time (hours). t<sub>m</sub>: maximum filtration time (hours).  $\tau$ : dimensionless filtration time.

Such as the modeling method that is often used to evaluate kinetic performance of GWRO desalination system by empirical correlation with dimensionless parameters was summarized in the Figure 2.

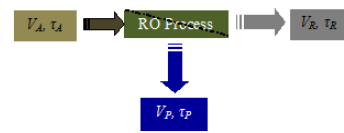


Figure 2. Summary of dimensionless parameters inputs for following the performance of GWRO process.

These proposed additional empirical correlations verify the initial condition:

$$\lim_{t \rightarrow 0} v = 0 \quad (3)$$

The ranges of variables used in this work are given in Table 1.

Such us,  $a_n$ : Normalized correlation constants;  $a_i$ : Correlation constants.

### 2.3. Regression analysis of results

Regression is commonly used to compute the best fit line. The performance of the regression analysis will produce an analysis report sheet outlining the regression results for each model. The performance an empirical correlation with dimensionless numbers for following the kinetic

separation were analyzed and improved via sets of statistical criteria as though reduced chi-Sqr, residual sum of residual, r-square (COD) and adj. R-square ( $R^2$ ) and as well, with two ANOVA analysis criteria such as sum of squares and mean square. All these statistical criteria were calculated by Origin 2021b software (Alkarkhi and Wasin, 2020; Siegel and Wagner, 2022).

### 2.3.1. Residual Sum of Squares (RSS)

Residual Sum of Squares is the sum of the square of the vertical deviations from database point to the fitting regression line. It can be inferred that the database is perfect fit if the value of RSS is equal to zero. This statistic can help to decide if the fitted regression line is a good fit for our database (Williams and Quave, 2019; Siegel and Wagner, 2022).

### 2.3.2. Scale error with sqrt (Reduced Chi-Sqr)

The Reduced Chi-square value, which is also called Scale Error with square, is equal to the residual sum of square (RSS) divided by the degree of freedom. Typically, a Reduced Chi-square value close to 1 indicates a good fit result, and it implies that the difference between observed database and fitted data is consistent with the error variance. If the error variance is over-estimated, the Reduced Chi-square value will be much less than 1. For under-estimated error variance, it will be much greater than 1 (Wilcox, 2022; Tyagi et al., 2022).

### 2.3.3. R-square (COD)

R-square, which is also known as the coefficient of determination (COD), is a statistical measure to qualify the linear regression. It is a percentage of the response variable variation that explained by the fitted regression line of correlation. Hence, R-square is always between 0 and 1. In general, the larger the R-square, the better the fitted line fits the databases (Wilcox, 2022; Siegel and Wagner, 2022).

### 2.3.4. Adj. R-Square

The Adj. R-square is a modified version of R-square, which is adjusted for the number of predictors in the fitted line. Thus, it can be used to compare with the fitted lines of the correlation with different numbers of predictors. If the number of predictors is greater than 1, Adj.-square is always smaller than R-square (Mostoufi and Constantinides, 2023; Siegel and Wagner, 2022).

## 3. Results and discussion

### 3.1. Regression analysis of dimensionless empirical correlations via GWRO kinetics

The optimizing DEC obtained from the best correlation fits are summarized in Tables 2–4. The average of these parameters for about 2561 data points covering the 95 kinetics are presented in Table 3.

**Table 2.** The dimensionless empirical correlations of the GWRO kinetics

| DEC | Equations   |
|-----|---|
| 1.  | $V = \frac{1 - \exp[-(a_1 \cdot \tau + a_2 \cdot \tau^{a_3})]}{[1 + a_4 \cdot \exp(-a_5 \cdot \tau + a_6 \cdot \tau^{a_7})]^{a_8}}$             |
| 2.  | $V = a_1 - a_1 \cdot \exp(-a_2 \cdot \tau^{a_3}) - a_4 \cdot \tau^2 - a_5 \cdot \tau$   |
| 3.  | $\tau = [a_1 \cdot V^{2a_2} + a_3 \cdot V^{a_4}]^{1/a_5}$   |
| 4.  | $\tau = a_1 \cdot V^{2a_2} + a_3 \cdot V^{a_2}$   |
| 5.  | $V = \frac{a_1 \cdot \tau^{a_2} \cdot [1 - a_3 \cdot \exp(-a_4 \cdot \tau^{a_5})]}{a_6 + a_7 \cdot \tau^{a_8}}$                                 |
| 6.  | $V = (a_1 \cdot \tau + a_2 \cdot \tau^{a_3}) [1 - (\exp(-a_4 + a_5 \cdot \tau + a_6 \cdot \tau^{a_7}))]$  |
| 7.  | $V = 1 - \frac{1 - a_1 \cdot \tau^{a_2} \cdot \exp(-a_3 \cdot \tau^{a_2})}{[1 - a_1 \cdot \tau^{a_4} \cdot \exp(-a_5 \cdot \tau^{a_2})]^{a_6}}$ |
| 8.  | $V = 1 - [1 - a_1 \cdot \tau^{a_2} \cdot \exp(-a_3 \cdot \tau^{a_4})]^{a_5}$  |
| 9.  | $V = \frac{1 - \exp(-a_1 \cdot \tau^{a_2})}{\left(1 + \frac{a_3}{(1 + a_4)^{a_5}} \cdot \exp(-a_6 \cdot \tau^{a_7})\right)^{a_5}}$              |
| 10. | $V = a_1 \cdot \tau^{a_2} + [1 - \exp(-a_3 \cdot \tau^{a_4})]$  |
| 11. | $V = 1 + a_1 \cdot \tau^{a_2} - \exp(-a_3 \cdot \tau^{a_4})$  |

|     |   |
|-----|---|
| 12. | $V = I + a_1.\tau^{a_2} + a_3.\tau^{a_4} - \exp\left[-a_5.(a_6.\tau^{a_7} + a_8.\tau^{a_9})\right]$ |
| 13. | $V = \left(\frac{a_1.\tau^{a_2}}{a_3 + a_4.\tau^{a_5}}\right)^{a_6}$                                |
| 14. | $V = a_1.[I - \exp(-a_2.\tau^{a_3})]^{a_4}$   |
| 15. | $V = a_1.[I - \exp(-a_2.\tau^{a_3})]^{a_4}$   |
| 16. | $V = a_1.[I - \exp(-a_2.\tau^{a_3})]^{a_4}$   |
| 17. | $V = a_1.[I - \exp(-a_2.\tau^{a_3})]^{a_4}$   |
| 18. | $V = \frac{a_1.\tau^{a_2}.[I - \exp(-a_3.\tau^{a_4})]}{I + a_5.\tau^{a_6}}$                         |
| 19. | $V = \frac{a_1.\tau^{a_2}}{I + a_3.\tau^{a_4}}$   |
| 20. | $V = \left[\frac{(a_1.\tau)^{a_2}}{I + a_3.\tau^{a_4}}\right]^{a_5}$                                |
| 21. | $V = \frac{a_1.\tau^{a_2}}{a_3 + a_4.\tau^{a_5}}$   |
| 22. | $V = \frac{a_1.\tau^{a_2}}{I + a_3.\tau^{a_4}}$   |
| 23. | $V = \frac{a_1.\tau^{a_2}}{a_3 + a_4.\tau^{a_5}}$   |
| 24. | $V = a_1.\tau^{a_2}.\exp(-a_3.\tau^{a_4})$  |
| 25. | $V = a_1.\tau^{a_2}.\exp(-a_3.\tau^{a_4})$  |
| 26. | $V = (a_1 + a_2.\tau + a_3.\tau^{a_4}).[I - \exp(-(a_1.\tau + a_2.\tau^{a_5}))]$                    |
| 27. | $V = I - \exp(-a_1.\tau^{a_2}) - a_3.\tau^{a_4}$  |
| 28. | $V = \frac{I - \exp[-(a_1.\tau + a_2.\tau^{a_3})]}{I + a_4.\exp[-(a_5.a_2 + a_6.\tau^{a_7})]}$      |
| 29. | $V = I - a_1.\exp(-a_2.\tau^{a_3}) - (I - a_1).\exp(-a_4.\tau)$                                     |
| 30. | $V = a_1.\tau^{a_2}.[\exp(-a_3.\tau^{a_2})]$  |
| 31. | $V = I - a_1.a_2.\exp(-a_3.\tau^{a_4}) - (I - a_1.a_2).\exp(-a_5.\tau^{a_6})$                       |
| 32. | $V = I - a_1.\exp(-a_2.\tau^{a_3}) - (I - a_1).\exp(-a_2.a_4.\tau^{a_5})$                           |
| 33. | $V = I - a_1.\exp(-a_2.\tau^{a_3}) - (I - a_1).\exp(-a_4.\tau^{a_5})$                               |
| 34. | $V = I - a_1^{a_2}.\exp(-a_3.\tau^{a_4}) - (I - a_1^{a_2}).\exp(-a_5.\tau^{a_6})$                   |
| 35. | $V = a_1 * [I - \exp(-a_2.\tau^{a_3})]$   |

|     |  |
|-----|--|
| 36. | $V = l - a_1.a_2.(-a_3.\tau^{a_4}) - (l - a_1.a_2).exp(-a_5.\tau^{a_4})$                         |
| 37. | $V = a_1.\tau^{a_2} + [l - exp(-a_3.\tau^{a_2})]$  |
| 38. | $V = \left[ \frac{a_1.\tau}{a_2 + a_3.\tau} \right]^{a_4}$                                       |
| 39. | $V = l - exp(-a_1.\tau^{a_2} - a_3.\tau^{a_4})$  |
| 40. | $V = \left[ \frac{a_1.\tau^{a_2}}{a_3 + a_1.\tau^{a_2}} \right]^{a_4}$                           |
| 41. | $V = [l - exp(-a_1.\tau^{a_2})]^{a_3}$   |
| 42. | $V = [l - exp(-a_1.\tau + a_2)]\tau^{a_3+a_4.\tau}$  |
| 43. | $V = a_1.\tau + a_2.\tau^{a_3} + l - [exp(-a_4.\tau^{a_5} + a_6.\tau^{a_7})]$                    |
| 44. | $V = a_1.\tau^{a_2}.exp(-a_3.\tau^{a_4}) - a_5.\tau^{a_6}$                                       |
| 45. | $V = a_1.\tau.[l - exp(-a_2.\tau + a_3.\tau^{a_4})]$   |
| 46. | $V = a_1.\tau + a_2.\tau^2 + a_3.\tau^{a_4}$   |
| 47. | $V = \frac{[l + a_1.exp(-a_2.\tau)]^{a_3}}{l + [l - a_4.exp(-a_5.\tau)]^{a_6}}$                  |
| 48. | $V = a_1.\tau - a_2.\tau^2$  |
| 49. | $V = a_1.\tau^{a_2} + a_3.\tau^{a_4}$  |
| 50. | $V = a_1.\tau^{a_2}$   |
| 51. | $V = \frac{a_1.\tau^{a_2}}{a_3 + (a_4 - l).\tau^{a_5}}$  |
| 52. | $V = a_1.\tau^{a_2}$   |
| 53. | $V = l - exp(-a_1.\tau^{a_2}) - a_3.\tau$  |
| 54. | $V = \frac{(a_1.\tau)^{a_2}}{(l + (a_1.\tau)^{a_2})}$  |
| 55. | $V = l - a_1^{a_2}.exp(-a_3.\tau) - (l - a_4.a_1^{a_2}).exp(-a_5.\tau)$                          |
| 56. | $V = \frac{a_1.\tau}{l + a_2.\tau^{a_3}}$  |
| 57. | $V = l - a_1^{a_2}.exp(-a_3.\tau^{a_4}) - (l - a_1^{a_2}).exp(-a_5.\tau^{a_4})$                  |
| 58. | $V = l - exp[-a_1.\tau^{a_2} - a_3.\tau]$  |
| 59. | $V = l - exp[-a_1.(a_2.\tau + a_3.\tau^{a_4})]$  |
| 60. | $V = [l - exp(-a_1.\tau^{a_2})]^{1/2}$   |
| 61. | $V = [l - exp(-a_1.\tau^{a_2})]^{1/2}$   |
| 62. | $V = 2.a_1 - (a_1 - a_2).[exp(-a_3.a_4.\tau) - a_1.exp(-a_5.a_4.\tau) - a_2.exp(-a_6.a_4.\tau)]$ |

|     |   |
|-----|---|
| 63. | $V = I - a_1 \cdot \exp(-a_2 \cdot \tau^{a_3}) + a_4 \cdot \tau^{a_5}$  |
| 64. | $V = I - a_1 \cdot \exp(-a_2 \cdot \tau^{a_3}) - (I - a_1) \cdot \exp(-a_4 \cdot a_5 \cdot \tau^{a_3})$   |
| 65. | $V = I - a_1 \cdot (\tau^{a_2} - \tau^{a_3})$   |
| 66. | $V = I - a_1 \cdot \exp(a_2 \cdot (I - \tau)^{a_3}) - (I - a_4) \cdot \exp(a_2 \cdot a_4 \cdot (I - \tau)^{a_5})$                                   |
| 67. | $V = I - a_1 \cdot \exp(-a_2 \cdot \tau^{a_3})$   |
| 68. | $V = I - [a_1 \cdot \exp(-a_2 \cdot \tau^{a_3})]^{a_4}$   |
| 69. | $V = I - a_1 \cdot \exp(-a_2 \cdot \tau) - (I - a_1) \cdot \tau \cdot \exp(-a_3 \cdot \tau)$  |
| 70. | $V = I - a_1 \cdot \exp(-a_2 \cdot (I - \tau)^{a_3}) - (I - a_1) \cdot \exp(-a_4 \cdot (I - \tau))$   |
| 71. | $V = I - \exp(-a_1 \cdot \tau^{a_2})$   |
| 72. | $V = I - \exp(-a_1 \cdot \tau^{a_2})$   |
| 73. | $V = I - \exp\left(a_1 \cdot \left(\frac{\tau}{a_2^2}\right)^{a_3}\right)$  |
| 74. | $V = \frac{a_1 \cdot \tau^{a_2} \cdot (I - \exp(-a_3 \cdot \tau^{a_2}))}{I + a_1 \cdot \tau^{a_2}}$   |
| 75. | $V = I - \exp\left[-\left(\frac{\tau}{a_1}\right)^{a_2}\right]$   |
| 76. | $V = I - \frac{I + a_1 \cdot \tau^{a_2} \cdot \ln(I + a_3 \cdot \tau^{a_2})}{[I + a_1 \cdot \tau^{a_4} \cdot \ln(I + a_3 \cdot \tau^{a_4})]^{a_5}}$ |
| 77. | $V = a_1 \cdot \tau^{a_2} \cdot [\exp(-(a_3 \cdot \tau + a_4))]^{a_4 \cdot \tau + a_5}$   |
| 78. | $V = I - \frac{a_1 \cdot \tau^{a_2}}{a_3 + a_4 \cdot \tau^{a_5}}$   |
| 79. | $V = \frac{a_1 \cdot \tau}{I + a_2 \cdot \tau}$   |
| 80. | $V = I - a_1 \cdot \tau^{a_2} \cdot [\exp(-(a_3 \cdot \tau + a_4)^{a_5 \cdot \tau + a_6})]$   |
| 81. | $V = \frac{a_1 \cdot [I - \exp(-a_2 \cdot \tau)]^{a_3}}{I + (a_1 - I) \cdot [I - \exp(-a_4 \cdot \tau)]^{a_5}}$                                     |
| 82. | $V = \frac{(a_1 \cdot \tau)^{a_2}}{I + (a_1 \cdot \tau)^{a_2}}$   |
| 83. | $V = \frac{a_1 \cdot \tau^{a_2}}{I + a_1 \cdot \tau^{a_2}}$   |
| 84. | $V = \frac{a_1 \cdot \tau^{a_2}}{a_3 + a_1 \cdot \tau^{a_2}}$   |
| 85. | $V = I - \exp(-a_1 \cdot \tau^2 - a_2 \cdot \tau)$  |

|     |   |
|-----|---|
| 86. | $V = 1 - a_1 \cdot \tau^{a_2} \cdot \exp(-a_3 \cdot \tau^{a_4})$  |
| 87. | $V = a_1 \cdot \tau^{a_2} \cdot [\exp(-(a_3 \cdot \tau + a_4)^{a_5 \tau + a_6})]$                         |
| 88. | $V = 1 - \exp(-a_1 \cdot \tau) - (1 - a_2) \cdot \tau^{a_3} \cdot \exp(-a_4 \cdot \tau)$                  |
| 89. | $V = 1 - a_1 \exp(-a_2 \cdot \tau) - (1 - a_1) \cdot \exp(-a_3 \cdot \tau)$                               |
| 90. | $V = 1 - \left( \frac{1}{1 + (a_1 - 1) \cdot a_2 \cdot \tau} \right)^{\frac{1}{a_1 - 1}}$                 |
| 91. | $V = 2 \cdot a_1 - a_1 \cdot \exp(-a_2 \cdot a_3 \cdot \tau) - a_1 \cdot \exp(-a_4 \cdot a_3 \cdot \tau)$ |
| 92. | $V = 1 - a_1 \cdot \tau^{a_2} \cdot \exp(-a_3 \cdot \tau^{a_2})$  |
| 93. | $V = 1 - \exp(-a_1 \cdot \tau^{a_2}) - a_3 \cdot \tau^{a_2}$  |
| 94. | $V = a_1 \cdot \tau^{a_2} \cdot [\exp(-(a_3 \cdot \tau^{a_4} + a_5))]^{a_5 \cdot \tau + a_6}$             |
| 95. | $V = a_1 - a_2 \cdot \exp[-a_3 \cdot (a_4 + a_5 \cdot \tau)^{a_6}]$                                       |

**Table 3.** Statistic value for dimensionless empirical correlations of  $V_A$ ,  $V_P$  and  $V_R$ 

| DEC | $V_A$   |                |                 |         | $V_P$   |                |                 |          | $V_R$   |                |                 |          |
|-----|---------|----------------|-----------------|---------|---------|----------------|-----------------|----------|---------|----------------|-----------------|----------|
|     | COD     | R <sup>2</sup> | Reduced Chi-Sqr | RSS     | COD     | R <sup>2</sup> | Reduced Chi-Sqr | RSS      | COD     | R <sup>2</sup> | Reduced Chi-Sqr | RSS      |
| 1   | 0,99861 | 0,9986         | 1,17E-04        | 0,29884 | 0,9957  | 0,99568        | 1,81E-05        | 0,04626  | 0,99374 | 0,99372        | 2,69E-05        | 0,06854  |
| 2   | 0,99857 | 0,99857        | 1,20E-04        | 0,30632 | 0,62188 | 0,62129        | 0,00159         | 4,06381  | 0,6504  | 0,64985        | 0,0015          | 3,82783  |
| 3   | 0,99799 | 0,99799        | 1,35E-04        | 0,34533 | 0,93029 | 0,93018        | 0,00468         | 11,93783 | 0,97173 | 0,97168        | 0,0019          | 4,8415   |
| 4   | 0,99794 | 0,99794        | 1,38E-04        | 0,35392 | 0,85666 | 0,85655        | 0,00961         | 24,548   | 0,90582 | 0,90575        | 0,00631         | 16,12802 |
| 5   | 0,99751 | 0,9975         | 2,09E-04        | 0,5341  | 0,98444 | 0,98439        | 6,56E-05        | 0,16727  | 0,98669 | 0,98665        | 5,71E-05        | 0,14573  |
| 6   | 0,99749 | 0,99749        | 2,10E-04        | 0,53677 | 0,95293 | 0,9528         | 1,98E-04        | 0,50586  | 0,96214 | 0,96204        | 1,63E-04        | 0,41452  |
| 7   | 0,99749 | 0,99749        | 2,10E-04        | 0,53705 | 0,74242 | 0,74192        | 0,00108         | 2,7683   | 0,8639  | 0,86363        | 1,49021         | 0,8639   |
| 8   | 0,99748 | 0,99748        | 2,11E-04        | 0,53904 | 0,97833 | 0,9783         | 9,12E-05        | 0,23287  | 0,98238 | 0,98236        | 0,19288         | 0,98238  |
| 9   | 0,99747 | 0,99747        | 2,12E-04        | 0,5419  | 0,98222 | 0,98218        | 7,49E-05        | 0,19108  | 0,98484 | 0,98481        | 6,50E-05        | 0,16594  |
| 10  | 0,99747 | 0,99747        | 2,12E-04        | 0,54146 | 0,97591 | 0,97588        | 1,01E-04        | 0,25893  | 0,97957 | 0,97954        | 8,76E-05        | 0,22373  |
| 11  | 0,99747 | 0,99747        | 2,12E-04        | 0,54146 | 0,97591 | 0,97588        | 1,01E-04        | 0,25893  | 0,97957 | 0,97954        | 8,76E-05        | 0,22373  |
| 12  | 0,99747 | 0,99747        | 2,12E-04        | 0,54135 | 0,55051 | 0,5491         | 0,0019          | 4,83086  | 0,56428 | 0,56292        | 0,00187         | 4,77073  |
| 13  | 0,99747 | 0,99747        | 2,12E-04        | 0,54155 | 0,98592 | 0,98589        | 5,93E-05        | 0,15136  | 0,68702 | 0,68641        | 0,00134         | 3,42684  |
| 14  | 0,99747 | 0,99747        | 2,12E-04        | 0,54151 | 0,53542 | 0,53487        | 0,00195         | 4,99304  | 0,56358 | 0,56306        | 0,00187         | 4,77847  |
| 15  | 0,99747 | 0,99747        | 2,12E-04        | 0,54151 | 0,53542 | 0,53487        | 0,00195         | 4,99304  | 0,56358 | 0,56306        | 0,00187         | 4,77847  |
| 16  | 0,99747 | 0,99747        | 2,12E-04        | 0,54151 | 0,53542 | 0,53487        | 0,00195         | 4,99304  | 0,56358 | 0,56306        | 0,00187         | 4,77847  |
| 17  | 0,99747 | 0,99747        | 2,12E-04        | 0,54151 | 0,53542 | 0,53487        | 0,00195         | 4,99304  | 0,56358 | 0,56306        | 0,00187         | 4,77847  |
| 18  | 0,99747 | 0,99747        | 2,12E-04        | 0,54152 | 0,97585 | 0,9758         | 1,02E-04        | 0,25953  | 0,97989 | 0,97985        | 8,63E-05        | 0,22021  |
| 19  | 0,99747 | 0,99747        | 2,12E-04        | 0,54155 | 0,97585 | 0,97583        | 1,02E-04        | 0,2595   | 0,97989 | 0,97987        | 8,62E-05        | 0,2202   |
| 20  | 0,99747 | 0,99747        | 2,12E-04        | 0,54159 | 0,53547 | 0,53475        | 0,00196         | 4,99243  | 0,56363 | 0,56295        | 0,00187         | 4,77788  |
| 21  | 0,99747 | 0,99747        | 2,12E-04        | 0,5415  | 0,65611 | 0,65557        | 0,00145         | 3,69591  | 0,68707 | 0,68657        | 0,00134         | 3,42638  |
| 22  | 0,99747 | 0,99747        | 2,12E-04        | 0,54155 | 0,97585 | 0,97583        | 1,02E-04        | 0,2595   | 0,97989 | 0,97987        | 8,62E-05        | 0,2202   |
| 23  | 0,99747 | 0,99747        | 2,12E-04        | 0,5415  | 0,65611 | 0,65557        | 0,00145         | 3,69591  | 0,68707 | 0,68657        | 0,00134         | 3,42638  |
| 24  | 0,99747 | 0,99747        | 2,12E-04        | 0,54144 | 0,90925 | 0,90915        | 3,82E-04        | 0,9753   | 0,92541 | 0,92532        | 3,20E-04        | 0,81672  |
| 25  | 0,99747 | 0,99747        | 2,12E-04        | 0,54144 | 0,90925 | 0,90915        | 3,82E-04        | 0,9753   | 0,92541 | 0,92532        | 3,20E-04        | 0,81672  |
| 26  | 0,99747 | 0,99747        | 2,12E-04        | 0,54144 | 0,90925 | 0,90915        | 3,82E-04        | 0,9753   | 0,92541 | 0,92532        | 3,20E-04        | 0,81672  |
| 27  | 0,99747 | 0,99747        | 2,12E-04        | 0,54164 | 0,50533 | 0,50456        | 0,00208         | 5,3164   | 0,53218 | 0,53145        | 0,00201         | 5,12224  |
| 28  | 0,99746 | 0,99746        | 2,13E-04        | 0,54429 | 0,96767 | 0,96763        | 1,36E-04        | 0,34749  | 0,97957 | 0,97954        | 8,76E-05        | 0,22373  |

|    |         |         |          |         |           |           |          |           |           |          |          |           |
|----|---------|---------|----------|---------|-----------|-----------|----------|-----------|-----------|----------|----------|-----------|
| 29 | 0,99745 | 0,99745 | 2,14E-04 | 0,54566 | 0,9236    | 0,92342   | 3,22E-04 | 0,82109   | 0,98485   | 0,98481  | 6,50E-05 | 0,16591   |
| 30 | 0,99745 | 0,99745 | 2,13E-04 | 0,54558 | 0,9812    | 0,98118   | 7,91E-05 | 0,20201   | 0,98413   | 0,98411  | 6,81E-05 | 0,17381   |
| 31 | 0,99746 | 0,99745 | 2,13E-04 | 0,54513 | 0,88815   | 0,88807   | 4,70E-04 | 1,20206   | 0,90605   | 0,90597  | 4,03E-04 | 1,02869   |
| 32 | 0,99746 | 0,99745 | 2,13E-04 | 0,54511 | 0,75831   | 0,75784   | 0,00102  | 2,59749   | 0,78626   | 0,78584  | 9,17E-04 | 2,34033   |
| 33 | 0,99746 | 0,99745 | 2,13E-04 | 0,54484 | 0,98151   | 0,98148   | 7,78E-05 | 0,19874   | 0,98437   | 0,98434  | 6,70E-05 | 0,17115   |
| 34 | 0,99746 | 0,99745 | 2,13E-04 | 0,54484 | 0,98116   | 0,98113   | 7,93E-05 | 0,2025    | 0,98404   | 0,98402  | 6,84E-05 | 0,17473   |
| 35 | 0,99746 | 0,99745 | 2,13E-04 | 0,54512 | 0,98116   | 0,98112   | 7,94E-05 | 0,20251   | 0,98404   | 0,98401  | 6,85E-05 | 0,17473   |
| 36 | 0,99745 | 0,99745 | 2,13E-04 | 0,54585 | 0,66491   | 0,66465   | 0,00141  | 3,60129   | 0,28173   | 0,28116  | 0,00308  | 7,86451   |
| 37 | 0,99744 | 0,99744 | 2,15E-04 | 0,54828 | 0,97348   | 0,97344   | 1,12E-04 | 0,28505   | 0,97761   | 0,97758  | 9,60E-05 | 0,24512   |
| 38 | 0,99744 | 0,99744 | 2,14E-04 | 0,54825 | 0,97324   | 0,97322   | 1,13E-04 | 0,28763   | 0,97761   | 0,9776   | 9,59E-05 | 0,24512   |
| 39 | 0,99741 | 0,9974  | 2,17E-04 | 0,55566 | 0,93071   | 0,93063   | 2,92E-04 | 0,74469   | 0,92925   | 0,92916  | 3,03E-04 | 0,77469   |
| 40 | 0,99735 | 0,99735 | 2,22E-04 | 0,56795 | 0,96767   | 0,96763   | 1,36E-04 | 0,34749   | 0,97315   | 0,97312  | 1,15E-04 | 0,29402   |
| 41 | 0,99734 | 0,99734 | 2,23E-04 | 0,56911 | 0,9818    | 0,98177   | 7,66E-05 | 0,19565   | 0,98568   | 0,98566  | 6,14E-05 | 0,15678   |
| 42 | 0,99734 | 0,99733 | 2,23E-04 | 0,57102 | 0,97121   | 0,97119   | 1,21E-04 | 0,30942   | 0,97737   | 0,97736  | 9,70E-05 | 0,24774   |
| 43 | 0,99733 | 0,99732 | 2,24E-04 | 0,57261 | 0,66227   | 0,66187   | 0,00142  | 3,62974   | 0,69239   | 0,69203  | 0,00132  | 3,36808   |
| 44 | 0,99747 | 0,99747 | 2,12E-04 | 0,54138 | 0,10485   | 0,10274   | 0,00377  | 9,62051   | 0,11094   | 0,10884  | 0,00382  | 9,73452   |
| 45 | 0,9973  | 0,9973  | 2,26E-04 | 0,57814 | 0,94133   | 0,94121   | 2,47E-04 | 0,63056   | 0,95305   | 0,95296  | 2,01E-04 | 0,51407   |
| 46 | 0,9973  | 0,99729 | 2,27E-04 | 0,57957 | 0,89996   | 0,8998    | 4,21E-04 | 1,07519   | 0,91648   | 0,91634  | 3,58E-04 | 0,91452   |
| 47 | 0,9973  | 0,99729 | 2,27E-04 | 0,57944 | 0,89996   | 0,89984   | 4,21E-04 | 1,07518   | 0,91648   | 0,91638  | 3,58E-04 | 0,91452   |
| 48 | 0,9973  | 0,99729 | 2,27E-04 | 0,57882 | 0,11658   | 0,1145    | 0,00372  | 9,49444   | 0,13224   | 0,1302   | 0,00372  | 9,50126   |
| 49 | 0,99693 | 0,99693 | 2,57E-04 | 0,65692 | -11,98906 | -11,99414 | 0,05462  | 139,59824 | -11,49731 | -11,5022 | 0,05353  | 136,83527 |
| 50 | 0,99687 | 0,99687 | 2,62E-04 | 0,67069 | 0,53547   | 0,53493   | 0,00195  | 4,99243   | 0,56363   | 0,56312  | 0,00187  | 4,77787   |
| 51 | 0,99687 | 0,99687 | 2,62E-04 | 0,67069 | 0,53547   | 0,53529   | 0,00195  | 4,99243   | 0,56363   | 0,56346  | 0,00187  | 4,77787   |
| 52 | 0,99687 | 0,99687 | 2,62E-04 | 0,6707  | 0,97585   | 0,97581   | 1,02E-04 | 0,25958   | 0,97988   | 0,97985  | 8,63E-05 | 0,22026   |
| 53 | 0,99687 | 0,99687 | 2,62E-04 | 0,67069 | 0,53547   | 0,53529   | 0,00195  | 4,99243   | 0,56363   | 0,56346  | 0,00187  | 4,77787   |
| 54 | 0,99669 | 0,99668 | 2,78E-04 | 0,70985 | 0,63312   | 0,63283   | 0,00154  | 3,943     | 0,60245   | 0,60214  | 0,0017   | 4,35286   |
| 55 | 0,9966  | 0,9966  | 2,84E-04 | 0,72767 | 0,95324   | 0,95322   | 1,97E-04 | 0,50254   | 0,96424   | 0,96422  | 1,53E-04 | 0,39158   |
| 56 | 0,99564 | 0,99563 | 3,66E-04 | 0,93422 | 0,98794   | 0,98793   | 5,07E-05 | 0,12956   | 0,98962   | 0,98961  | 4,45E-05 | 0,11363   |
| 57 | 0,99529 | 0,99529 | 3,94E-04 | 1,00841 | 0,97245   | 0,97244   | 1,16E-04 | 0,29613   | 0,97721   | 0,9772   | 9,76E-05 | 0,2495    |
| 58 | 0,99481 | 0,9948  | 4,35E-04 | 1,11287 | 0,96767   | 0,96762   | 1,36E-04 | 0,34749   | 0,97315   | 0,9731   | 1,15E-04 | 0,29402   |
| 59 | 0,99418 | 0,99417 | 4,88E-04 | 1,24796 | 0,97583   | 0,97581   | 1,02E-04 | 0,25978   | 0,98107   | 0,98105  | 8,11E-05 | 0,20728   |
| 60 | 0,99418 | 0,99417 | 4,88E-04 | 1,24796 | 0,97604   | 0,97601   | 1,01E-04 | 0,25755   | 0,98107   | 0,98105  | 8,11E-05 | 0,20722   |
| 61 | 0,9941  | 0,9941  | 4,94E-04 | 1,26442 | 0,96137   | 0,96135   | 1,62E-04 | 0,41521   | 0,9653    | 0,96529  | 1,49E-04 | 0,37989   |
| 62 | 0,9941  | 0,9941  | 4,94E-04 | 1,26442 | 0,96137   | 0,96135   | 1,62E-04 | 0,41521   | 0,9653    | 0,96529  | 1,49E-04 | 0,37989   |
| 63 | 0,99372 | 0,99371 | 5,26E-04 | 1,34478 | 0,97926   | 0,97922   | 8,73E-05 | 0,22288   | 0,98015   | 0,98011  | 8,52E-05 | 0,21739   |
| 64 | 0,99246 | 0,99245 | 6,32E-04 | 1,6151  | 0,44676   | 0,44568   | 0,00233  | 5,94584   | 0,48634   | 0,48534  | 0,0022   | 5,62414   |
| 65 | 0,99229 | 0,99228 | 6,46E-04 | 1,65202 | 0,98192   | 0,98189   | 7,61E-05 | 0,19429   | 0,97314   | 0,9731   | 1,15E-04 | 0,29404   |
| 66 | 0,99222 | 0,99221 | 6,52E-04 | 1,66758 | 0,44273   | 0,44229   | 0,00234  | 5,9892    | 0,47259   | 0,47218  | 0,00226  | 5,77472   |
| 67 | 0,99182 | 0,9918  | 6,86E-04 | 1,75326 | 0,89486   | 0,89466   | 4,43E-04 | 1,12993   | 0,89702   | 0,89682  | 1,12751  | 0,89702   |
| 68 | 0,99165 | 0,99164 | 7,00E-04 | 1,78983 | 0,96773   | 0,96771   | 1,36E-04 | 0,34677   | 0,97322   | 0,9732   | 1,15E-04 | 0,2932    |
| 69 | 0,99165 | 0,99163 | 7,00E-04 | 1,78983 | 0,96773   | 0,96768   | 1,36E-04 | 0,34677   | 0,97322   | 0,97318  | 1,15E-04 | 0,2932    |
| 70 | 0,99131 | 0,9913  | 7,28E-04 | 1,86148 | 0,97771   | 0,97768   | 9,38E-05 | 0,23961   | 0,97403   | 0,974    | 1,11E-04 | 0,2843    |
| 71 | 0,99095 | 0,99094 | 7,59E-04 | 1,93938 | 0,85878   | 0,85856   | 5,95E-04 | 1,51777   | 0,85134   | 0,85111  | 6,38E-04 | 1,62765   |
| 72 | 0,98942 | 0,98942 | 8,86E-04 | 2,2669  | 0,96767   | 0,96765   | 1,36E-04 | 0,34749   | 0,97315   | 0,97314  | 1,15E-04 | 0,29402   |
| 73 | 0,98942 | 0,98941 | 8,86E-04 | 2,2669  | 0,96767   | 0,96764   | 1,36E-04 | 0,34749   | 0,97315   | 0,97313  | 1,15E-04 | 0,29402   |
| 74 | 0,98942 | 0,98941 | 8,86E-04 | 2,26702 | 0,96767   | 0,96764   | 1,36E-04 | 0,34749   | 0,97315   | 0,97313  | 1,15E-04 | 0,29402   |
| 75 | 0,98942 | 0,98941 | 8,86E-04 | 2,26689 | 0,97781   | 0,97779   | 9,33E-05 | 0,23851   | 0,55185   | 0,5515   | 0,00192  | 4,90688   |



|    |          |          |          |           |          |          |          |          |         |         |          |          |
|----|----------|----------|----------|-----------|----------|----------|----------|----------|---------|---------|----------|----------|
| 76 | 0,98942  | 0,98941  | 8,86E-04 | 2,26689   | 0,96767  | 0,96764  | 1,36E-04 | 0,34749  | 0,97315 | 0,97313 | 1,15E-04 | 0,29402  |
| 77 | 0,98886  | 0,98884  | 9,34E-04 | 2,38766   | 0,97977  | 0,97974  | 8,52E-05 | 0,2174   | 0,98321 | 0,98319 | 7,20E-05 | 0,1838   |
| 78 | 0,98848  | 0,98846  | 9,66E-04 | 2,46894   | 0,87347  | 0,87322  | 5,33E-04 | 1,35989  | 0,87063 | 0,87038 | 5,55E-04 | 1,41649  |
| 79 | 0,98547  | 0,98545  | 0,00122  | 3,113     | 0,83464  | 0,83438  | 6,96E-04 | 1,77721  | 0,85079 | 0,85056 | 6,40E-04 | 1,63371  |
| 80 | 0,98103  | 0,98102  | 0,00159  | 4,06468   | 0,95739  | 0,95738  | 1,79E-04 | 0,4579   | 0,96789 | 0,96788 | 1,38E-04 | 0,35154  |
| 81 | 0,98104  | 0,981    | 0,00159  | 4,06347   | -0,07376 | -0,07586 | 0,00452  | 11,54006 | 0,96328 | 0,96321 | 1,58E-04 | 0,40201  |
| 82 | 0,97462  | 0,97458  | 0,00213  | 5,43757   | 0,98418  | 0,98416  | 6,66E-05 | 0,17     | 0,98652 | 0,9865  | 5,78E-05 | 0,14763  |
| 83 | 0,97397  | 0,97396  | 0,00218  | 5,57792   | 0,07573  | 0,07536  | 0,00389  | 9,93352  | 0,07285 | 0,07248 | 0,00397  | 10,15155 |
| 84 | 0,97397  | 0,97396  | 0,00218  | 5,57804   | 0,97535  | 0,97534  | 1,04E-04 | 0,26491  | 0,97829 | 0,97828 | 9,30E-05 | 0,23769  |
| 85 | 0,97397  | 0,97395  | 0,00218  | 5,57795   | 0,97535  | 0,97535  | 1,04E-04 | 0,2649   | 0,97829 | 0,97827 | 9,30E-05 | 0,23769  |
| 86 | 0,97233  | 0,97232  | 0,00232  | 5,92875   | 0,94867  | 0,94865  | 2,16E-04 | 0,55162  | 0,93942 | 0,9394  | 2,60E-04 | 0,6633   |
| 87 | 0,75643  | 0,75614  | 0,02041  | 52,19179  | 0,96765  | 0,96761  | 1,36E-04 | 0,34768  | 0,97147 | 0,97143 | 1,22E-04 | 0,31242  |
| 88 | 0,97062  | 0,97055  | 0,00247  | 6,2958    | 0,93696  | 0,93681  | 2,66E-04 | 0,67751  | 0,94952 | 0,9494  | 2,17E-04 | 0,5527   |
| 89 | 0,96505  | 0,96501  | 0,00293  | 7,48858   | 0,98231  | 0,98229  | 7,44E-05 | 0,19012  | 0,98505 | 0,98504 | 6,41E-05 | 0,16365  |
| 90 | 0,93121  | 0,93116  | 0,00576  | 14,73953  | 0,98098  | 0,98096  | 8,00E-05 | 0,20445  | 0,93368 | 0,93363 | 2,84E-04 | 0,72613  |
| 91 | 0,90466  | 0,90463  | 0,00798  | 20,42827  | 0,97725  | 0,97724  | 9,56E-05 | 0,24448  | 0,98169 | 0,98168 | 7,84E-05 | 0,20047  |
| 92 | 0,83059  | 0,83039  | 0,0142   | 36,30168  | 0,97178  | 0,97175  | 1,19E-04 | 0,3033   | 0,97201 | 0,97198 | 1,20E-04 | 0,30648  |
| 93 | 0,75643  | 0,75614  | 0,02041  | 52,19179  | 0,96765  | 0,96761  | 1,36E-04 | 0,34768  | 0,97147 | 0,97143 | 1,22E-04 | 0,31242  |
| 94 | 0,34804  | 0,34753  | 0,05461  | 139,69978 | 0,97324  | 0,97322  | 1,13E-04 | 0,28763  | 0,97761 | 0,9776  | 9,59E-05 | 0,24512  |
| 95 | -1,41905 | -1,42474 | 0,20295  | 518,34669 | 0,96723  | 0,96715  | 1,38E-04 | 0,35219  | 0,97389 | 0,97383 | 1,12E-04 | 0,28583  |

**Table 4.** ANOVA values for dimensionless empirical correlations concerning  $V_A$ ,  $V_P$ ,  $V_R$ 

| DEC | $V_A$                     |                        |                         |                      | $V_P$                     |                        |                         |                      | $V_R$                     |                        |                         |                      |
|-----|---------------------------|------------------------|-------------------------|----------------------|---------------------------|------------------------|-------------------------|----------------------|---------------------------|------------------------|-------------------------|----------------------|
|     | Sum of Squares-Regression | Mean Square-Regression | Sum of Squares-Residual | Mean Square-Residual | Sum of Squares-Regression | Mean Square-Regression | Sum of Squares-Residual | Mean Square-Residual | Sum of Squares-Regression | Mean Square-Regression | Sum of Squares-Residual | Mean Square-Residual |
| 1   | 519,04785                 | 64,88098               | 0,29884                 | 1,17E-04             | 2479,43397                | 309,92925              | 0,04626                 | 1,81E-05             | 2474,44991                | 309,30624              | 0,06854                 | 2,69E-05             |
| 2   | 519,04037                 | 103,80807              | 0,30632                 | 1,20E-04             | 2475,41643                | 495,08329              | 4,06381                 | 0,00159              | 2470,69063                | 494,13813              | 3,82783                 | 0,0015               |
| 3   | 859,34167                 | 171,86833              | 0,34533                 | 1,35E-04             | 844,75345                 | 168,95069              | 11,93783                | 0,00468              | 851,84978                 | 170,36996              | 4,8415                  | 0,0019               |
| 4   | 859,33308                 | 286,44436              | 0,35392                 | 1,38E-04             | 832,14328                 | 277,38109              | 24,548                  | 0,00961              | 840,56326                 | 280,18775              | 16,12802                | 0,00631              |
| 5   | 518,81259                 | 64,85157               | 0,5341                  | 2,09E-04             | 2479,31297                | 309,91412              | 0,16727                 | 6,56E-05             | 2474,37273                | 309,29659              | 0,14573                 | 5,71E-05             |
| 6   | 518,80992                 | 64,85124               | 0,53677                 | 2,10E-04             | 2478,97438                | 309,8718               | 0,50586                 | 1,98E-04             | 2474,10394                | 309,26299              | 0,41452                 | 1,63E-04             |
| 7   | 518,80964                 | 86,46827               | 0,53705                 | 2,10E-04             | 2476,71194                | 412,78532              | 2,7683                  | 0,00108              | 2473,02825                | 412,17137              | 1,49021                 | 5,84E-04             |
| 8   | 518,80765                 | 103,76153              | 0,53904                 | 2,11E-04             | 2479,24737                | 495,84947              | 0,23287                 | 9,12E-05             | 2474,32558                | 494,86512              | 0,19288                 | 7,56E-05             |
| 9   | 518,80479                 | 74,11497               | 0,5419                  | 0,5419               | 2479,28916                | 354,18417              | 0,19108                 | 7,49E-05             | 2474,35252                | 353,47893              | 0,16594                 | 6,50E-05             |
| 10  | 518,80523                 | 129,70131              | 0,54146                 | 2,12E-04             | 2479,22131                | 619,80533              | 0,25893                 | 1,01E-04             | 2474,29473                | 618,57368              | 0,22373                 | 8,76E-05             |
| 11  | 518,80523                 | 129,70131              | 0,54146                 | 2,12E-04             | 2479,22131                | 619,80533              | 0,25893                 | 1,01E-04             | 2474,29473                | 618,57368              | 0,22373                 | 8,76E-05             |
| 12  | 518,80534                 | 57,64504               | 0,54135                 | 2,12E-04             | 2474,64938                | 274,96104              | 4,83086                 | 0,0019               | 2469,74773                | 274,41641              | 4,77073                 | 0,00187              |
| 13  | 518,80514                 | 86,46752               | 0,54155                 | 2,12E-04             | 2479,32888                | 413,22148              | 0,15136                 | 5,93E-05             | 2471,09162                | 411,8486               | 3,42684                 | 0,00134              |
| 14  | 518,80518                 | 129,7013               | 0,54151                 | 2,12E-04             | 2474,4872                 | 618,6218               | 4,99304                 | 0,00195              | 2469,73999                | 617,435                | 4,77847                 | 0,00187              |
| 15  | 518,80518                 | 129,7013               | 0,54151                 | 2,12E-04             | 2474,4872                 | 618,6218               | 4,99304                 | 0,00195              | 2469,73999                | 617,435                | 4,77847                 | 0,00187              |
| 16  | 518,80518                 | 129,7013               | 0,54151                 | 2,12E-04             | 2474,4872                 | 618,6218               | 4,99304                 | 0,00195              | 2469,73999                | 617,435                | 4,77847                 | 0,00187              |
| 17  | 518,80518                 | 129,7013               | 0,54151                 | 2,12E-04             | 2474,4872                 | 618,6218               | 4,99304                 | 0,00195              | 2469,73999                | 617,435                | 4,77847                 | 0,00187              |
| 18  | 518,80517                 | 86,46753               | 0,54152                 | 2,12E-04             | 2479,22071                | 413,20345              | 0,25953                 | 1,02E-04             | 2474,29825                | 412,38304              | 0,22021                 | 8,63E-05             |
| 19  | 518,80514                 | 129,70128              | 0,54155                 | 2,12E-04             | 2479,22074                | 619,80518              | 0,2595                  | 1,02E-04             | 2474,29826                | 618,57457              | 0,2202                  | 8,62E-05             |
| 20  | 518,8051                  | 103,76102              | 0,54159                 | 2,12E-04             | 2474,48781                | 494,89756              | 4,99243                 | 0,00196              | 2469,74058                | 493,94812              | 4,77788                 | 0,00187              |
| 21  | 518,80519                 | 103,76104              | 0,5415                  | 2,12E-04             | 2475,78433                | 495,15687              | 3,69591                 | 0,00145              | 2471,09208                | 494,21842              | 3,42638                 | 0,00134              |
| 22  | 518,80514                 | 129,70128              | 0,54155                 | 2,12E-04             | 2479,22074                | 619,80518              | 0,2595                  | 1,02E-04             | 2474,29826                | 618,57457              | 0,2202                  | 8,62E-05             |
| 23  | 518,80519                 | 103,76104              | 0,5415                  | 2,12E-04             | 2475,78433                | 495,15687              | 3,69591                 | 0,00145              | 2471,09208                | 494,21842              | 3,42638                 | 0,00134              |
| 24  | 518,80525                 | 129,70131              | 0,54144                 | 2,12E-04             | 2478,50494                | 619,62623              | 0,9753                  | 3,82E-04             | 2473,70173                | 618,42543              | 0,81672                 | 3,20E-04             |
| 25  | 518,80525                 | 129,70131              | 0,54144                 | 2,12E-04             | 2478,50494                | 619,62623              | 0,9753                  | 3,82E-04             | 2473,70173                | 618,42543              | 0,81672                 | 3,20E-04             |
| 26  | 518,80505                 | 103,76101              | 0,54164                 | 2,12E-04             | 2474,16384                | 494,83277              | 5,3164                  | 0,00208              | 2469,39622                | 493,87924              | 5,12224                 | 0,00201              |
| 27  | 518,8024                  | 129,7006               | 0,54429                 | 2,13E-04             | 2479,13275                | 619,78319              | 0,34749                 | 1,36E-04             | 2474,29473                | 618,57368              | 0,22373                 | 8,76E-05             |
| 28  | 518,80103                 | 74,11443               | 0,54566                 | 2,14E-04             | 2478,65915                | 354,09416              | 0,82109                 | 3,22E-04             | 2474,35255                | 353,47894              | 0,16591                 | 6,50E-05             |
| 29  | 518,80111                 | 129,70028              | 0,54558                 | 2,13E-04             | 2479,27823                | 619,81956              | 0,20201                 | 7,91E-05             | 2474,34465                | 618,58616              | 0,17381                 | 6,81E-05             |

|    |           |           |          |          |            |            |           |          |            |            |           |          |
|----|-----------|-----------|----------|----------|------------|------------|-----------|----------|------------|------------|-----------|----------|
| 30 | 518,80156 | 172,93385 | 0,54513  | 2,13E-04 | 2478,27817 | 826,09272  | 1,20206   | 4,70E-04 | 2473,48977 | 824,49659  | 1,02869   | 4,03E-04 |
| 31 | 518,80158 | 86,46693  | 0,54511  | 2,13E-04 | 2476,88275 | 412,81379  | 2,59749   | 0,00102  | 2472,17813 | 412,02969  | 2,34033   | 9,17E-04 |
| 32 | 518,80185 | 103,76037 | 0,54484  | 2,13E-04 | 2479,2815  | 495,8563   | 0,19874   | 7,78E-05 | 2474,34731 | 494,86946  | 0,17115   | 6,70E-05 |
| 33 | 518,80185 | 103,76037 | 0,54484  | 2,13E-04 | 2479,27774 | 495,85555  | 0,2025    | 7,93E-05 | 2474,34373 | 494,86875  | 0,17473   | 6,84E-05 |
| 34 | 518,80157 | 86,46693  | 0,54512  | 2,13E-04 | 2479,27773 | 413,21296  | 0,20251   | 7,94E-05 | 2474,34373 | 412,39062  | 0,17473   | 6,85E-05 |
| 35 | 518,80084 | 172,93361 | 0,54585  | 2,13E-04 | 2475,87895 | 825,29298  | 3,60129   | 0,00141  | 2466,65395 | 822,21798  | 7,86451   | 0,00308  |
| 36 | 518,79841 | 103,75968 | 0,54828  | 2,15E-04 | 2479,19519 | 495,83904  | 0,28505   | 1,12E-04 | 2474,27334 | 494,85467  | 0,24512   | 9,60E-05 |
| 37 | 518,79844 | 172,93281 | 0,54825  | 2,14E-04 | 2479,1926  | 826,39753  | 0,28763   | 1,13E-04 | 2474,27334 | 824,75778  | 0,24512   | 9,59E-05 |
| 38 | 518,79103 | 129,69776 | 0,55566  | 2,17E-04 | 2478,73555 | 619,68389  | 0,74469   | 2,92E-04 | 2473,74377 | 618,43594  | 0,77469   | 3,03E-04 |
| 39 | 518,77874 | 129,69468 | 0,56795  | 2,22E-04 | 2479,13275 | 619,78319  | 0,34749   | 1,36E-04 | 2474,22444 | 618,55611  | 0,29402   | 1,15E-04 |
| 40 | 518,77758 | 129,6944  | 0,56911  | 2,23E-04 | 2479,28459 | 619,82115  | 0,19565   | 7,66E-05 | 2474,36167 | 618,59042  | 0,15678   | 6,14E-05 |
| 41 | 518,77567 | 172,92522 | 0,57102  | 2,23E-04 | 2479,17082 | 826,39027  | 0,30942   | 1,21E-04 | 2474,27072 | 824,75691  | 0,24774   | 9,70E-05 |
| 42 | 518,77408 | 129,69352 | 0,57261  | 2,24E-04 | 2475,8505  | 618,96263  | 3,62974   | 0,00142  | 2471,15038 | 617,78759  | 3,36808   | 0,00132  |
| 43 | 518,80531 | 74,11504  | 0,54138  | 2,12E-04 | 2469,85973 | 352,8371   | 9,62051   | 0,00377  | 2464,78394 | 352,11199  | 9,73452   | 0,00382  |
| 44 | 518,76855 | 86,46143  | 0,57814  | 2,26E-04 | 2478,84968 | 413,14161  | 0,63056   | 2,47E-04 | 2474,00439 | 412,33407  | 0,51407   | 2,01E-04 |
| 45 | 518,76712 | 103,75342 | 0,57957  | 2,27E-04 | 2478,40505 | 495,68101  | 1,07519   | 4,21E-04 | 2473,60394 | 494,72079  | 0,91452   | 3,58E-04 |
| 46 | 518,76725 | 129,69181 | 0,57944  | 2,27E-04 | 2478,40506 | 619,60126  | 1,07518   | 4,21E-04 | 2473,60394 | 618,40098  | 0,91452   | 3,58E-04 |
| 47 | 518,76787 | 74,1097   | 0,57882  | 2,27E-04 | 2469,9858  | 352,85511  | 9,49444   | 0,00372  | 2465,0172  | 352,14531  | 9,50126   | 0,00372  |
| 48 | 518,68977 | 259,34488 | 0,65692  | 2,57E-04 | 2339,882   | 1169,941   | 139,59824 | 0,05462  | 2337,68319 | 1168,8416  | 136,83527 | 0,05353  |
| 49 | 518,676   | 129,669   | 0,67069  | 2,62E-04 | 2474,48781 | 618,62195  | 4,99243   | 0,00195  | 2469,74058 | 617,43515  | 4,77787   | 0,00187  |
| 50 | 518,67599 | 259,338   | 0,67069  | 2,62E-04 | 2474,48781 | 1237,24391 | 4,99243   | 0,00195  | 2469,74058 | 1234,87029 | 4,77787   | 0,00187  |
| 51 | 518,67599 | 103,7352  | 0,6707   | 2,62E-04 | 2479,22066 | 495,84413  | 0,25958   | 1,02E-04 | 2474,2982  | 494,85964  | 0,22026   | 8,63E-05 |
| 52 | 518,67599 | 259,338   | 0,67069  | 2,62E-04 | 2474,48781 | 1237,24391 | 4,99243   | 0,00195  | 2469,74058 | 1234,87029 | 4,77787   | 0,00187  |
| 53 | 518,63684 | 172,87895 | 0,70985  | 2,78E-04 | 2475,53724 | 825,17908  | 3,943     | 0,00154  | 2470,1656  | 823,38853  | 4,35286   | 0,0017   |
| 54 | 518,61902 | 259,30951 | 0,72767  | 2,84E-04 | 2478,9777  | 1239,48885 | 0,50254   | 1,97E-04 | 2474,12688 | 1237,06344 | 0,39158   | 1,53E-04 |
| 55 | 518,41247 | 103,68249 | 0,93422  | 3,66E-04 | 2479,35068 | 495,87014  | 0,12956   | 5,07E-05 | 2474,40483 | 494,88097  | 0,11363   | 4,45E-05 |
| 56 | 518,33828 | 259,16914 | 1,00841  | 3,94E-04 | 2479,18411 | 1239,59205 | 0,29613   | 1,16E-04 | 2474,26896 | 1237,13448 | 0,2495    | 9,76E-05 |
| 57 | 518,23382 | 103,64676 | 1,11287  | 4,35E-04 | 2479,13275 | 495,82655  | 0,34749   | 1,36E-04 | 2474,22444 | 494,84489  | 0,29402   | 1,15E-04 |
| 58 | 518,09873 | 172,69958 | 1,24796  | 4,88E-04 | 2479,22046 | 826,40682  | 0,25978   | 1,02E-04 | 2474,31118 | 824,77039  | 0,20728   | 8,11E-05 |
| 59 | 518,09873 | 129,52468 | 1,24796  | 4,88E-04 | 2479,22269 | 619,80567  | 0,25755   | 1,01E-04 | 2474,31124 | 618,57781  | 0,20722   | 8,11E-05 |
| 60 | 518,08227 | 259,04114 | 1,26442  | 4,94E-04 | 2479,06503 | 1239,53251 | 0,41521   | 1,62E-04 | 2474,13857 | 1237,06928 | 0,37989   | 1,49E-04 |
| 61 | 518,08227 | 259,04114 | 1,26442  | 4,94E-04 | 2479,06503 | 1239,53251 | 0,41521   | 1,62E-04 | 2474,13857 | 1237,06928 | 0,37989   | 1,49E-04 |
| 62 | 518,00191 | 86,33365  | 1,34478  | 5,26E-04 | 2479,25736 | 413,20956  | 0,22288   | 8,73E-05 | 2474,30107 | 412,38351  | 0,21739   | 8,52E-05 |
| 63 | 517,73159 | 86,2886   | 1,6151   | 6,32E-04 | 2473,5344  | 412,25573  | 5,94584   | 0,00233  | 2468,89432 | 411,48239  | 5,62414   | 0,0022   |
| 64 | 517,69467 | 103,53893 | 1,65202  | 6,46E-04 | 2479,28595 | 495,85719  | 0,19429   | 7,61E-05 | 2474,22441 | 494,84488  | 0,29404   | 1,15E-04 |
| 65 | 517,67911 | 172,5597  | 1,66758  | 6,52E-04 | 2473,49104 | 824,49701  | 5,9892    | 0,00234  | 2468,74374 | 822,91458  | 5,77472   | 0,00226  |
| 66 | 517,59343 | 86,26557  | 1,75326  | 6,86E-04 | 2478,35031 | 413,05838  | 1,12993   | 4,43E-04 | 2473,39095 | 412,23183  | 1,12751   | 4,42E-04 |
| 67 | 517,55686 | 172,51895 | 1,78983  | 7,00E-04 | 2479,13347 | 826,37782  | 0,34677   | 1,36E-04 | 2474,22525 | 824,74175  | 0,2932    | 1,15E-04 |
| 68 | 517,55686 | 103,51137 | 1,78983  | 7,00E-04 | 2479,13347 | 495,82669  | 0,34677   | 1,36E-04 | 2474,22525 | 494,84505  | 0,2932    | 1,15E-04 |
| 69 | 517,48521 | 129,3713  | 1,86148  | 7,28E-04 | 2479,24063 | 619,81016  | 0,23961   | 9,38E-05 | 2474,23416 | 618,55854  | 0,2843    | 1,11E-04 |
| 70 | 517,40731 | 103,48146 | 1,93938  | 7,59E-04 | 2477,96247 | 495,59249  | 1,51777   | 5,95E-04 | 2472,89081 | 494,57816  | 1,62765   | 6,38E-04 |
| 71 | 517,07979 | 258,5399  | 2,2669   | 8,86E-04 | 2479,13275 | 1239,56637 | 0,34749   | 1,36E-04 | 2474,22444 | 1237,11222 | 0,29402   | 1,15E-04 |
| 72 | 517,07979 | 172,35993 | 2,2669   | 8,86E-04 | 2479,13275 | 826,37758  | 0,34749   | 1,36E-04 | 2474,22444 | 824,74148  | 0,29402   | 1,15E-04 |
| 73 | 517,07967 | 172,35989 | 2,26702  | 8,86E-04 | 2479,13275 | 826,37758  | 0,34749   | 1,36E-04 | 2474,22444 | 824,74148  | 0,29402   | 1,15E-04 |
| 74 | 517,0798  | 172,35993 | 2,26689  | 8,86E-04 | 2479,24173 | 826,41391  | 0,23851   | 9,33E-05 | 2469,61158 | 823,20386  | 4,90688   | 0,00192  |
| 75 | 517,0798  | 172,35993 | 2,26689  | 8,86E-04 | 2479,13275 | 826,37758  | 0,34749   | 1,36E-04 | 2474,22444 | 824,74148  | 0,29402   | 1,15E-04 |
| 76 | 516,95903 | 103,39181 | 2,38766  | 9,34E-04 | 2479,26284 | 495,85257  | 0,2174    | 8,52E-05 | 2474,33466 | 494,86693  | 0,1838    | 7,20E-05 |
| 77 | 516,87775 | 86,14629  | 2,46894  | 9,66E-04 | 2478,12035 | 413,02006  | 1,35989   | 5,33E-04 | 2473,10197 | 412,18366  | 1,41649   | 5,55E-04 |
| 78 | 516,23369 | 103,24674 | 3,113    | 0,00122  | 2477,70302 | 495,5406   | 1,77721   | 6,96E-04 | 2472,88475 | 494,57695  | 1,63371   | 6,40E-04 |
| 79 | 515,28201 | 257,641   | 4,06468  | 0,00159  | 2479,02234 | 1239,51117 | 0,4579    | 1,79E-04 | 2474,16692 | 1237,08346 | 0,35154   | 1,38E-04 |
| 80 | 515,28322 | 85,88054  | 4,06347  | 0,00159  | 2467,94018 | 411,32336  | 11,54006  | 0,00452  | 2474,11645 | 412,35274  | 0,40201   | 1,58E-04 |
| 81 | 513,90912 | 102,78182 | 5,43757  | 0,00213  | 2479,31024 | 495,86205  | 0,17      | 6,66E-05 | 2474,37083 | 494,87417  | 0,14763   | 5,78E-05 |
| 82 | 513,76877 | 256,88439 | 5,57792  | 0,00218  | 2469,54672 | 1234,77336 | 9,93352   | 0,00389  | 2464,36691 | 1232,18345 | 10,15155  | 0,00397  |
| 83 | 513,76865 | 256,88432 | 5,57804  | 0,00218  | 2479,21533 | 1239,60767 | 0,26491   | 1,04E-04 | 2474,28077 | 1237,14039 | 0,23769   | 9,30E-05 |
| 84 | 513,76874 | 171,25625 | 5,57795  | 0,00218  | 2479,21534 | 826,40511  | 0,2649    | 1,04E-04 | 2474,28077 | 824,76026  | 0,23769   | 9,30E-05 |
| 85 | 513,41794 | 256,70897 | 5,92875  | 0,00232  | 2478,92862 | 1239,46431 | 0,55162   | 2,16E-04 | 2473,85516 | 1236,92758 | 0,6633    | 2,60E-04 |
| 86 | 467,1549  | 116,78873 | 52,19179 | 0,02041  | 2479,13256 | 619,78314  | 0,34768   | 1,36E-04 | 2474,20604 | 618,55151  | 0,31242   | 1,22E-04 |
| 87 | 513,05089 | 73,29298  | 6,2958   | 0,00247  | 2478,80273 | 354,11468  | 0,67751   | 2,66E-04 | 2473,96576 | 353,42368  | 0,5527    | 2,17E-04 |
| 88 | 511,85811 | 127,96453 | 7,48858  | 0,00293  | 2479,29012 | 619,82253  | 0,19012   | 7,44E-05 | 2474,35481 | 618,5887   | 0,16365   | 6,41E-05 |

|    |           |           |           |         |            |            |         |          |            |            |         |          |
|----|-----------|-----------|-----------|---------|------------|------------|---------|----------|------------|------------|---------|----------|
| 89 | 504,60716 | 168,20239 | 14,73953  | 0,00576 | 2479,27579 | 826,42526  | 0,20445 | 8,00E-05 | 2473,79233 | 824,59744  | 0,72613 | 2,84E-04 |
| 90 | 498,91842 | 249,45921 | 20,42827  | 0,00798 | 2479,23576 | 1239,61788 | 0,24448 | 9,56E-05 | 2474,31799 | 1237,15899 | 0,20047 | 7,84E-05 |
| 91 | 483,04501 | 120,76125 | 36,30168  | 0,0142  | 2479,17694 | 619,79424  | 0,3033  | 1,19E-04 | 2474,21198 | 618,553    | 0,30648 | 1,20E-04 |
| 92 | 467,1549  | 116,78873 | 52,19179  | 0,02041 | 2479,13256 | 619,78314  | 0,34768 | 1,36E-04 | 2474,20604 | 618,55151  | 0,31242 | 1,22E-04 |
| 93 | 379,64691 | 126,54897 | 139,69978 | 0,05461 | 2479,1926  | 826,39753  | 0,28763 | 1,13E-04 | 2474,27334 | 824,75778  | 0,24512 | 9,59E-05 |
| 94 | 1         | 0,14286   | 518,34669 | 0,20295 | 2479,12805 | 354,16115  | 0,35219 | 1,38E-04 | 2474,23263 | 353,4618   | 0,28583 | 1,12E-04 |
| 95 | 0         | 0         | 519,34669 | 0,20327 | 10,56481   | 2,11296    | 0,18256 | 7,15E-05 | 2471,94528 | 411,99088  | 2,57318 | 0,00101  |

**Table 5.** Estimated model parameters ( $a_i$ ) of 95 equations proposed in this work for  $V_A$ .

| DEC | $a_1$     | $a_2$    | $a_3$      | $a_4$    | $a_5$    | $a_6$    | $a_7$   | $a_8$    | $a_9$   | $a_{10}$ |
|-----|-----------|----------|------------|----------|----------|----------|---------|----------|---------|----------|
| 1   | 1,02521   | 3,15094  | 11,22294   | 8,68E+13 | 47,1946  | 0,03322  | -3,4179 | 0,05526  | ---     | ---      |
| 2   | 0,05385   | 3,53E+09 | 46,46943   | -0,9535  | -0,00985 | ---      | ---     | ---      | ---     | ---      |
| 3   | 0,02552   | 0,22593  | 0,97361    | 0,02682  | 0,07023  | ---      | ---     | ---      | ---     | ---      |
| 4   | 0,44527   | 0,35435  | 0,53726    | ---      | ---      | ---      | ---     | ---      | ---     | ---      |
| 5   | 1,26489   | 1,30891  | 1,03202    | 0,95055  | 0,95596  | 0,73483  | 0,03323 | 30,81155 | ---     | ---      |
| 6   | 11,22445  | 24,7755  | 2,90634    | 0,49054  | -0,66815 | 0,71501  | 0,90637 | ---      | ---     | ---      |
| 7   | 1,3882    | 1,38343  | 0,3239     | 1,16035  | 0,78195  | 0,55423  | ---     | ---      | ---     | ---      |
| 8   | 1,33023   | 1,92063  | 0,28535    | -0,58338 | 1,1311   | ---      | ---     | ---      | ---     | ---      |
| 9   | 1,19839   | 2,20442  | 0,07862    | -0,99981 | -0,11362 | -6,73569 | 0,77656 | ---      | ---     | ---      |
| 10  | 1,60835   | 2,28501  | -0,47      | 2,68787  | ---      | ---      | ---     | ---      | ---     | ---      |
| 11  | 1,60835   | 2,28501  | -0,47      | 2,68787  | ---      | ---      | ---     | ---      | ---     | ---      |
| 12  | 0,13009   | 2,23624  | 0,13009    | 2,23422  | 1,6279   | 0,26525  | 5,00182 | 0,57991  | 2,18165 | ---      |
| 13  | 1,09608   | -0,41501 | 0,23396    | 0,84516  | -4,68045 | 0,50639  | ---     | ---      | ---     | ---      |
| 14  | 1,55944   | 0,53464  | 4,36411    | 0,49539  | ---      | ---      | ---     | ---      | ---     | ---      |
| 15  | 1,55944   | 0,53464  | 4,36411    | 0,49539  | ---      | ---      | ---     | ---      | ---     | ---      |
| 16  | 1,55944   | 0,53464  | 4,36411    | 0,49539  | ---      | ---      | ---     | ---      | ---     | ---      |
| 17  | 1,55944   | 0,53464  | 4,36411    | 0,49539  | ---      | ---      | ---     | ---      | ---     | ---      |
| 18  | 2,77371   | -1,76773 | 0,41013    | 3,92643  | -0,07404 | 2,90398  | ---     | ---      | ---     | ---      |
| 19  | 8,85738   | -2,52073 | 7,79457    | -4,67597 | ---      | ---      | ---     | ---      | ---     | ---      |
| 20  | 1,77019   | 2,01238  | 2,07251    | -4,96836 | 0,30926  | ---      | ---     | ---      | ---     | ---      |
| 21  | 1,03709   | -2,27939 | 0,12166    | 0,90756  | -4,44072 | ---      | ---     | ---      | ---     | ---      |
| 22  | 8,85738   | -2,52073 | 7,79457    | -4,67597 | ---      | ---      | ---     | ---      | ---     | ---      |
| 23  | 1,03709   | -2,27939 | 0,12166    | 0,90756  | -4,44072 | ---      | ---     | ---      | ---     | ---      |
| 24  | 1,14491   | 2,16274  | 0,12802    | 4,19631  | ---      | ---      | ---     | ---      | ---     | ---      |
| 25  | 1,14491   | 2,16274  | 0,12802    | 4,19631  | ---      | ---      | ---     | ---      | ---     | ---      |
| 26  | -0,03463  | 0,94099  | 0,79478    | -0,46828 | 2,24286  | ---      | ---     | ---      | ---     | ---      |
| 27  | 0,88341   | 2,6037   | -0,42431   | 1,83767  | ---      | ---      | ---     | ---      | ---     | ---      |
| 28  | 1,0973    | 0,64854  | 1,13829    | -0,38215 | 1,79606  | -1,42851 | 0,19807 | ---      | ---     | ---      |
| 29  | 2,43656   | 0,52749  | 2,29834    | -0,00948 | ---      | ---      | ---     | ---      | ---     | ---      |
| 30  | 1,27304   | 2,25138  | 0,22883    | ---      | ---      | ---      | ---     | ---      | ---     | ---      |
| 31  | -11,14475 | -5,98751 | 0,24943    | 2,33499  | 0,23409  | 2,34297  | ---     | ---      | ---     | ---      |
| 32  | 1,78225   | 0,64655  | 2,40844    | -0,29283 | 1,61342  | ---      | ---     | ---      | ---     | ---      |
| 33  | 1,77627   | 0,64819  | 2,4095     | -0,19204 | 1,61387  | ---      | ---     | ---      | ---     | ---      |
| 34  | 2,0046    | 4,07717  | 0,27255    | 2,32384  | 0,21108  | 2,35588  | ---     | ---      | ---     | ---      |
| 35  | 2,61153   | 0,49104  | 2,25726    | ---      | ---      | ---      | ---     | ---      | ---     | ---      |
| 36  | 0,01834   | 0,01834  | 1265,03034 | 2,28075  | 0,88933  | ---      | ---     | ---      | ---     | ---      |
| 37  | 0,42856   | 2,27566  | 0,88286    | ---      | ---      | ---      | ---     | ---      | ---     | ---      |
| 38  | 3,62946   | 2,58692  | 1,01616    | 2,55039  | ---      | ---      | ---     | ---      | ---     | ---      |
| 39  | 1,69582   | 2,50341  | 2,35781    | 13,33978 | ---      | ---      | ---     | ---      | ---     | ---      |
| 40  | 23,93459  | 35,09321 | 9,15043    | 0,05853  | ---      | ---      | ---     | ---      | ---     | ---      |

|    |           |           |             |           |           |          |         |     |     |     |
|----|-----------|-----------|-------------|-----------|-----------|----------|---------|-----|-----|-----|
| 41 | 1,80736   | 18,66985  | 0,11095     | ---       | ---       | ---      | ---     | --- | --- | --- |
| 42 | 9,89E+07  | 5,85E+07  | 2,25787     | -0,58071  | ---       | ---      | ---     | --- | --- | --- |
| 43 | -0,00629  | 1,62885   | 2,26461     | -0,23928  | 2,61288   | -0,23928 | 2,61329 | --- | --- | --- |
| 44 | 1,77955   | 1,59739   | -0,36302    | 0,01308   | 1,53178   | 1,3896   | ---     | --- | --- | --- |
| 45 | 12,18648  | -1,06085  | 1,15934     | 0,98165   | ---       | ---      | ---     | --- | --- | --- |
| 46 | -0,17324  | -25,31128 | 26,51063    | 1,99023   | ---       | ---      | ---     | --- | --- | --- |
| 47 | 0,00622   | 18,10413  | 0,15652     | -1,05341  | 0,4154    | 6,47515  | ---     | --- | --- | --- |
| 48 | -0,01779  | -1,05824  | ---         | ---       | ---       | ---      | ---     | --- | --- | --- |
| 49 | 0,51922   | 2,01255   | 0,51922     | 2,01388   | ---       | ---      | ---     | --- | --- | --- |
| 50 | 1,03843   | 2,01314   | ---         | ---       | ---       | ---      | ---     | --- | --- | --- |
| 51 | 0,71598   | 2,01246   | 1,28508     | 0,4044    | 8,19E-04  | ---      | ---     | --- | --- | --- |
| 52 | 1,03843   | 2,01314   | ---         | ---       | ---       | ---      | ---     | --- | --- | --- |
| 53 | 1,53475   | 3,24692   | -0,19526    | ---       | ---       | ---      | ---     | --- | --- | --- |
| 54 | 1,46269   | -1,96442  | ---         | ---       | ---       | ---      | ---     | --- | --- | --- |
| 55 | 1,08672   | 46,59699  | -0,73567    | 0,9991    | -0,75808  | ---      | ---     | --- | --- | --- |
| 56 | -8,30E+35 | -0,92662  | ---         | ---       | ---       | ---      | ---     | --- | --- | --- |
| 57 | 0,07451   | -8,09647  | 0,93333     | 2,71855   | 0,93333   | ---      | ---     | --- | --- | --- |
| 58 | 2,38975   | 4,00029   | 0,24901     | ---       | ---       | ---      | ---     | --- | --- | --- |
| 59 | 0,79142   | 0,31469   | 3,01966     | 4,00061   | ---       | ---      | ---     | --- | --- | --- |
| 60 | 1,93749   | 4,94341   | ---         | ---       | ---       | ---      | ---     | --- | --- | --- |
| 61 | 1,93749   | 4,94341   | ---         | ---       | ---       | ---      | ---     | --- | --- | --- |
| 62 | 3,36089   | 4,35406   | 3,27784     | 0,93104   | 0,29601   | 0,30031  | ---     | --- | --- | --- |
| 63 | 1,01222   | -1,69E+15 | 8,52E+15    | 1,04501   | 1,94978   | ---      | ---     | --- | --- | --- |
| 64 | 1,08525   | 1,96183   | 2,94445     | 2,37E-06  | 2,37E-06  | ---      | ---     | --- | --- | --- |
| 65 | 1,03879   | 2,01396   | 64429,78407 | ---       | ---       | ---      | ---     | --- | --- | --- |
| 66 | 0,08937   | 2,07543   | 0,35951     | 1,06056   | 0,35187   | ---      | ---     | --- | --- | --- |
| 67 | 0,96871   | 2,40706   | 3,31342     | ---       | ---       | ---      | ---     | --- | --- | --- |
| 68 | 0,96265   | 1,94741   | 3,31346     | 0,83529   | ---       | ---      | ---     | --- | --- | --- |
| 69 | 1,09154   | 0,66528   | -3,02797    | ---       | ---       | ---      | ---     | --- | --- | --- |
| 70 | 2,46104   | 0,31193   | 0,05234     | 0,91866   | ---       | ---      | ---     | --- | --- | --- |
| 71 | 2,31296   | 3,03642   | ---         | ---       | ---       | ---      | ---     | --- | --- | --- |
| 72 | 2,8247    | 3,03637   | ---         | ---       | ---       | ---      | ---     | --- | --- | --- |
| 73 | 0,45093   | 3,03095   | ---         | ---       | ---       | ---      | ---     | --- | --- | --- |
| 74 | 1,92E+44  | 3,03603   | 2,31279     | ---       | ---       | ---      | ---     | --- | --- | --- |
| 75 | 0,6479    | 3,03522   | ---         | ---       | ---       | ---      | ---     | --- | --- | --- |
| 76 | 0,66743   | 1,54166   | 0,08461     | 1,5467    | 44,32724  | ---      | ---     | --- | --- | --- |
| 77 | 0,25099   | 1,99577   | 1,20E+05    | -4,04E+04 | -2,04E+04 | ---      | ---     | --- | --- | --- |
| 78 | 0,73216   | -0,03851  | 0,83068     | 5,36124   | 5,29118   | ---      | ---     | --- | --- | --- |
| 79 | 0,3622    | -0,67459  | ---         | ---       | ---       | ---      | ---     | --- | --- | --- |
| 80 | 0,89084   | -0,0581   | 1,80364     | -0,42399  | 1,80364   | -0,42399 | ---     | --- | --- | --- |
| 81 | -4,44251  | 4,12434   | 10,28025    | 10,39576  | 6,60766   | ---      | ---     | --- | --- | --- |
| 82 | 1,51616   | 4,12649   | ---         | ---       | ---       | ---      | ---     | --- | --- | --- |
| 83 | 5,58203   | 4,13203   | ---         | ---       | ---       | ---      | ---     | --- | --- | --- |
| 84 | -367,9288 | 4,12873   | -66,00968   | ---       | ---       | ---      | ---     | --- | --- | --- |
| 85 | 2,38215   | -0,52407  | ---         | ---       | ---       | ---      | ---     | --- | --- | --- |
| 86 | 9,33E+08  | -4,0027   | 21,74897    | -0,1358   | ---       | ---      | ---     | --- | --- | --- |
| 87 | 0,42918   | 1,11955   | -0,18921    | 0,18921   | 1,32518   | -0,46482 | ---     | --- | --- | --- |

|    |            |           |          |          |          |         |     |     |     |     |
|----|------------|-----------|----------|----------|----------|---------|-----|-----|-----|-----|
| 88 | 3,02105    | -33,70161 | 2,03861  | 5,64076  | ---      | ---     | --- | --- | --- | --- |
| 89 | 78,07395   | 3,21628   | 3,27893  | ---      | ---      | ---     | --- | --- | --- | --- |
| 90 | -1,00197   | 0,5003    | ---      | ---      | ---      | ---     | --- | --- | --- | --- |
| 91 | 1846,07783 | 0,00182   | 0,11134  | 0,00182  | ---      | ---     | --- | --- | --- | --- |
| 92 | 9,33E+08   | -4,0027   | 21,74897 | -0,1358  | ---      | ---     | --- | --- | --- | --- |
| 93 | 46,48518   | -0,19539  | 0,5522   | ---      | ---      | ---     | --- | --- | --- | --- |
| 94 | 1          | 1         | 1        | 1        | 1        | 1       | --- | --- | --- | --- |
| 95 | 2,01487    | 2,50454   | -0,73645 | -0,50831 | -8,22496 | 6,87359 | --- | --- | --- | --- |

**Table 6.** Normalized correlation constants ( $a_n$ ) of  $V_A$ .

| DEC | $a_1$              | $a_2$             | $a_3$              | $a_4$              | $a_5$             | $a_6$                |
|-----|--------------------|-------------------|--------------------|--------------------|-------------------|----------------------|
| 1   | -0.999999991354167 | 0.999995822493937 | -0.999999999999982 | 1,00E+00           | 1                 | -0.00525082884619910 |
| 2   | -0.999999991354167 | 1,00E+00          | -0.999999999999974 | -0.999999999069146 | 0.995382794469027 | ---                  |
| 3   | -0.999999991354167 | 0.999995822493933 | -0.999999999999984 | -0.999999999069124 | 0.995390627328406 | ---                  |
| 4   | -0.999999991354167 | 0.999995822493933 | -0.999999999999984 | ---                | ---               | ---                  |
| 5   | -0.999999991354167 | 0.999995822493935 | -0.999999999999984 | -0.999999999069103 | 0.995477263174284 | 0.0978567565661077   |
| 6   | -0.999999991354167 | 0.999995822493962 | -0.999999999999984 | -0.999999999069113 | 0.995318404217662 | 0.0949440381857085   |
| 7   | -0.999999991354167 | 0.999995822493935 | -0.999999999999985 | -0.999999999069098 | 0.995460242746455 | 0.0713160431705424   |
| 8   | -0.999999991354167 | 0.999995822493935 | -0.999999999999985 | -0.999999999069138 | 0.995494394130724 | ---                  |
| 9   | -0.999999991354167 | 0.999995822493936 | -0.999999999999985 | -0.999999999069148 | 0.995372644421353 | -1                   |
| 10  | -0.999999991354167 | 0.999995822493936 | -0.999999999999985 | -0.999999999069063 | ---               | ---                  |
| 11  | -0.999999991354167 | 0.999995822493936 | -0.999999999999985 | -0.999999999069063 | ---               | ---                  |
| 12  | -0.999999991354167 | 0.999995822493936 | -0.999999999999985 | -0.999999999069073 | 0.995542987594005 | 0.0288479625667191   |
| 13  | -0.999999991354167 | 0.999995822493932 | -0.999999999999985 | -0.999999999069105 | 0.994925949401391 | 0.0642855463330903   |
| 14  | -0.999999991354167 | 0.999995822493934 | -0.999999999999984 | -0.999999999069113 | ---               | ---                  |
| 15  | -0.999999991354167 | 0.999995822493934 | -0.999999999999984 | -0.999999999069113 | ---               | ---                  |
| 16  | -0.999999991354167 | 0.999995822493934 | -0.999999999999984 | -0.999999999069113 | ---               | ---                  |
| 17  | -0.999999991354167 | 0.999995822493934 | -0.999999999999984 | -0.999999999069113 | ---               | ---                  |
| 18  | -0.999999991354167 | 0.999995822493931 | -0.999999999999985 | -0.999999999069034 | 0.995376515857095 | 0.416631886477462    |
| 19  | -0.999999991354167 | 0.999995822493930 | -0.999999999999983 | -0.999999999069232 | ---               | ---                  |
| 20  | -0.999999991354167 | 0.999995822493935 | -0.999999999999984 | -0.999999999069239 | 0.995414007552899 | ---                  |
| 21  | -0.999999991354167 | 0.999995822493930 | -0.999999999999985 | -0.999999999069104 | 0.994949398094935 | ---                  |
| 22  | -0.999999991354167 | 0.999995822493930 | -0.999999999999983 | -0.999999999069232 | ---               | ---                  |
| 23  | -0.999999991354167 | 0.999995822493930 | -0.999999999999985 | -0.999999999069104 | 0.994949398094935 | ---                  |
| 24  | -0.999999991354167 | 0.999995822493936 | -0.999999999999985 | -0.999999999069028 | ---               | ---                  |
| 25  | -0.999999991354167 | 0.999995822493936 | -0.999999999999985 | -0.999999999069028 | ---               | ---                  |
| 26  | -0.999999991354167 | 0.999995822493934 | -0.999999999999984 | -0.999999999069135 | 0.995603138633013 | ---                  |
| 27  | -0.999999991354167 | 0.999995822493936 | -0.999999999999985 | -0.999999999069082 | ---               | ---                  |
| 28  | -0.999999991354167 | 0.999995822493934 | -0.999999999999984 | -0.999999999069133 | 0.995559435816198 | -0.220064544193374   |
| 29  | -0.999999991354167 | 0.999995822493934 | -0.999999999999984 | -0.999999999069125 | ---               | ---                  |
| 30  | -0.999999991354167 | 0.999995822493936 | -0.999999999999985 | ---                | ---               | ---                  |
| 31  | -0.999999991354167 | 0.999995822493926 | -0.999999999999985 | -0.999999999069071 | 0.995406654955003 | 0.334186672623386    |
| 32  | -0.999999991354167 | 0.999995822493934 | -0.999999999999984 | -0.999999999069131 | 0.995541571262789 | ---                  |
| 33  | -0.999999991354167 | 0.999995822493934 | -0.999999999999984 | -0.999999999069129 | 0.995541615278607 | ---                  |
| 34  | -0.999999991354167 | 0.999995822493938 | -0.999999999999985 | -0.999999999069071 | 0.995404404279500 | 0.336083907451386    |
| 35  | -0.999999991354167 | 0.999995822493934 | -0.999999999999984 | ---                | ---               | ---                  |
| 36  | -0.999999991354167 | 0.999995822493933 | -0.999999999999688 | -0.999999999069072 | 0.995470745898804 | ---                  |
| 37  | -0.999999991354167 | 0.999995822493936 | -0.999999999999984 | ---                | ---               | ---                  |
| 38  | -0.999999991354167 | 0.999995822493936 | -0.999999999999984 | -0.999999999069066 | ---               | ---                  |
| 39  | -0.999999991354167 | 0.999995822493936 | -0.999999999999984 | -0.999999999068817 | ---               | ---                  |
| 40  | -0.999999991354167 | 0.999995822493974 | -0.999999999999982 | -0.999999999069123 | ---               | ---                  |
| 41  | -0.999999991354167 | 0.999995822493955 | -0.999999999999985 | ---                | ---               | ---                  |
| 42  | -0.999999991354167 | 0.999995891724558 | -0.999999999999984 | -0.999999999069138 | ---               | ---                  |
| 43  | -0.999999991354167 | 0.999995822493935 | -0.999999999999984 | -0.999999999069130 | 0.995639331373117 | -0.0452970326130405  |
| 44  | -0.999999991354167 | 0.999995822493935 | -0.999999999999985 | -0.999999999069124 | 0.995533585815240 | 0.194080803686896    |
| 45  | -0.999999991354167 | 0.999995822493932 | -0.999999999999984 | -0.999999999069102 | ---               | ---                  |
| 46  | -0.999999991354167 | 0.999995822493903 | -0.999999999999978 | -0.999999999069079 | ---               | ---                  |

|    |                   |                  |                    |                    |                   |                     |
|----|-------------------|------------------|--------------------|--------------------|-------------------|---------------------|
| 47 | -0.99999991354167 | 0.99995822493954 | -0.99999999999985  | -0.999999999069149 | 0.995424389417217 | 0.941445836958311   |
| 48 | -0.99999991354167 | 0.99995822493932 | ---                | ---                | ---               | ---                 |
| 49 | -0.99999991354167 | 0.99995822493935 | -0.99999999999984  | -0.999999999069078 | ---               | ---                 |
| 50 | -0.99999991354167 | 0.99995822493935 | ---                | ---                | ---               | ---                 |
| 51 | -0.99999991354167 | 0.99995822493935 | -0.99999999999984  | -0.999999999069115 | 0.995383838035170 | ---                 |
| 52 | -0.99999991354167 | 0.99995822493935 | ---                | ---                | ---               | ---                 |
| 53 | -0.99999991354167 | 0.99995822493937 | -0.99999999999985  | ---                | ---               | ---                 |
| 54 | -0.99999991354167 | 0.99995822493931 | ---                | ---                | ---               | ---                 |
| 55 | -0.99999991354167 | 0.99995822493988 | -0.99999999999985  | -0.999999999069101 | 0.995309607900930 | ---                 |
| 56 | -1,00E+00         | 0.99995822493932 | ---                | ---                | ---               | ---                 |
| 57 | -0.99999991354167 | 0.99995822493923 | -0.99999999999984  | -0.999999999069062 | 0.995475049667694 | ---                 |
| 58 | -0.99999991354167 | 0.99995822493938 | -0.99999999999985  | ---                | ---               | ---                 |
| 59 | -0.99999991354167 | 0.99995822493933 | -0.99999999999984  | -0.999999999069032 | ---               | ---                 |
| 60 | -0.99999991354167 | 0.99995822493939 | ---                | ---                | ---               | ---                 |
| 61 | -0.99999991354167 | 0.99995822493939 | ---                | ---                | ---               | ---                 |
| 62 | -0.99999991354167 | 0.99995822493938 | -0.99999999999984  | -0.999999999069103 | 0.995412711531586 | 0.0340003291871429  |
| 63 | -0.99999991354167 | -1,00E+00        | 1,00E+00           | -0.999999999069100 | 0.995574471619691 | ---                 |
| 64 | -0.99999991354167 | 0.99995822493935 | -0.99999999999984  | -0.999999999069124 | 0.995383758158198 | ---                 |
| 65 | -0.99999991354167 | 0.99995822493935 | -0.999999999984860 | ---                | ---               | ---                 |
| 66 | -0.99999991354167 | 0.99995822493935 | -0.99999999999985  | -0.999999999069100 | 0.995418175361817 | ---                 |
| 67 | -0.99999991354167 | 0.99995822493936 | -0.99999999999984  | ---                | ---               | ---                 |
| 68 | -0.99999991354167 | 0.99995822493935 | -0.99999999999984  | -0.999999999069105 | ---               | ---                 |
| 69 | -0.99999991354167 | 0.99995822493934 | -0.99999999999985  | ---                | ---               | ---                 |
| 70 | -0.99999991354167 | 0.99995822493933 | -0.99999999999985  | -0.999999999069103 | ---               | ---                 |
| 71 | -0.99999991354167 | 0.99995822493937 | ---                | ---                | ---               | ---                 |
| 72 | -0.99999991354167 | 0.99995822493937 | ---                | ---                | ---               | ---                 |
| 73 | -0.99999991354167 | 0.99995822493937 | ---                | ---                | ---               | ---                 |
| 74 | 1,00E+00          | 0.99995822493937 | -0.99999999999984  | ---                | ---               | ---                 |
| 75 | -0.99999991354167 | 0.99995822493937 | ---                | ---                | ---               | ---                 |
| 76 | -0.99999991354167 | 0.99995822493935 | -0.99999999999985  | -0.999999999069089 | 0.999719535119013 | ---                 |
| 77 | -0.99999991354167 | 0.99995822493935 | -0.999999999971816 | -1,00E+00          | -1,00E+00         | ---                 |
| 78 | -0.99999991354167 | 0.99995822493933 | -0.99999999999984  | -0.999999999069001 | 0.995901303741688 | ---                 |
| 79 | -0.99999991354167 | 0.99995822493932 | ---                | ---                | ---               | ---                 |
| 80 | -0.99999991354167 | 0.99995822493933 | -0.99999999999984  | -0.999999999069134 | 0.995560177238202 | -0.0724417456323920 |
| 81 | -0.99999991354167 | 0.99995822493938 | -0.99999999999982  | -0.999999999068885 | 0.996030072506866 | ---                 |
| 82 | -0.99999991354167 | 0.99995822493938 | ---                | ---                | ---               | ---                 |
| 83 | -0.99999991354167 | 0.99995822493938 | ---                | ---                | ---               | ---                 |
| 84 | -0.99999991354167 | 0.99995822493938 | -1                 | ---                | ---               | ---                 |
| 85 | -0.99999991354167 | 0.99995822493932 | ---                | ---                | ---               | ---                 |
| 86 | -0.99999991354167 | 0.99995822493928 | -0.99999999999979  | -0.999999999069128 | ---               | ---                 |
| 87 | -0.99999991354167 | 0.99995822493934 | -0.99999999999985  | -0.999999999069120 | 0.995513377664044 | -0.0784420630628512 |
| 88 | -0.99999991354167 | 0.99995822493893 | -0.99999999999984  | -0.999999999068995 | ---               | ---                 |
| 89 | -0.99999991354167 | 0.99995822493937 | -0.99999999999984  | ---                | ---               | ---                 |
| 90 | -0.99999991354167 | 0.99995822493934 | ---                | ---                | ---               | ---                 |
| 91 | -0.99999991354167 | 0.99995822493933 | -0.99999999999985  | -0.999999999069124 | ---               | ---                 |
| 92 | -0.99999991354167 | 0.99995822493928 | -0.99999999999979  | -0.999999999069128 | ---               | ---                 |
| 93 | -0.99999991354167 | 0.99995822493933 | -0.99999999999984  | ---                | ---               | ---                 |
| 94 | -0.99999991354167 | 0.99995822493934 | -0.99999999999984  | -0.999999999069101 | 0.995481570855691 | 0.136825754191258   |
| 95 | -0.99999991354167 | 0.99995822493936 | -0.99999999999985  | -0.999999999069136 | 0.994579250495322 | 1                   |

Table 7. Estimated model parameters ( $a_i$ ) of 95 equations proposed in this work for  $V_p$ 

| DEC | $a_1$      | $a_2$      | $a_3$      | $a_4$     | $a_5$     | $a_6$        | $a_7$    | $a_8$   | $a_9$ | $a_{10}$ |
|-----|------------|------------|------------|-----------|-----------|--------------|----------|---------|-------|----------|
| 1   | 0,90701    | 6,26229    | 0,3386     | 212,9391  | 208,24451 | -10641,04919 | 3,90E+13 | 0,19898 | ---   | ---      |
| 2   | 0,71452    | 0,16435    | -1,68177   | 1,07328   | -1,9273   | ---          | ---      | ---     | ---   | ---      |
| 3   | 5267,46569 | 1476,77484 | 3,73E-05   | 345,34186 | 11,27481  | ---          | ---      | ---     | ---   | ---      |
| 4   | 1,04852    | 132,15195  | 0,63623    | ---       | ---       | ---          | ---      | ---     | ---   | ---      |
| 5   | 0,55713    | -0,86442   | -3580,8315 | 5,99062   | -0,15286  | 5,54351      | 0,04969  | -1,5505 | ---   | ---      |
| 6   | -6,07587   | 8,64379    | 0,37844    | 0,69251   | -7,17942  | 7,17584      | 1,04471  | ---     | ---   | ---      |
| 7   | 1,27709    | 0,05012    | 0,22682    | -8,23285  | 77,07524  | 22311,3115   | ---      | ---     | ---   | ---      |

|    |            |           |            |             |           |          |          |         |         |     |
|----|------------|-----------|------------|-------------|-----------|----------|----------|---------|---------|-----|
| 8  | 0,11619    | 0,91114   | 2,40078    | 0,46855     | 483,51346 | ---      | ---      | ---     | ---     | --- |
| 9  | 39,57239   | 0,88076   | -0,03104   | 1,25358     | -1,60656  | 4,9799   | 0,50675  | ---     | ---     | --- |
| 10 | -0,0062    | -0,08303  | 16,76157   | 0,69592     | ---       | ---      | ---      | ---     | ---     | --- |
| 11 | -0,0062    | -0,08303  | 16,76157   | 0,69592     | ---       | ---      | ---      | ---     | ---     | --- |
| 12 | 0,23044    | 0,04336   | 0,23044    | 0,04336     | 3,00106   | 0,14032  | 0,09299  | 0,14032 | 0,10567 | --- |
| 13 | 2,06281    | 0,05061   | 2,05963    | 3,49E-04    | -2,66814  | 0,21132  | ---      | ---     | ---     | --- |
| 14 | 0,28936    | 1,05E-04  | -0,39805   | -0,13858    | ---       | ---      | ---      | ---     | ---     | --- |
| 15 | 0,28936    | 1,05E-04  | -0,39805   | -0,13858    | ---       | ---      | ---      | ---     | ---     | --- |
| 16 | 0,28936    | 1,05E-04  | -0,39805   | -0,13858    | ---       | ---      | ---      | ---     | ---     | --- |
| 17 | 0,28936    | 1,05E-04  | -0,39805   | -0,13858    | ---       | ---      | ---      | ---     | ---     | --- |
| 18 | 1,80099    | -0,00679  | 0,80859    | 2,09E-04    | 0,00342   | -1,29555 | ---      | ---     | ---     | --- |
| 19 | 306,27726  | 1,30149   | 306,71095  | 1,30774     | ---       | ---      | ---      | ---     | ---     | --- |
| 20 | 0,98581    | -6,36563  | 31,27241   | -0,00221    | -0,00867  | ---      | ---      | ---     | ---     | --- |
| 21 | 0,8348     | -3,38062  | 0,09813    | 0,77125     | -3,46329  | ---      | ---      | ---     | ---     | --- |
| 22 | 306,27726  | 1,30149   | 306,71095  | 1,30774     | ---       | ---      | ---      | ---     | ---     | --- |
| 23 | 0,8348     | -3,38062  | 0,09813    | 0,77125     | -3,46329  | ---      | ---      | ---     | ---     | --- |
| 24 | 46,06941   | 0,53732   | 3,85314    | 0,15798     | ---       | ---      | ---      | ---     | ---     | --- |
| 25 | 46,06941   | 0,53732   | 3,85314    | 0,15798     | ---       | ---      | ---      | ---     | ---     | --- |
| 26 | 0,81112    | 1,02832   | -0,6699    | 1,68674     | -0,8533   | ---      | ---      | ---     | ---     | --- |
| 27 | 13,5085    | 0,6441    | -1,36E-06  | 1069744,045 | ---       | ---      | ---      | ---     | ---     | --- |
| 28 | 3,75922    | 1,8176    | -0,57275   | 0,98043     | 11,05933  | 4,91584  | -5,27305 | ---     | ---     | --- |
| 29 | 3,54738    | 13,21061  | 0,8445     | 16,40852    | ---       | ---      | ---      | ---     | ---     | --- |
| 30 | 3,4669     | 0,30732   | 1,26815    | ---         | ---       | ---      | ---      | ---     | ---     | --- |
| 31 | 1625,34597 | 246,06362 | 1,03013    | 0,54689     | 1,03013   | 0,5469   | ---      | ---     | ---     | --- |
| 32 | 1,43473    | 12,07708  | 0,73814    | 3,0664      | 1,44549   | ---      | ---      | ---     | ---     | --- |
| 33 | 17,68894   | 14,29437  | 0,90169    | 14,84411    | 0,9288    | ---      | ---      | ---     | ---     | --- |
| 34 | 10,71585   | 1,23941   | 14,30378   | 0,90239     | 14,81638  | 0,9277   | ---      | ---     | ---     | --- |
| 35 | 0,98458    | 38,14367  | -172,48909 | ---         | ---       | ---      | ---      | ---     | ---     | --- |
| 36 | 0,16388    | 0,16454   | -0,28265   | 0,68794     | 15,44312  | ---      | ---      | ---     | ---     | --- |
| 37 | -0,00743   | 0,66413   | 14,56378   | ---         | ---       | ---      | ---      | ---     | ---     | --- |
| 38 | 0,40964    | -0,00596  | 0,41473    | -0,35299    | ---       | ---      | ---      | ---     | ---     | --- |
| 39 | 7,07128    | 0,64405   | 6,43519    | 0,64409     | ---       | ---      | ---      | ---     | ---     | --- |
| 40 | 0,26898    | 1,64601   | 7,90E-04   | 0,40169     | ---       | ---      | ---      | ---     | ---     | --- |
| 41 | 10,25755   | 0,37496   | 4,0485     | ---         | ---       | ---      | ---      | ---     | ---     | --- |
| 42 | -1,38846   | 4,81179   | 0,06805    | -0,21381    | ---       | ---      | ---      | ---     | ---     | --- |
| 43 | -3,75035   | 4,13468   | 1,0903     | 0,50003     | -1,42081  | 0,49968  | -1,46794 | ---     | ---     | --- |
| 44 | 15,94403   | 0,48938   | -0,58326   | 0,20835     | 27,55809  | 0,62869  | ---      | ---     | ---     | --- |
| 45 | 1,46395    | 0,42835   | 1,27103    | -0,75588    | ---       | ---      | ---      | ---     | ---     | --- |
| 46 | -1,46891   | 0,62782   | 1,86175    | 0,24429     | ---       | ---      | ---      | ---     | ---     | --- |
| 47 | 0,68792    | -53,70252 | 0,68092    | 0,72522     | -10,4247  | 0,51072  | ---      | ---     | ---     | --- |
| 48 | 3,83515    | 3,17467   | ---        | ---         | ---       | ---      | ---      | ---     | ---     | --- |
| 49 | 0,51487    | 0,05514   | 0,51487    | 0,05514     | ---       | ---      | ---      | ---     | ---     | --- |
| 50 | 1,02974    | 0,05514   | ---        | ---         | ---       | ---      | ---      | ---     | ---     | --- |
| 51 | 1,17111    | 1,31983   | 0,00354    | 2,1728      | 1,32528   | ---      | ---      | ---     | ---     | --- |
| 52 | 1,02974    | 0,05514   | ---        | ---         | ---       | ---      | ---      | ---     | ---     | --- |
| 53 | 14,07946   | -172,5444 | 0,01128    | ---         | ---       | ---      | ---      | ---     | ---     | --- |
| 54 | 126,40175  | 0,99748   | ---        | ---         | ---       | ---      | ---      | ---     | ---     | --- |
| 55 | 1,13071    | -1,43429  | 51,84724   | 1,11368     | 5,51363   | ---      | ---      | ---     | ---     | --- |
| 56 | 87,16636   | 1,02605   | ---        | ---         | ---       | ---      | ---      | ---     | ---     | --- |
| 57 | 1,44E+11   | -24,23326 | 1,59445    | 0,6441      | 13,50851  | ---      | ---      | ---     | ---     | --- |
| 58 | 73,11221   | 0,8683    | -68,4413   | ---         | ---       | ---      | ---      | ---     | ---     | --- |
| 59 | 5,01114    | -10,47879 | 11,4297    | 0,84015     | ---       | ---      | ---      | ---     | ---     | --- |
| 60 | 23,41877   | 0,95439   | ---        | ---         | ---       | ---      | ---      | ---     | ---     | --- |
| 61 | 23,41877   | 0,95439   | ---        | ---         | ---       | ---      | ---      | ---     | ---     | --- |
| 62 | 0,49638    | 1,44356   | 1,08444    | 24,74384    | 3,07021   | 1,08445  | ---      | ---     | ---     | --- |
| 63 | 1,18485    | -1,59E+14 | 3,09E+15   | 1,21501     | 0,04687   | ---      | ---      | ---     | ---     | --- |
| 64 | 0,93432    | 35,34633  | 0,87269    | 2,17341     | 2,1633    | ---      | ---      | ---     | ---     | --- |
| 65 | 1,02983    | 0,0552    | 1651,03186 | ---         | ---       | ---      | ---      | ---     | ---     | --- |
| 66 | 9,41084    | 3,5349    | -16,74588  | 0,62713     | -2,54644  | ---      | ---      | ---     | ---     | --- |

|    |             |             |           |             |           |          |     |     |     |
|----|-------------|-------------|-----------|-------------|-----------|----------|-----|-----|-----|
| 67 | 0,98512     | 13,95874    | 0,65733   | ---         | ---       | ---      | --- | --- | --- |
| 68 | 0,9761      | 22,58514    | 0,65729   | 0,61911     | ---       | ---      | --- | --- | --- |
| 69 | 0,85659     | 37,0282     | 3,954     | ---         | ---       | ---      | --- | --- | --- |
| 70 | 90626,27337 | 4,48656     | -3,31275  | 28941,89962 | ---       | ---      | --- | --- | --- |
| 71 | 13,50851    | 0,6441      | ---       | ---         | ---       | ---      | --- | --- | --- |
| 72 | 12,57032    | 0,64407     | ---       | ---         | ---       | ---      | --- | --- | --- |
| 73 | 1,21597     | 0,64459     | ---       | ---         | ---       | ---      | --- | --- | --- |
| 74 | 228,9838    | 0,72924     | 21,28457  | ---         | ---       | ---      | --- | --- | --- |
| 75 | 0,10447     | 0,64435     | ---       | ---         | ---       | ---      | --- | --- | --- |
| 76 | 2537,93595  | 0,88588     | 0,00842   | 0,48992     | 2,8816    | ---      | --- | --- | --- |
| 77 | 0,45266     | 0,13161     | 0,65288   | -0,00373    | 0,65669   | ---      | --- | --- | --- |
| 78 | 0,1247      | -18,54545   | 7,42E+16  | 2,63859     | -18,15078 | ---      | --- | --- | --- |
| 79 | 119,19887   | 117,72534   | ---       | ---         | ---       | ---      | --- | --- | --- |
| 80 | -24,90594   | 39,48381    | 5,73496   | 20,57044    | 5,73496   | 20,57044 | --- | --- | --- |
| 81 | 1,57405     | 13,40336    | 0,60671   | 20,46533    | 3,13156   | ---      | --- | --- | --- |
| 82 | 1,13E-32    | -0,05586    | ---       | ---         | ---       | ---      | --- | --- | --- |
| 83 | 504,20715   | 1,41972     | ---       | ---         | ---       | ---      | --- | --- | --- |
| 84 | 118,93954   | 1,41876     | 0,2366    | ---         | ---       | ---      | --- | --- | --- |
| 85 | -43,48794   | 47,98653    | ---       | ---         | ---       | ---      | --- | --- | --- |
| 86 | 0,95638     | -1,45E-09   | 15,33985  | 0,69237     | ---       | ---      | --- | --- | --- |
| 87 | 1,62263     | 0,33552     | 129,99757 | 2,48945     | -0,02398  | 0,19619  | --- | --- | --- |
| 88 | 13,49305    | 7,87853     | 0,6147    | 20,39681    | ---       | ---      | --- | --- | --- |
| 89 | 0,07998     | 6,2917      | 58,45335  | ---         | ---       | ---      | --- | --- | --- |
| 90 | 1,54576     | 74,97195    | ---       | ---         | ---       | ---      | --- | --- | --- |
| 91 | 0,49627     | 24,28382    | 4,04404   | 7,24547     | ---       | ---      | --- | --- | --- |
| 92 | 0,95638     | -1,45E-09   | 15,33985  | 0,69237     | ---       | ---      | --- | --- | --- |
| 93 | 14,56378    | 0,66413     | 0,00743   | ---         | ---       | ---      | --- | --- | --- |
| 94 | 0,02881     | -0,46266    | 0,17099   | -0,19581    | 0,6282    | 12,49095 | --- | --- | --- |
| 95 | 0,99465     | 26711,35807 | 8,20292   | 3,33173     | 104,38148 | 0,18811  | --- | --- | --- |

**Table 8.** Normalized correlation constants ( $a_n$ ) of  $V_p$ .

| DEC | $a_1$              | $a_2$             | $a_3$              | $a_4$              | $a_5$             | $a_6$                |
|-----|--------------------|-------------------|--------------------|--------------------|-------------------|----------------------|
| 1   | -0.999999991354167 | 0.999995822493937 | -0.999999999999982 | 1                  | 1                 | -0.00525082884619910 |
| 2   | -0.999999991354167 | 1                 | -0.999999999999974 | -0.999999999069146 | 0.995382794469027 | -0.0101327917421054  |
| 3   | -0.999999991354167 | 0.999995822493933 | -0.999999999999984 | -0.999999999069124 | 0.995390627328406 | ---                  |
| 4   | -0.999999991354167 | 0.999995822493933 | -0.999999999999984 | -0.999999999069124 | 0.995383757926381 | ---                  |
| 5   | -0.999999991354167 | 0.999995822493935 | -0.999999999999984 | ---                | ---               | ---                  |
| 6   | -0.999999991354167 | 0.999995822493962 | -0.999999999999984 | -0.999999999069113 | 0.995318404217662 | 0.0949440381857085   |
| 7   | -0.999999991354167 | 0.999995822493935 | -0.999999999999985 | -0.999999999069098 | 0.995460242746455 | 0.0713160431705424   |
| 8   | -0.999999991354167 | 0.999995822493935 | -0.999999999999985 | -0.999999999069138 | 0.995494394130724 | -0.0101327917421054  |
| 9   | -0.999999991354167 | 0.999995822493936 | -0.999999999999985 | -0.999999999069148 | 0.995372644421353 | ---                  |
| 10  | -0.999999991354167 | 0.999995822493936 | -0.999999999999985 | -0.999999999069063 | 0.995383757926381 | -0.0101327917421054  |
| 11  | -0.999999991354167 | 0.999995822493936 | -0.999999999999985 | -0.999999999069063 | ---               | ---                  |
| 12  | -0.999999991354167 | 0.999995822493936 | -0.999999999999985 | -0.999999999069073 | ---               | ---                  |
| 13  | -0.999999991354167 | 0.999995822493932 | -0.999999999999985 | -0.999999999069105 | 0.994925949401391 | 0.0642855463330903   |
| 14  | -0.999999991354167 | 0.999995822493934 | -0.999999999999984 | -0.999999999069113 | 0.995383757926381 | -0.0101327917421054  |
| 15  | -0.999999991354167 | 0.999995822493934 | -0.999999999999984 | -0.999999999069113 | ---               | ---                  |
| 16  | -0.999999991354167 | 0.999995822493934 | -0.999999999999984 | -0.999999999069113 | ---               | ---                  |
| 17  | -0.999999991354167 | 0.999995822493934 | -0.999999999999984 | -0.999999999069113 | ---               | ---                  |
| 18  | -0.999999991354167 | 0.999995822493931 | -0.999999999999985 | -0.999999999069034 | ---               | ---                  |
| 19  | -0.999999991354167 | 0.999995822493930 | -0.999999999999983 | -0.999999999069232 | 0.995383757926381 | -0.0101327917421054  |
| 20  | -0.999999991354167 | 0.999995822493935 | -0.999999999999984 | -0.999999999069239 | ---               | ---                  |
| 21  | -0.999999991354167 | 0.999995822493930 | -0.999999999999985 | -0.999999999069104 | 0.994949398094935 | ---                  |
| 22  | -0.999999991354167 | 0.999995822493930 | -0.999999999999983 | -0.999999999069232 | 0.995383757926381 | ---                  |



|    |                    |                   |                    |                    |                   |                     |
|----|--------------------|-------------------|--------------------|--------------------|-------------------|---------------------|
| 23 | -0.999999991354167 | 0.999995822493930 | -0.99999999999985  | -0.999999999069104 | ---               | ---                 |
| 24 | -0.999999991354167 | 0.999995822493936 | -0.99999999999985  | -0.999999999069028 | 0.995383757926381 | ---                 |
| 25 | -0.999999991354167 | 0.999995822493936 | -0.99999999999985  | -0.999999999069028 | ---               | ---                 |
| 26 | -0.999999991354167 | 0.999995822493934 | -0.99999999999984  | -0.999999999069135 | ---               | ---                 |
| 27 | -0.999999991354167 | 0.999995822493936 | -0.99999999999985  | -0.999999999069082 | 0.995383757926381 | ---                 |
| 28 | -0.999999991354167 | 0.999995822493934 | -0.99999999999984  | -0.999999999069133 | ---               | ---                 |
| 29 | -0.999999991354167 | 0.999995822493934 | -0.99999999999984  | -0.999999999069125 | 0.995383757926381 | -0.0101327917421054 |
| 30 | -0.999999991354167 | 0.999995822493936 | -0.99999999999985  | -0.999999999069124 | ---               | ---                 |
| 31 | -0.999999991354167 | 0.999995822493926 | -0.99999999999985  | ---                | ---               | ---                 |
| 32 | -0.999999991354167 | 0.999995822493934 | -0.99999999999984  | -0.999999999069131 | 0.995541571262789 | -0.0101327917421054 |
| 33 | -0.999999991354167 | 0.999995822493934 | -0.99999999999984  | -0.999999999069129 | 0.995541615278607 | ---                 |
| 34 | -0.999999991354167 | 0.999995822493938 | -0.99999999999985  | -0.999999999069071 | 0.995404404279500 | ---                 |
| 35 | -0.999999991354167 | 0.999995822493934 | -0.99999999999984  | -0.999999999069124 | 0.995383757926381 | -0.0101327917421054 |
| 36 | -0.999999991354167 | 0.999995822493933 | -0.999999999999688 | ---                | ---               | ---                 |
| 37 | -0.999999991354167 | 0.999995822493936 | -0.99999999999984  | -0.999999999069124 | 0.995383757926381 | ---                 |
| 38 | -0.999999991354167 | 0.999995822493936 | -0.99999999999984  | ----               | ---               | ---                 |
| 39 | -0.999999991354167 | 0.999995822493936 | -0.99999999999984  | -0.999999999068817 | ---               | ---                 |
| 40 | -0.999999991354167 | 0.999995822493974 | -0.99999999999982  | -0.999999999069123 | ---               | ---                 |
| 41 | -0.999999991354167 | 0.999995822493955 | -0.99999999999985  | -0.999999999069124 | ---               | ---                 |
| 42 | -0.999999991354167 | 0.999995891724558 | -0.99999999999984  | ---                | ---               | ---                 |
| 43 | -0.999999991354167 | 0.999995822493935 | -0.99999999999984  | -0.999999999069130 | ---               | ---                 |
| 44 | -0.999999991354167 | 0.999995822493935 | -0.99999999999985  | -0.999999999069124 | 0.995533585815240 | 0.194080803686896   |
| 45 | -0.999999991354167 | 0.999995822493932 | -0.99999999999984  | -0.999999999069102 | 0.995383757926381 | -0.0101327917421054 |
| 46 | -0.999999991354167 | 0.999995822493903 | -0.99999999999978  | -0.999999999069079 | ---               | ---                 |
| 47 | -0.999999991354167 | 0.999995822493954 | -0.99999999999985  | -0.999999999069149 | ---               | ---                 |
| 48 | -0.999999991354167 | 0.999995822493932 | -0.99999999999985  | -0.999999999069124 | 0.995383757926381 | -0.0101327917421054 |
| 49 | -0.999999991354167 | 0.999995822493935 | ---                | ---                | ---               | ---                 |
| 50 | -0.999999991354167 | 0.999995822493935 | -0.99999999999985  | -0.999999999069124 | ---               | ---                 |
| 51 | -0.999999991354167 | 0.999995822493935 | ---                | ---                | ---               | ---                 |
| 52 | -0.999999991354167 | 0.999995822493935 | -0.99999999999985  | -0.999999999069124 | 0.995383757926381 | ---                 |
| 53 | -0.999999991354167 | 0.999995822493937 | ---                | ---                | ---               | ---                 |
| 54 | -0.999999991354167 | 0.999995822493931 | -0.99999999999985  | ---                | ---               | ---                 |
| 55 | -0.999999991354167 | 0.999995822493988 | ---                | ---                | ---               | ---                 |
| 56 | -1                 | 0.999995822493932 | -0.99999999999985  | -0.999999999069124 | 0.995383757926381 | ---                 |
| 57 | -0.999999991354167 | 0.999995822493923 | ---                | ---                | ---               | ---                 |
| 58 | -0.999999991354167 | 0.999995822493938 | -0.99999999999985  | -0.999999999069124 | 0.995383757926381 | ---                 |
| 59 | -0.999999991354167 | 0.999995822493933 | -0.99999999999984  | ---                | ---               | ---                 |
| 60 | -0.999999991354167 | 0.999995822493939 | -0.99999999999985  | -0.999999999069124 | ---               | ---                 |
| 61 | -0.999999991354167 | 0.999995822493939 | ---                | ---                | ---               | ---                 |
| 62 | -0.999999991354167 | 0.999995822493938 | ---                | ---                | ---               | ---                 |
| 63 | -0.999999991354167 | -1                | 1                  | -0.999999999069100 | 0.995574471619691 | -0.0101327917421054 |
| 64 | -0.999999991354167 | 0.999995822493935 | -0.99999999999984  | -0.999999999069124 | 0.995383758158198 | ---                 |
| 65 | -0.999999991354167 | 0.999995822493935 | -0.99999999984860  | -0.999999999069124 | 0.995383757926381 | ---                 |
| 66 | -0.999999991354167 | 0.999995822493935 | -0.99999999999985  | ---                | ---               | ---                 |
| 67 | -0.999999991354167 | 0.999995822493936 | -0.99999999999984  | -0.999999999069124 | 0.995383757926381 | ---                 |
| 68 | -0.999999991354167 | 0.999995822493935 | -0.99999999999984  | ---                | ---               | ---                 |
| 69 | -0.999999991354167 | 0.999995822493934 | -0.99999999999985  | -0.999999999069124 | ---               | ---                 |

|    |                    |                   |                   |                    |                   |                     |
|----|--------------------|-------------------|-------------------|--------------------|-------------------|---------------------|
| 70 | -0.999999991354167 | 0.999995822493933 | -0.99999999999985 | ---                | ---               | ---                 |
| 71 | -0.999999991354167 | 0.999995822493937 | -0.99999999999985 | -0.999999999069124 | ---               | ---                 |
| 72 | -0.999999991354167 | 0.999995822493937 | ---               | ---                | ---               | ---                 |
| 73 | -0.999999991354167 | 0.999995822493937 | ---               | ---                | ---               | ---                 |
| 74 | 1                  | 0.999995822493937 | ---               | ---                | ---               | ---                 |
| 75 | -0.999999991354167 | 0.999995822493937 | -0.99999999999985 | ---                | ---               | ---                 |
| 76 | -0.999999991354167 | 0.999995822493935 | ---               | ---                | ---               | ---                 |
| 77 | -0.999999991354167 | 0.999995822493935 | -0.99999999971816 | -1                 | -1                | ---                 |
| 78 | -0.999999991354167 | 0.999995822493933 | -0.99999999999984 | -0.999999999069001 | 0.995901303741688 | ---                 |
| 79 | -0.999999991354167 | 0.999995822493932 | -0.99999999999985 | -0.999999999069124 | 0.995383757926381 | ---                 |
| 80 | -0.999999991354167 | 0.999995822493933 | ---               | ---                | ---               | ---                 |
| 81 | -0.999999991354167 | 0.999995822493938 | -0.99999999999982 | -0.999999999068885 | 0.996030072506866 | -0.0101327917421054 |
| 82 | -0.999999991354167 | 0.999995822493938 | -0.99999999999985 | -0.999999999069124 | 0.995383757926381 | ---                 |
| 83 | -0.999999991354167 | 0.999995822493938 | ---               | ---                | ---               | ---                 |
| 84 | -0.999999991354167 | 0.999995822493938 | ---               | ---                | ---               | ---                 |
| 85 | -0.999999991354167 | 0.999995822493932 | -0.99999999999985 | ---                | ---               | ---                 |
| 86 | -0.999999991354167 | 0.999995822493928 | ---               | ---                | ---               | ---                 |
| 87 | -0.999999991354167 | 0.999995822493934 | -0.99999999999985 | -0.999999999069120 | ---               | ---                 |
| 88 | -0.999999991354167 | 0.999995822493893 | -0.99999999999984 | -0.999999999068995 | 0.995383757926381 | -0.0101327917421054 |
| 89 | -0.999999991354167 | 0.999995822493937 | -0.99999999999984 | -0.999999999069124 | ---               | ---                 |
| 90 | -0.999999991354167 | 0.999995822493934 | -0.99999999999985 | ---                | ---               | ---                 |
| 91 | -0.999999991354167 | 0.999995822493933 | ---               | ---                | ---               | ---                 |
| 92 | -0.999999991354167 | 0.999995822493928 | -0.99999999999979 | -0.999999999069128 | ---               | ---                 |
| 93 | -0.999999991354167 | 0.999995822493933 | -0.99999999999984 | -0.999999999069124 | ---               | ---                 |
| 94 | -0.999999991354167 | 0.999995822493934 | -0.99999999999984 | ---                | ---               | ---                 |
| 95 | -0.999999991354167 | 0.999995822493936 | -0.99999999999985 | -0.999999999069136 | 0.994579250495322 | 1                   |

**Table 9.** Estimated model parameters ( $a_i$ ) of 95 equations proposed in this work for  $V_R$ 

| DEC | $a_1$    | $a_2$    | $a_3$       | $a_4$     | $a_5$    | $a_6$      | $a_7$      | $a_8$     | $a_9$  | $a_{10}$ |
|-----|----------|----------|-------------|-----------|----------|------------|------------|-----------|--------|----------|
| 1   | 5,46724  | 3,23425  | 0,14134     | -0,00251  | 81,5262  | -231,05565 | 14569,3707 | -641,6868 | ---    | ---      |
| 2   | 0,7047   | 0,1595   | -1,71718    | 1,08259   | -1,94149 | ---        | ---        | ---       | ---    | ---      |
| 3   | 30,59179 | 653,4999 | 0,01046     | 151,25586 | 5,23029  | ---        | ---        | ---       | ---    | ---      |
| 4   | 0,82145  | 109,8694 | 0,58772     | ---       | ---      | ---        | ---        | ---       | ---    | ---      |
| 5   | 0,62237  | -0,81831 | -2167,81924 | 5,6623    | -0,15541 | 5,28312    | 0,06467    | -1,46454  | ---    | ---      |
| 6   | -4,99062 | 7,18245  | 0,37645     | 0,72638   | -7,91844 | 7,9134     | 1,04618    | ---       | ---    | ---      |
| 7   | 2,35734  | 0,12819  | 0,84871     | -15,39824 | 124,1633 | 1,52844    | ---        | ---       | ---    | ---      |
| 8   | 0,11176  | 0,82307  | 1,90522     | 0,48868   | 317,8094 | ---        | ---        | ---       | ---    | ---      |
| 9   | 31,13    | 0,80671  | -0,03741    | 1,49907   | -1,54291 | 5,38275    | 0,51636    | ---       | ---    | ---      |
| 10  | -0,00566 | -0,11398 | 13,44069    | 0,64077   | ---      | ---        | ---        | ---       | ---    | ---      |
| 11  | -0,00566 | -0,11398 | 13,44069    | 0,64077   | ---      | ---        | ---        | ---       | ---    | ---      |
| 12  | 0,43138  | 0,05727  | 0,43138     | 0,05727   | 1,46907  | 0,06266    | 0,06577    | 0,06266   | 0,0658 | ---      |
| 13  | 5,25617  | 1,24579  | 3,39823     | -0,14114  | -0,46697 | 0,03503    | ---        | ---       | ---    | ---      |
| 14  | 0,28548  | 8,82E-05 | -0,41984    | -0,13754  | ---      | ---        | ---        | ---       | ---    | ---      |
| 15  | 0,28548  | 8,82E-05 | -0,41984    | -0,13754  | ---      | ---        | ---        | ---       | ---    | ---      |
| 16  | 0,28548  | 8,82E-05 | -0,41984    | -0,13754  | ---      | ---        | ---        | ---       | ---    | ---      |
| 17  | 0,28548  | 8,82E-05 | -0,41984    | -0,13754  | ---      | ---        | ---        | ---       | ---    | ---      |
| 18  | 1,78718  | -0,01211 | 0,82303     | -5,72E-04 | 0,00737  | -1,11852   | ---        | ---       | ---    | ---      |
| 19  | 140,0477 | 1,11355  | 139,73204   | 1,12568   | ---      | ---        | ---        | ---       | ---    | ---      |

|    |            |           |            |          |          |         |          |     |     |     |
|----|------------|-----------|------------|----------|----------|---------|----------|-----|-----|-----|
| 20 | 1,04526    | -8,28701  | 53,46308   | -0,00385 | -0,00697 | ---     | ---      | --- | --- | --- |
| 21 | 0,839      | -3,31382  | 0,1009     | 0,7726   | -3,40032 | ---     | ---      | --- | --- | --- |
| 22 | 140,0477   | 1,11355   | 139,73204  | 1,12568  | ---      | ---     | ---      | --- | --- | --- |
| 23 | 0,839      | -3,31382  | 0,1009     | 0,7726   | -3,40032 | ---     | ---      | --- | --- | --- |
| 24 | 42,38533   | 0,53637   | 3,7685     | 0,16069  | ---      | ---     | ---      | --- | --- | --- |
| 25 | 42,38533   | 0,53637   | 3,7685     | 0,16069  | ---      | ---     | ---      | --- | --- | --- |
| 26 | 0,80321    | 1,05509   | -0,69389   | 1,67272  | -0,84698 | ---     | ---      | --- | --- | --- |
| 27 | 13,4411    | 0,64078   | 0,00566    | -0,11389 | ---      | ---     | ---      | --- | --- | --- |
| 28 | 13,09366   | 2,38657   | -0,1929    | 66,69841 | 2,26205  | 5,58112 | 0,48233  | --- | --- | --- |
| 29 | 2,3488     | 11,41734  | 0,76971    | 15,51808 | ---      | ---     | ---      | --- | --- | --- |
| 30 | 3,4411     | 0,31051   | 1,25952    | ---      | ---      | ---     | ---      | --- | --- | --- |
| 31 | 1538,23853 | 233,5121  | 1,02985    | 0,54834  | 1,02984  | 0,54834 | ---      | --- | --- | --- |
| 32 | 1,326      | 11,17761  | 0,69932    | 3,62678  | 1,49639  | ---     | ---      | --- | --- | --- |
| 33 | 15,27358   | 12,49652  | 0,8475     | 12,94452 | 0,87458  | ---     | ---      | --- | --- | --- |
| 34 | 10,00211   | 1,20503   | 12,49918   | 0,84795  | 12,92435 | 0,87369 | ---      | --- | --- | --- |
| 35 | 0,98275    | 1416822   | -91,3627   | ---      | ---      | ---     | ---      | --- | --- | --- |
| 36 | 0,02948    | 0,02948   | -7,74282   | 0,62012  | 12,14833 | ---     | ---      | --- | --- | --- |
| 37 | -0,00672   | 0,61951   | 12,13205   | ---      | ---      | ---     | ---      | --- | --- | --- |
| 38 | -22,92583  | 0,29351   | -23,20661  | -0,46042 | ---      | ---     | ---      | --- | --- | --- |
| 39 | 5,51294    | 0,5985    | 5,71675    | 0,59854  | ---      | ---     | ---      | --- | --- | --- |
| 40 | 0,13208    | 1,57271   | 5,49E-04   | 0,39421  | ---      | ---     | ---      | --- | --- | --- |
| 41 | 9,43766    | 0,36225   | 3,77885    | ---      | ---      | ---     | ---      | --- | --- | --- |
| 42 | -1,37005   | 4,80184   | 0,07102    | -0,21912 | ---      | ---     | ---      | --- | --- | --- |
| 43 | -3,77778   | 4,17944   | 1,09538    | 0,47941  | -1,48989 | 0,47994 | -1,51995 | --- | --- | --- |
| 44 | 15,52642   | 0,48968   | -0,56205   | 0,21501  | 26,22675 | 0,62947 | ---      | --- | --- | --- |
| 45 | 1,46397    | 0,41909   | 1,27281    | -0,75241 | ---      | ---     | ---      | --- | --- | --- |
| 46 | -1,45852   | 0,61417   | 1,86424    | 0,24775  | ---      | ---     | ---      | --- | --- | --- |
| 47 | 0,68061    | 48,67717  | 0,67952    | 0,7341   | 8,39397  | 0,49495 | ---      | --- | --- | --- |
| 48 | 3,82919    | 3,16677   | ---        | ---      | ---      | ---     | ---      | --- | --- | --- |
| 49 | 0,51544    | 0,05772   | 0,51543    | 0,05772  | ---      | ---     | ---      | --- | --- | --- |
| 50 | 1,03087    | 0,05772   | ---        | ---      | ---      | ---     | ---      | --- | --- | --- |
| 51 | 1,18032    | 1,12768   | 0,00793    | 2,17793  | 1,13892  | ---     | ---      | --- | --- | --- |
| 52 | 1,03087    | 0,05772   | ---        | ---      | ---      | ---     | ---      | --- | --- | --- |
| 53 | 3606,82293 | -158,336  | 0,00976    | ---      | ---      | ---     | ---      | --- | --- | --- |
| 54 | 119,19161  | 0,99732   | ---        | ---      | ---      | ---     | ---      | --- | --- | --- |
| 55 | 1,14272    | -1,60886  | 53,30105   | 1,12186  | 6,60203  | ---     | ---      | --- | --- | --- |
| 56 | 84,75332   | 1,02513   | ---        | ---      | ---      | ---     | ---      | --- | --- | --- |
| 57 | 1,43E+11   | -24,18817 | 1,60002    | 0,59854  | 11,23069 | ---     | ---      | --- | --- | --- |
| 58 | 36,61242   | 0,78343   | -31,62791  | ---      | ---      | ---     | ---      | --- | --- | --- |
| 59 | 3,4198     | -9,01931  | 10,48399   | 0,78025  | ---      | ---     | ---      | --- | --- | --- |
| 60 | 16,3626    | 0,86299   | ---        | ---      | ---      | ---     | ---      | --- | --- | --- |
| 61 | 16,3626    | 0,86299   | ---        | ---      | ---      | ---     | ---      | --- | --- | --- |
| 62 | 0,49644    | 1,43959   | 1,1078     | 20,84757 | 3,95477  | 1,1078  | ---      | --- | --- | --- |
| 63 | 0,72842    | -6,7E+13  | 1,47E+15   | 0,75769  | 0,07743  | ---     | ---      | --- | --- | --- |
| 64 | 981,66374  | 11,342    | 0,59957    | 3,3678   | 3,3678   | ---     | ---      | --- | --- | --- |
| 65 | 1,03096    | 0,05778   | 1666,21239 | ---      | ---      | ---     | ---      | --- | --- | --- |
| 66 | 47812,8389 | 6,58549   | -0,69044   | 0,02952  | -64,9304 | ---     | ---      | --- | --- | --- |

|    |            |           |           |             |          |         |     |     |     |     |
|----|------------|-----------|-----------|-------------|----------|---------|-----|-----|-----|-----|
| 67 | 1,01697    | 10,97746  | 0,58764   | ---         | ---      | ---     | --- | --- | --- | --- |
| 68 | 1,02959    | 19,14503  | 0,58764   | 0,57709     | ---      | ---     | --- | --- | --- | --- |
| 69 | 0,83798    | 35,6977   | 4,19571   | ---         | ---      | ---     | --- | --- | --- | --- |
| 70 | 381985,405 | 6,32299   | -2,76517  | 7234379,943 | ---      | ---     | --- | --- | --- | --- |
| 71 | 11,23069   | 0,59854   | ---       | ---         | ---      | ---     | --- | --- | --- | --- |
| 72 | 11,34467   | 0,59852   | ---       | ---         | ---      | ---     | --- | --- | --- | --- |
| 73 | 1,16673    | 0,59895   | ---       | ---         | ---      | ---     | --- | --- | --- | --- |
| 74 | -2,09E+12  | -135,7754 | 8,77291   | ---         | ---      | ---     | --- | --- | --- | --- |
| 75 | 0,13993    | 0,59865   | ---       | ---         | ---      | ---     | --- | --- | --- | --- |
| 76 | 1186,6152  | 0,80952   | 0,00961   | 0,43432     | 3,37303  | ---     | --- | --- | --- | --- |
| 77 | 0,47278    | 0,14951   | 0,7639    | -0,00231    | 0,60929  | ---     | --- | --- | --- | --- |
| 78 | 0,15626    | -30,53205 | 3,86E+27  | 3,12853     | -30,1431 | ---     | --- | --- | --- | --- |
| 79 | 112,49272  | 111,04957 | ---       | ---         | ---      | ---     | --- | --- | --- | --- |
| 80 | 5,01813    | -0,1044   | 14,99176  | 1,30972     | -1,54501 | 1,92013 | --- | --- | --- | --- |
| 81 | 1,51376    | 13,07375  | 0,57427   | 20,60312    | 3,09849  | ---     | --- | --- | --- | --- |
| 82 | 1,17E-32   | -0,05505  | ---       | ---         | ---      | ---     | --- | --- | --- | --- |
| 83 | 380,45305  | 1,3526    | ---       | ---         | ---      | ---     | --- | --- | --- | --- |
| 84 | 34,63708   | 1,35259   | 0,09104   | ---         | ---      | ---     | --- | --- | --- | --- |
| 85 | -41,33985  | 45,87023  | ---       | ---         | ---      | ---     | --- | --- | --- | --- |
| 86 | 5,89E+08   | -3,83413  | 26,2177   | -0,08372    | ---      | ---     | --- | --- | --- | --- |
| 87 | 1,65567    | 0,34001   | 142,80576 | 2,5704      | -0,02235 | 0,19099 | --- | --- | --- | --- |
| 88 | 13,19441   | 6,67883   | 0,56887   | 19,61145    | ---      | ---     | --- | --- | --- | --- |
| 89 | -11943,269 | 49,03662  | 49,03637  | ---         | ---      | ---     | --- | --- | --- | --- |
| 90 | 1,59223    | 75,13448  | ---       | ---         | ---      | ---     | --- | --- | --- | --- |
| 91 | 0,49625    | 28,17097  | 3,98293   | 6,53106     | ---      | ---     | --- | --- | --- | --- |
| 92 | 5,89E+08   | -3,83413  | 26,2177   | -0,08372    | ---      | ---     | --- | --- | --- | --- |
| 93 | 12,13205   | 0,61951   | 0,00672   | ---         | ---      | ---     | --- | --- | --- | --- |
| 94 | 0,02173    | -0,51337  | 0,20336   | -0,16334    | 0,59758  | 14,759  | --- | --- | --- | --- |
| 95 | 0,99713    | 0,24519   | 1,37408   | -0,56078    | 25,37448 | 0,48862 | --- | --- | --- | --- |

**Table 10.** Normalized correlation constants ( $a_n$ ) of  $V_R$ 

| DEC | $a_1$             | $a_2$             | $a_3$ | $a_4$              | $a_5$               | $a_6$             |
|-----|-------------------|-------------------|-------|--------------------|---------------------|-------------------|
| 1   | 0.871921182270907 | 0.999999957706903 | -1    | -0.999995743741039 | -0.234693648269660  | -1                |
| 2   | 0.871921182266641 | 0.999999957706812 | -1    | -0.999995443757433 | -0.670852573994134  | ---               |
| 3   | 0.871921182293410 | 0.999999957726314 | -1    | -0.999953927289804 | -0.633376565489139  | ---               |
| 4   | 0.871921182266746 | 0.999999957710086 | -1    | ---                | ---                 | ---               |
| 5   | 0.871921182266567 | 0.999999957706782 | -1    | -0.999994177664060 | -0.661519444802971  | 0.922902235485151 |
| 6   | 0.871921182261540 | 0.999999957707021 | -1    | -0.999995542234219 | -0.702085019639975  | 0.944302750059852 |
| 7   | 0.871921182268121 | 0.999999957706811 | -1    | -1                 | -0.0118942425114921 | 0.892353364618423 |
| 8   | 0.871921182266110 | 0.999999957706831 | -1    | -0.999995607948073 | 1                   | ---               |
| 9   | 0.871921182293892 | 0.999999957706831 | -1    | -0.999995328618578 | -0.668769801311492  | 0.923712846244111 |
| 10  | 0.871921182266005 | 0.999999957706803 | -1    | -0.999995565901712 | ---                 | ---               |
| 11  | 0.871921182266005 | 0.999999957706803 | -1    | -0.999995565901712 | ---                 | ---               |
| 12  | 0.871921182266396 | 0.999999957706809 | -1    | -0.999995727214433 | -0.653030753530205  | 0.880427468419803 |
| 13  | 0.871921182270718 | 0.999999957706844 | -1    | -0.999995782066287 | -0.663147496027327  | 0.880202664894057 |
| 14  | 0.871921182266266 | 0.999999957706807 | -1    | -0.999995781071042 | ---                 | ---               |
| 15  | 0.871921182266266 | 0.999999957706807 | -1    | -0.999995781071042 | ---                 | ---               |
| 16  | 0.871921182266266 | 0.999999957706807 | -1    | -0.999995781071042 | ---                 | ---               |

|    |                   |                   |                    |                    |                    |                   |
|----|-------------------|-------------------|--------------------|--------------------|--------------------|-------------------|
| 17 | 0.871921182266266 | 0.999999957706807 | -1                 | -0.999995781071042 | ---                | ---               |
| 18 | 0.871921182267611 | 0.999999957706806 | -1                 | -0.999995743205265 | -0.660668840815614 | 0.870817138034694 |
| 19 | 0.871921182391444 | 0.999999957706840 | -1                 | -0.999995431844896 | ---                | ---               |
| 20 | 0.871921182266946 | 0.999999957706560 | -1                 | -0.999995744111491 | -0.660743774229908 | ---               |
| 21 | 0.871921182266761 | 0.999999957706708 | -1                 | -0.999995529456371 | -0.678475664145720 | ---               |
| 22 | 0.871921182391444 | 0.999999957706840 | -1                 | -0.999995431844896 | ---                | ---               |
| 23 | 0.871921182266761 | 0.999999957706708 | -1                 | -0.999995529456371 | -0.678475664145720 | ---               |
| 24 | 0.871921182303973 | 0.999999957706823 | -1                 | -0.999995698623239 | ---                | ---               |
| 25 | 0.871921182303973 | 0.999999957706823 | -1                 | -0.999995698623239 | ---                | ---               |
| 26 | 0.871921182266729 | 0.999999957706838 | -1                 | -0.999995280611801 | -0.665133231506104 | ---               |
| 27 | 0.871921182278049 | 0.999999957706826 | -1                 | -0.999995774532831 | ---                | ---               |
| 28 | 0.871921182277737 | 0.999999957706878 | -1                 | -0.999977303797725 | -0.648887050680384 | 0.925326826533732 |
| 29 | 0.871921182268114 | 0.999999957707148 | -1                 | -0.999991452963643 | ---                | ---               |
| 30 | 0.871921182269092 | 0.999999957706816 | -1                 | ---                | ---                | ---               |
| 31 | 0.871921183643743 | 0.999999957713778 | -1                 | -0.999995591454642 | -0.655325942062989 | 0.884379063656295 |
| 32 | 0.871921182267198 | 0.999999957707141 | -1                 | -0.999994740398028 | -0.652887993357367 | ---               |
| 33 | 0.871921182279690 | 0.999999957707180 | -1                 | -0.999992164442593 | -0.656137250424440 | ---               |
| 34 | 0.871921182274968 | 0.999999957706843 | -1                 | -0.999995508625328 | -0.593171392157283 | 0.887026180091382 |
| 35 | 0.871921182266890 | 1                 | -1                 | ---                | ---                | ---               |
| 36 | 0.871921182266036 | 0.999999957706808 | -1                 | -0.999995571610551 | -0.597226470829530 | ---               |
| 37 | 0.871921182266004 | 0.999999957706825 | -1                 | ---                | ---                | ---               |
| 38 | 0.871921182245476 | 0.999999957706816 | -1                 | -0.999995870333512 | ---                | ---               |
| 39 | 0.871921182270948 | 0.999999957706825 | -1                 | -0.999995577576495 | ---                | ---               |
| 40 | 0.871921182266128 | 0.999999957706854 | -1,00E+00          | -0.999995634064976 | ---                | ---               |
| 41 | 0.871921182274463 | 0.999999957706818 | -1                 | ---                | ---                | ---               |
| 42 | 0.871921182264783 | 0.999999957706950 | -1                 | -0.999995803624413 | ---                | ---               |
| 43 | 0.871921182262626 | 0.999999957706932 | -1                 | -0.999995610510830 | -0.668492746246928 | 0.883822546784742 |
| 44 | 0.871921182279916 | 0.999999957706822 | -1                 | -0.999995683606089 | -0.523659938161644 | 0.885039154501166 |
| 45 | 0.871921182267321 | 0.999999957706820 | -1                 | -0.999995951056223 | ---                | ---               |
| 46 | 0.871921182264704 | 0.999999957706825 | -1                 | -0.999995674554884 | ---                | ---               |
| 47 | 0.871921182266620 | 0.999999957708260 | -1                 | -0.999995540099970 | -0.616844812062921 | 0.883944671320444 |
| 48 | 0.871921182269440 | 0.999999957706901 | ---                | ---                | ---                | ---               |
| 49 | 0.871921182266471 | 0.999999957706809 | -1                 | -0.999995727090027 | ---                | ---               |
| 50 | 0.871921182266933 | 0.999999957706809 | ---                | ---                | ---                | ---               |
| 51 | 0.871921182267067 | 0.999999957706840 | -1                 | -0.999995140942907 | -0.654755946468070 | ---               |
| 52 | 0.871921182266933 | 0.999999957706809 | ---                | ---                | ---                | ---               |
| 53 | 0.871921185496483 | 0.999999957702080 | -1                 | ---                | ---                | ---               |
| 54 | 0.871921182372765 | 0.999999957706837 | ---                | ---                | ---                | ---               |
| 55 | 0.871921182267033 | 0.999999957706759 | -1                 | -0.999995432900963 | -0.626208562579591 | ---               |
| 56 | 0.871921182341920 | 0.999999957706838 | ---                | ---                | ---                | ---               |
| 57 | 1,00E+00          | 0.999999957706085 | -1                 | -0.999995577576495 | -0.602021582286452 | ---               |
| 58 | 0.871921182298802 | 0.999999957706830 | -1                 | ---                | ---                | ---               |
| 59 | 0.871921182269073 | 0.999999957706538 | -1                 | -0.999995527341475 | ---                | ---               |
| 60 | 0.871921182280665 | 0.999999957706833 | ---                | ---                | ---                | ---               |
| 61 | 0.871921182280665 | 0.999999957706833 | ---                | ---                | ---                | ---               |
| 62 | 0.871921182266454 | 0.999999957706850 | -1                 | -0.999989979588261 | -0.640041772504453 | 0.888930948582601 |
| 63 | 0.871921182266662 | -1,00E+00         | -0.999999999999238 | -0.999995533578347 | -0.660302743534903 | ---               |

|    |                   |                   |          |                    |                    |                   |
|----|-------------------|-------------------|----------|--------------------|--------------------|-------------------|
| 64 | 0.871921183145243 | 0.999999957707145 | -1       | -0.999994811994890 | -0.643108973772782 | ---               |
| 65 | 0.871921182266933 | 0.999999957706809 | -1       | ---                | ---                | ---               |
| 66 | 0.871921225089869 | 0.999999957707004 | -1       | -0.999995734886118 | -1                 | ---               |
| 67 | 0.871921182266921 | 0.999999957707135 | -1       | ---                | ---                | ---               |
| 68 | 0.871921182266932 | 0.999999957707378 | -1       | -0.999995583506500 | ---                | ---               |
| 69 | 0.871921182266760 | 0.999999957707872 | -1       | ---                | ---                | ---               |
| 70 | 0.871921524393556 | 0.999999957706996 | -1       | 1                  | ---                | ---               |
| 71 | 0.871921182276069 | 0.999999957706825 | ---      | ---                | ---                | ---               |
| 72 | 0.871921182276171 | 0.999999957706825 | ---      | ---                | ---                | ---               |
| 73 | 0.871921182267055 | 0.999999957706825 | ---      | ---                | ---                | ---               |
| 74 | -1,00E+00         | 0.999999957702754 | -1       | ---                | ---                | ---               |
| 75 | 0.871921182266135 | 0.999999957706825 | ---      | ---                | ---                | ---               |
| 76 | 0.871921183328809 | 0.999999957706831 | -1       | -0.999995622976281 | -0.643081644501042 | ---               |
| 77 | 0.871921182266433 | 0.999999957706811 | -1       | -0.999995743685747 | -0.657523518588869 | ---               |
| 78 | 0.871921182266150 | 0.999999957705896 | 1,00E+00 | -0.999994878142782 | -0.818219584166580 | ---               |
| 79 | 0.871921182366765 | 0.999999957710122 | ---      | ---                | ---                | ---               |
| 80 | 0.871921182270504 | 0.999999957706804 | -1       | -0.999995380965731 | -0.668780774824045 | 0.895540237329223 |
| 81 | 0.871921182267366 | 0.999999957707197 | -1       | -0.999990047168201 | -0.644516248375528 | ---               |
| 82 | 0.871921182266010 | 0.999999957706805 | ---      | ---                | ---                | ---               |
| 83 | 0.871921182606765 | 0.999999957706847 | ---      | ---                | ---                | ---               |
| 84 | 0.871921182297033 | 0.999999957706847 | -1       | ---                | ---                | ---               |
| 85 | 0.87192118228984  | 0.999999957708176 | ---      | ---                | ---                | ---               |
| 86 | 0.872448723690103 | 0.999999957706692 | -1       | -0.999995766192120 | ---                | ---               |
| 87 | 0.871921182267493 | 0.999999957706817 | -1       | -0.999995032441786 | -0.660824142145656 | 0.881471588450892 |
| 88 | 0.871921182277827 | 0.999999957707006 | -1       | -0.999990321322419 | ---                | ---               |
| 89 | 0.871921171568949 | 0.999999957708271 | -1       | ---                | ---                | ---               |
| 90 | 0.871921182267436 | 0.999999957709050 | ---      | ---                | ---                | ---               |
| 91 | 0.871921182266454 | 0.999999957707648 | -1       | -0.999993937489185 | ---                | ---               |
| 92 | 0.872448723690103 | 0.999999957706692 | -1       | -0.999995766192120 | ---                | ---               |
| 93 | 0.871921182276876 | 0.999999957706825 | -1       | ---                | ---                | ---               |
| 94 | 0.871921182266029 | 0.999999957706792 | -1       | -0.999995788203635 | -0.657584708985060 | 1                 |
| 95 | 0.871921182266903 | 0.999999957706814 | -1       | -0.999995898078747 | -0.528113459849224 | 0.883893169101191 |

The best performing model was selected based on the smallest reduced chi-Sqr, residual sum of residual ( $\approx 0$ ) and the DEC were classed according to adjusted R-squared. such us, the minimum value of adjusted R-squared that was taken greater than or equal 0.97. The parameters of optimizing models are presented in the Tables 5–10.

### 3.2. Graphical performance of the regression results

#### 3.2.1. Fitted curves plot

The Figure 2 indicates the validation of the best-fit correlation (DEC 1) to follow the scatterplot of each data points:alimentation, permeate and rejection witch it presented by graphics A,B and C respectively. So, the fit DEC 1 is closely related by thethe area of 95% confidence bands and followed the 95% prediction bands. Also, DEC 1 predicted adequately scatterplot of each data points A, B and C. thus, this includes both the uncertainty in the true

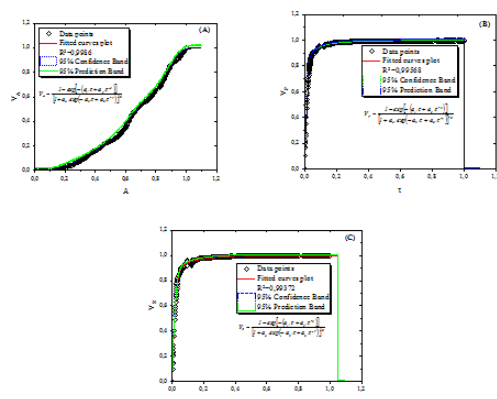
position of DEC 1 (enclosed by the confidence bands), and also accounts for scatter of data around the three graphs (A, B and C).

#### 3.2.2. Residual plots

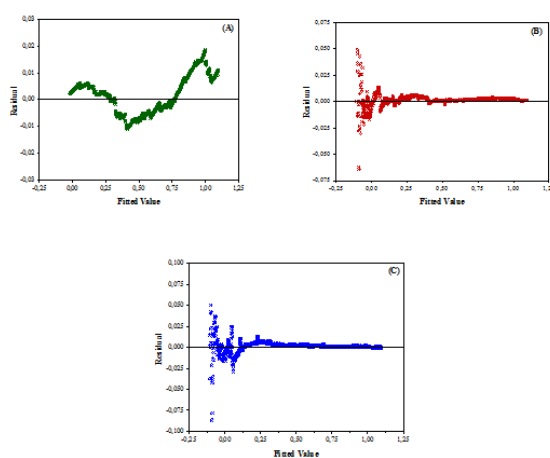
Figure 3 below present residuals plot versus fits values using DEC 1. These residual plots can be used to assess the quality of the correlation regression. Such us,

$$\text{The Residual Value} = \text{Observed Value of } V - \text{Predicted Value of } V \quad (5)$$

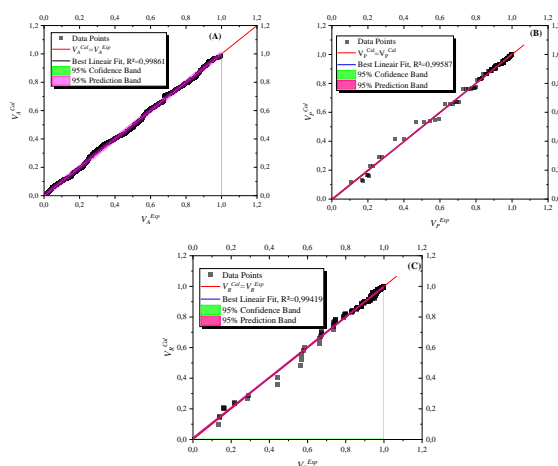
where: V: cumulative dimensionless volume of the filtrate at time  $\tau$ .



**Figure 3.** Fitted curves plot of DEC 1 of the filtrate at time  $\tau$  versus data points for the alimentation (A), permeate (B) and rejection (C).



**Figure 4.** Residuals values vs. Fits Plot using DEC 1 for the alimentation (A), permeate (B) and rejection (C).



**Figure 5.** Scatter plot of the predicted values of alimentation (A), permeate (B) and rejection (C) versus experimental values by DEC 1 correlation for the validation set.

The underlying statistical assumptions were considered about residuals to Adj. R-Square. For these assumptions to hold true for a particular regression model, the residuals would have to be randomly distributed around zero (Figure 4). The scatter plot (A, B and C) of the residuals disordered the excellent regression. How over, the

maximum residual values for the three graphics A, B and C move away to the zero line by 0,075 in absolute value. This result was argument by the regression equation, line of DEC 1 i.e., predicted vs experimental validation results which it indicates excellent significant of DEC 1 for the prediction of cumulative dimensionless volume (Figure 5).

#### 4. Conclusion

The novel dimensionless empirical correlation proposed in this study the kinetic separation performance of three cumulative dimensionless volume: alimentation, permeate and rejection as a function of the dimensionless filtration time and vice versa. Results show that 95 correlations as a whole correlates with the experimental data with a least  $R^2$  was around 0.96796 and COD of 0.96797 in comparison to the best correlation with  $R^2$  of 0.99796 and COD of 0.99796 for negligible errors and perfect alignment of correlation to RO kinetic separation according to statistical criteria.

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